

GOODYEAR AEROSPACE

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AND FIVE DEGREES OF (Goodyear Aerospace
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GOODYEAR AEROSPACE CORPORATION

AKRON 15, OHIO

USERS MANUAL

DYNAMICS OF TWO BODIES CONNECTED

BY AN ELASTIC TETHER - SIX DEGREES OF FREEDOM FOREBODY

AND FIVE DEGREES OF FREEDOM DECELERATOR
(REF. NASA CONTRACT NAS8-29144 S/A1)

BY

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ABSTRACT

One important aspect to recovering a body falling through the atmosphere, is to decelerate and stabilize it. This is usually accomplished by means of a parachute. The design of the recovery system necessitates a knowledge of the dynamics and loads during parachute deployment and inflation. In many cases, a pitch plane analysis will provide adequate information. However, if the body is in a general tumbling motion, it is necessary to analyze its motion in three dimensions.

This report contains the equations of motion and a computer program for the dynamics of a six degree of freedom body joined to a five degree of freedom body by a quasilinear elastic tether. The forebody is assumed to be a completely general rigid body with six degrees of freedom; the decelerator is also assumed to be rigid, but with only five degrees of freedom (symmetric about its longitudinal axis). The tether is represented by a spring and dashpot in parallel, where the spring constant is a function of tether elongation. Lagrange's equation is used to derive the equations of motion with the Lagrange multiplier technique used to express the constraint provided by the tether. A computer program is included which provides a time history of the dynamics of both bodies and the tension in the tether.

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NOMENCLATURE

The following is a list of variables used in the computer program and in the derivation of the equations as discussed in this report. A brief description and associated units are included.

<u>FORTTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
A	a	Distance along the longitudinal axis of the forebody (X_b) from the intersection of the body axes to the tether-forebody confluence point, positive towards the nose	(m)	ft
AA(6,4)		Dummy variables used to express incremental velocities of the forebody in the Runge-Kutta integration	(m/sec)	ft/sec or rad/sec
AALPDE(8)		An array of eight variables signifying angle-of-attack of the forebody used with damping coefficients		deg
AALPFE(16)		An array of sixteen variables signifying angle-of-attack of the forebody used with force coefficients		deg
AALPME(16)		An array of sixteen variables signifying angle-of-attack of the forebody used with moment coefficients		deg
AALPPE(8)		An array of eight variables signifying angles of attack of the decelerator		deg
AAM(8)		An array of eight variables signifying Mach number of the forebody used with force and moment coefficients		
AAMD(8)		An array of eight variables signifying Mach number of the forebody used with damping coefficients		
AAMP(8)		An array of eight variables signifying Mach number of the decelerator		
AERATO		Suspension Line AE Ratio (AERATO = AE/AE_{Nylon})		

<u>FORTTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
AIPHI		Number of elements in PPHIE array (= 2 to 8)		
AIPHID		Number of elements in PPHIDE array (= 2 to 8)		
AJALPD		Number of elements in AALPDE array (= 8)		
AJALPF		Number of elements in AALPFE array (= 8 or 16)		
AJALPM		Number of elements in AALPME array (= 8 or 16)		
AKAM		Number of elements in AAM array (= 2 to 8)		
AKAMD		Number of elements in AAMD array (= 2 to 8)		
ALPE	α	Angle-of-attack of the forebody		deg
ALPPE	α_p	Angle-of-attack of the decelerator		deg
AM		Mach number of the forebody		
AMAX1		Larger ordinate of two points on the longitudinal added mass versus D_o log log plot	kg	slug
AMAX2		Smaller ordinate of two points on the longitudinal added mass versus D_o log log plot	kg	slug
AMAY1		Larger ordinate of two points on the lateral added mass versus D_o log log plot	kg	slug

<u>FORTTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
AMAY2		Smaller ordinate of two points on the lateral added mass versus D_o log log plot	kg	slug
AMP		Mach number of the decelerator		
AP	a_p	Distance along the longitudinal axis of the decelerator (X_{pb}) from the c.g. to the tether-decelerator confluence point	(m)	ft
AX		Exponent of longitudinal added mass equation (MPAL = RH000 * BX * DS ** AX)		
AY		Exponent of lateral added mass equation (MPAS = RH000 * BY * DS ** AY)		
B	b	Distance along the lateral axis of the forebody (Y_b) from the intersection of the body axes to the tether-forebody confluence point, positive towards the left wing	(m)	ft
BB(5,4)		Dummy variables used to express incre- mental velocities of the decelerator in the Runge-Kutta integration	(m/sec)	ft/sec or rad/sec
BX		Coefficient of longitudinal added mass equation (MPAL = RH000 * BX * DS ** AX)		
BY		Coefficient of lateral added mass equation (MPAS = RH000 * BY * DS ** AY)		
C	c	Distance along the vertical axis of the forebody (Z_b) from the intersection of the body axes to the tether-forebody confluence point, positive up	(m)	ft

<u>FORTTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
CA	C_A	Axial force coefficient of forebody		
CAP	C_{AP}	Axial force coefficient of decelerator		
CC(3,3)	C_{ij}	Elements of transformation matrix from inertial coordinates to body coordinates of the forebody		
CAA(8,16,8)		A three dimensional array of variables signifying axial force coefficients of the forebody corresponding to AAM(8), AALPFE(16), and PPHIE(8)		
CCAP(8,8)		A two dimensional array of 64 variables signifying axial force coefficients of the decelerator with respect to angle of attack corresponding to AAMP(1) thru AAMP(8)		
CCHI	C_χ	$\cos(\chi)$		
CCHIP	C_{χ_p}	$\cos(\chi_p)$		
CCLL(8,16,8)		A three dimensional array of variables signifying rolling moment coefficients of the forebody corresponding to AAM(8), AALPME(16), and PPHIE(8)		
CCLLP(8,8,8)		A three dimensional array of variables signifying roll damping coefficients of the forebody corresponding to AAMD(8), AALPDE(8), and PPHIDE(8)		
CCLM(8,16,8)		A three dimensional array of variables signifying pitching moment coefficients of the forebody corresponding to AAM(8), AALPME(16), and PPHIE(8)		

<u>FORTTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
CCLMQ(8,8,8)		A three dimensional array of variables signifying pitch damping coefficients of the forebody corresponding to AAMD(8), AALPDE(8), and PPHIDE(8)		
CCLN(8,16,8)		A three dimensional array of variables signifying yawing moment coefficients of the forebody corresponding to AAM(8), AALPME(16), and PPHIE(8)		
CCLNR(8,8,8)		A three dimensional array of variables signifying yaw damping coefficients of the forebody corresponding to AAM(8), AALPDE(8), and PPHIDE(8)		
CCN(8,16,8)		A three dimensional array of variables signifying normal force coefficients of the forebody corresponding to AAM(8), AALPFE(16), PPHIE(8)		
CCM(8,8)		A two dimensional array of 64 variables signifying the pitching moment coefficients of the decelerator with respect to angle of attack corresponding to AAMP(1) thru AAMP(8)		
CCNP(8,8)		A two dimensional array of 64 variables signifying the normal force coefficient of the decelerator with respect to angle of attack corresponding to AAMP(1) thru AAMP(8)		
CCP(3,3)	C _{pij}	Elements of transformation matrix from inertial coordinates to body coordinates of the decelerator		

<u>FORTTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNIT S</u>	<u>ENGLISH UNITS</u>
CCRIT		c/cr = damping ratio = 0.06		
CCY(8,16,8)		A three dimensional array of variables signifying side force coefficients of the forebody corresponding to AAM(8), AALPFE(16), and PPHIE(8)		
CDAP		Drag area of decelerator	(m ²)	ft ²
	c.g.	Center of gravity		
CGAM	C _γ	Cos(γ)		
CGAMP	C _{γ_p}	Cos(γ _p)		
CHIE	χ	Flight path angle of forebody in horizontal plane, measured from X axis toward Y axis		deg
CHIE	χ _p	Flight path angle of decelerator in horizontal plane, measured from X axis toward Y axis		deg
CLL	C _l	Rolling moment coefficient of the forebody		
CLLP	C _{l_p}	Rolling damping coefficient of the forebody		
CLM	C _m	Pitching moment coefficient of the forebody		
CLMQ	C _{m_q}	Pitch damping coefficient of the forebody		
CLN	C _n	Yawing moment coefficient of the forebody		
CLNR	C _{n_r}	Yaw damping coefficient of the forebody		

<u>FORTTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
CN	C_N	Normal force coefficient of the forebody		
CNP	C_{Np}	Normal force coefficient of the decelerator		
COM(20)		Input variable used to define computer simulation - up to eighty figures		
CPHI	C_ϕ	$\cos(\phi)$		
CPHII	C_{ϕ_i}	$\cos(\phi_i)$		
CPHIPI	$C_{\phi_{pi}}$	$\cos(\phi_{pi})$		
CPSI	C_ψ	$\cos(\psi)$		
CPSIP	C_{ψ_p}	$\cos(\psi_p)$		
CS	C_s	Damping coefficient of tether	$\frac{N\text{-sec}}{m}$	$\frac{lb_f\text{-sec}}{ft}$
CSIGP		Cosine of one half the apex angle of the cone formed by the suspension lines		
CTHE	C_θ	$\cos(\theta)$		
CTHEP	C_{θ_p}	$\cos(\theta_p)$		
CY	C_Y	Side force coefficient of forebody		
D	d	Aerodynamic reference length of forebody	(m)	ft
DI(6,6)		A two dimensional array of variables signifying the coefficients of the second derivatives in the equations of motions	(kg) (kg-m ²)	slug or slug-ft ²
DDP(3,3)		A two dimensional array of variables signifying the coefficients of the second derivatives in the equations of motion of the decelerator	(kg) (kg-m ²)	slugs or slug-ft ²
DELSX		Total suspension line deflection array	m	ft

<u>FORTTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
DELTX		Total tether line deflection array	m	ft
DLTO		Initial elongation of tether beyond unstretched length. DLTO is negative if the forebody and decelerator confluence points are closer together than LTO	(m)	ft
DLTX		Tether deflection component in array element (DLX(I) associated with load PX(I)	m	ft
DLX		Effective spring deflection array	m	ft
DMD		Rate of change of longitudinal added mass	kg/sec	slug/sec
DP	d_p	Aerodynamic reference length of decelerator	(m)	ft
DPR		Degress per radian - 57.2957795		
DS		Parachute diameter associated with SP	m	ft
DSP		Parachute projected diameter associated with DS	m	ft
DSX1		Larger abscissa of two points on the longitudinal added mass versus D_o log log plot	m	ft
DSX2		Smaller abscissa of two points on the longitudinal added mass versus D_o log log plot	m	ft
DSY1		Larger abscissa of two points on the lateral added mass versus D_o log log plot	m	ft

<u>FORTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
DSY2		Smaller abscissa of two points on the lateral added mass versus D_0 log log plot	m	ft
DT		Integration increment		sec
DTP		Number of integrations between data output		
DTF1		Number of integrations between data output when $T \leq TDTC$		
DT1		Integration increment when $T \leq TDTC$		sec
DTT		Estimated parachute system period/12	sec	sec
DYPR	q	Dynamic pressure of forebody	(N/m ²)	lb _f /ft ²
DYPRP	q _p	Dynamic pressure of decelerator	(N/m ²)	lb _f /ft ²
EE(6)		An array signifying the nonhomo- geneous terms in the six equations of motion of the forebody	(N/m) (N)	ft-lb _f or lb _f
EPL		Suspension line strain array	m/m	ft/ft
EPS		Number used to check for inconsistent equations in PIVERT Subroutine, 10^{-13}		
EPSI		Number used to check if θ is approaching a singular point $\theta = \frac{2n+1}{2}\pi$. If θ is approaching a singular point, the accelerations are kept fixed until this region is passed. EPSI = 0.0000061 freezes the accelerations if θ is within 0.2° of a singular point.		
EPT		Tether line strain array	m/m	ft/ft

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<u>FORTTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
ETAI		Number which controls DT if θ is near a singular point. $ETAI = 0.00061$ sets $DT = \frac{DT1}{5}$, if θ is within 2° of a singularity		
FF(5)		An array signifying the accelerations of the decelerator	(m/sec)	ft/sec or rad/sec
FREQP		Estimated parachute system frequency	1/sec	1/sec
FSULT		Ultimate design factor of safety for parachute		
FX	F_x	Generalized force on forebody in X direction	(N)	lb _f
FXB	F_{xb}	Body force in direction of X_b due to aerodynamics	(N)	lb _f
FXP	F_{xp}	Generalized force on decelerator in X direction	(N)	lb _f
FXPB	F_{xpb}	Body force in direction of X_{pb}	(N)	lb _f
FY	F_y	Generalized force on forebody in Y direction	(N)	lb _f
FYB	F_{yb}	Body force in direction of Y_b due to aerodynamics	(N)	lb _f
FYP	F_{yp}	Generalized force on decelerator in Y direction	(N)	lb _f
FYPB	F_{ypb}	Body force in direction of Y_{pb}	(N)	lb _f
FZ	F_z	Generalized force on forebody in Z direction	(N)	lb _f
FZB	F_{zb}	Body force in direction of Z_b due to aerodynamics	(N)	lb _f

<u>FORTTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
FZP	F_{zp}	Generalized force on decelerator in Z direction	(N)	lb _f
FZPB	F_{zpb}	Body force in direction of Z_{pb}	(N)	lb _f
G	g	Acceleration of gravity at Z	(m/sec ²)	ft/sec ²
GAME	γ	Flight path angle of forebody in vertical plane		deg
GAMPE	γ_p	Flight path angle of decelerator in vertical plane		deg
GLOAD		Limit design load factor of forebody		
GO		Acceleration of gravity at earth's surface, 32.17	(m/sec ²)	ft/sec ²
HHH		Altitude below which simulation is ended	(m)	ft
ICXO		Canopy roll moment of inertia about its C.M.	kg-m ²	slug-ft ²
ICYO		Canopy pitch moment of inertia about its C.M.	kg-m ²	slug-ft ²
IERSW		Variable signifying whether or not the equations being solved in sub- routine PIVER are consistent		
ILXO		Parachute lines roll moment of inertia about its C.M.	kg-m ²	slug-ft ²
ILYO		Parachute lines pitch moment of inertia about its C.M.	kg-m ²	slug-ft ²
IXB	I_{xb}	Moment of inertia about X_b axis	(kg-m ²)	slug-ft ²

<u>FORTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
IXPB	I_{xpb}	Apparent moment of inertia about X_{pb} axis	$(kg-m^2)$	slug-ft ²
IXYB	I_{xyb}	Product of inertia associated with X_b and Y_b axes	$(kg-m^2)$	slug-ft ²
IXZB	I_{xzb}	Product of inertia associated with X_b and Z_b axes	$(kg-m^2)$	slug-ft ²
IYB	I_{y_b}	Moment of inertia about Y_b axis	$(kg-m^2)$	slug-ft ²
IYPB	I_{ypb}	Apparent moment of inertia about Y_{pb} axis	$(kg-m^2)$	slug-ft ²
IYZB	I_{yzb}	Product of inertia associated with Y_b and Z_b axes	$(kg-m^2)$	slug-ft ²
IZB	I_{zb}	Moment of inertia about Z_b axis	$(kg-m^2)$	slug-ft ²
KS	K_s	Tether spring constant	(N/m)	lb _f /ft
LS		Suspension line length	m	ft
LSCL		Distance along parachute centerline between the confluence point and the projected diameter plane	m	ft
LT	L_T	Tether length - distance between confluence points	(m)	ft
LTD	\dot{L}_T	Time rate of change of tether length	(m/sec)	ft/sec
LTO	L_{TO}	Unstretched tether length	(m)	ft
M	m	Mass of forebody	(kg)	slugs
MP	m_p	Real mass of decelerator	(kg)	slugs
MPAL		Added mass of the decelerator along X_{pb} axis	(kg)	slugs

<u>FORTTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
MPAS		Added mass of the decelerator along Y_{pb} or Z_{pb} axis	(kg)	slugs
MPL	m_{pl}	Apparent longitudinal (X_{pb}) mass of decelerator	(kg)	slugs
MPS	m_{ps}	Apparent side (Y_{pb} or Z_{pb}) mass of decelerator	(kg)	slugs
NS		Number of parachute suspension lines		
NT		Number of tether lines		
OMETRC		Option variable: if OMETRC = 1., Input and Output are in the metric system. If OMETRC = 0.0 Input and Output are in the English system.		
OMXBE	ω_{xb}	Angular velocity about X_b axis		deg/sec
OMYBE	ω_{yb}	Angular velocity about Y_b axis		deg/sec
OMZBE	ω_{zb}	Angular velocity about Z_b axis		deg/sec
OPAM		Option variable: if OPAM = 1., added mass of the decelerator $\neq 0$; if OPAM = 0., added mass of decelerator = 0		
OPDA		Option variable: if OPDA = 1., damping moment coefficients of the forebody are read in as arrays; if OPDA = 0., damping moment coefficients are read in as constants		
OPOS		Option variable: if OPOS = 1., at least one of the c.g. offsets or products of inertia of the forebody $\neq 0$.; if OPOS = 0., all c.g. offsets and products of inertia = 0.		

<u>FORTTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
OPPLOT		Option variable: if OPPLOT = 1., a plot tape can be made; if OPPLOT = 0., no plot tape is made.		
OPPRIN		Option variable: if OPPRIN = 1., all aerodynamic coefficient arrays are printed out; if OPPRIN = 0, no aerodynamic coefficient arrays are printed out		
OPDT		Option for automatic DT determination (OPDT = 1)		
OPSP		Option for automatic parachute area calculations (OPSP = 1)		
OPSYM		Option variable: if OPSYM = 1., the forebody is aerodynamically symmetric such that $C_y = C_m = 0$; if OPSYM = 0, the forebody is not symmetric		
PCT01		Parachute overinflation at reefed stage (I). (percent/100)		
PCT01		Parachute overinflation at reefed stage 1. (percent/100)		
PCT02		Parachute overinflation at reefed stage 2. (percent/100)		
PCT03		Parachute overinflation at reefed stage 3. (percent/100)		
PHIAE		Aerodynamic roll angle of forebody, $0 \leq \text{PHIAE} \leq 180^\circ$		deg
PHIDDE	0	Angular acceleration about X_b axis		deg/sec ²
PHIDE	0	Angular velocity about X_b axis		deg/sec ²

<u>FORTTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
PHIE	\emptyset	Euler angle rotation about X_b axis		deg
PHIE	\emptyset_i	Aerodynamic roll angle of forebody, $-180^\circ \leq \emptyset_i \leq 180^\circ$		deg
PHIPI	\emptyset_{pi}	Aerodynamic roll angle of decelerator, $-180^\circ \leq \emptyset_{pi} \leq 180^\circ$		deg
POROS		Parachute porosity. Use POROS = 0.15		
PPHIDE(8)		An array of eight variables signifying forebody roll angle used with damping coefficients		deg
PPHIE(8)		An array of eight variables signifying forebody roll angle used with force and moment coefficients		deg
PSIDDE	$\ddot{\psi}$	Angular acceleration of forebody about -Z axis		deg/sec ²
PSIDE	$\dot{\psi}$	Angular velocity of forebody about -Z axis		deg/sec
PSIE	ψ	Euler angle rotation of forebody about -Z axis		deg
PSIPDE	$\dot{\psi}_p$	Angular velocity of decelerator about -Z axis		deg/sec
PSIPE	ψ_p	Angular rotation of decelerator about -Z axis		deg
PSPDDE	$\ddot{\psi}_p$	Angular acceleration of decelerator about -Z axis		deg/sec ²
PULAN		Angle between tether and forebody centerline	deg	deg
PS		Suspension line load array	N	lb _f

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<u>FORTTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
PSX		Total suspension line load array	N	lb _f
PT		Tether line load array	N	lb _f
PTX		Total tether line array	N	lb _f
PX		Effective spring load array	N	lb _f
QMAXPB		Parachute load due to rate of change of mass of the parachute times the relative velocity, XPBDR	N	lb _f
QPHI	Q_{θ}	Generalized force about X_b axis	(m-N)	ft-lb _f
QPSI	Q_{ψ}	Generalized force of forebody about -Z axis	(m-N)	ft-lb _f
QPSIP	$Q_{\psi p}$	Generalized for of decelerator about -Z axis	(m/N)	ft/lb _f
QTHE	Q_{θ}	Generalized force of forebody about negative line of modes	(m/N)	ft/lb _f
QTHER	$Q_{\theta p}$	Generalized force of decelerator about negative line of modes	(m/N)	ft/lb _f
RATIO		Nondimensional length used in the decelerator's body torque expressions		
RE		Radius of earth - 20,926,435.	(m)	ft
RHO		Density of atmosphere at Z (1962 Standard)	(kg/m ²)	slug/ft ²
RHOOO		Air density ratio (RHO/RHOO)		
S	S	Aerodynamic reference area of forebody	(m ²)	ft ²
SCHI		sin (χ)		
SCHIP		sin (χ_p)		
SGAM		sin (γ)		

<u>FORTTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
SGAMP		$\sin(\gamma_p)$		
SP		Parachute drag area	m^2	ft^2
SPD		Time rate of change of parachute drag area	m^2/sec	ft^2/sec
SPHI	$S\theta$	$\sin(\theta)$		
SPHII	$S\theta_i$	$\sin(\theta_i)$		
SPHIPI	$S\theta_{pi}$	$\sin(\theta_{pi})$		
SPR0		Initial parachute area	m^2	ft^2
SPR1		First reefed stage parachute drag area	m^2	ft^2
SPR2		Second reefed stage parachute drag area	m^2	ft^2
SPR3		Third reefed stage parachute drag area	m^2	ft^2
SPRL		Parachute drag area associated with reefed stage (I-1)	m^2	ft^2
SPRU		Parachute drag area associated with reefed stage (I)	m^2	ft^2
SPSI	$S\psi$	$\sin(\psi)$		
SPSIP	$S\psi_p$	$\sin(\psi_p)$		
SSP(16)		An array of sixteen variables signifying aerodynamic reference area of the decelerator corresponding to TTIP(16)	(M^2)	ft^2
STHE	$S\theta$	$\sin(\theta)$		
STHEP	$S\theta_p$	$\sin(\theta_p)$		
T		Flight time		sec
TENS		Tension in tether	N	lb_f
THEDDE	$\ddot{\theta}$	Angular acceleration of forebody about negative line of nodes		deg/sec^2

<u>FORTTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
THEDE	$\dot{\theta}$	Angular velocity of forebody about negative line of nodes		deg/sec ²
THEE	θ	Euler angle rotation of forebody about negative line of nodes		deg
THEPDE	$\dot{\theta}_p$	Angular velocity of decelerator about negative line of nodes		deg/sec
THEPE	θ_p	Euler angle rotation of decelerator about negative line of nodes		deg
THPDDE	$\ddot{\theta}_p$	Angular acceleration of decelerator about negative line of nodes		deg/sec ²
TFI		Parachute inflation time from Stage (I) to Stage (I + 1)	sec	sec
TINF		Time when inflated area first equals SPRU	sec	sec
TINT		Time at start of inflation of reefed stage (I)	sec	sec
TNINY		Total time spent in region where (1-ABS(SIN(THI))). LT.EPSI	sec	sec
TO		Initial time	sec	sec
TOIF		One half the time spent in the over- inflation of stage I	sec	sec
TOTRO		Time at start of inflation of first reefed stage	sec	sec
TOTR1		Time at start of inflation of second reefed stage	sec	sec
TOTR2		Time at start of inflation of third reefed stage	sec	sec

<u>FORTTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
TOTR3		Time at end . third reefed stage	sec	sec
TPD		Total tether load (tension + damping)	N	lb _f
TPDRB		Component of tether load normal to forebody centerline	N	lb _f
TPDXB		Tether load component along forebody XB axis	N	lb _f
TPDYB		Tether load component along forebody YB axis	N	lb _f
TPDZB		Tether load component along forebody ZB axis	N	lb _f
TRO		Time from "TO" to start of inflation of first stage	sec	sec
TR1		Time from "TO" to start of inflation of second stage	sec	sec
TR2		Time from "TO" to start of inflation of third stage	sec	sec
TR3		Time from "TO" to end of third stage (TR3 > TTT)	sec	sec
TTIP(16)		An array of sixteen variables signifying inflation time events		sec
TXB	T _{xb}	Torque about X _b axis due to aerodynamics	(m-N)	ft-lb _f
TTT		Flight time at which simulation is ended		sec
TYB	T _{yb}	Torque about Y _b axis due to aerodynamics	(m-N)	ft-lb _f
TYPB	T _{ypb}	Torque about X _{pb} axis due to aero- dynamics	(m-N)	ft-lb _f
TZB	T _{xb}	Torque about Z _b axis due to aerodynamics	(M-N)	ft-lb _f

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<u>FORTTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
TZPB	T_{zpb}	Torque about Z_{pb} axis due to aerodynamics	(m-N)	ft-lb _f
V		Total velocity of forebody	(m/sec)	ft/sec
VP		Total velocity of decelerator	(m/sec)	ft/sec
VS		Speed of sound at Z	(m/sec)	ft/sec
WT		Weight of forebody	(N)	lb
WTC		Parachute canopy weight	kg·m/sec ²	lb
WTCM		Mass of parachute canopy	kg	slug
WTL		Parachute suspension lines weight	kg·m/sec ²	lb
WFLM		Mass of parachute suspension lines	kg	slug
WTP		Weight of decelerator	(N)	lb
X	X	Down range inertial axis or displacement of forebody	(m)	ft
	X_b	Longitudinal body axis or displacement of forebody	(m)	ft
XBAR	\bar{X}	c.g. offset along X_b axis	(m)	ft
XBD	X_b	X_b body axis velocity	(m/sec)	ft/sec
X	\dot{X}	Down range velocity of forebody	(m/sec)	ft/sec
XDD	\ddot{X}	Down range acceleration of forebody	(m/sec ²)	ft/sec ²
XP	X_p	Down range displacement of decelerator	(m)	ft
XPBD	\dot{X}_{pb}	X_{pb} body axis velocity of decelerator	(m/sec)	ft/sec
XPBDR		Velocity of air entering or exiting the parachute relative to the parachute velocity	m/sec	ft/sec

<u>FOPIRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
XPBDI		Parachute velocity, XPBD, at $T = TINT$. It is used to calculate fill time	m/sec	ft/sec
XPB	\dot{X}_p	Down range velocity of decelerator	(m/sec)	ft/sec
XPDD	\ddot{X}_p	Down range acceleration of decelerator	(m/sec ²)	ft/sec ²
Y	Y	Cross range inertial axis or displacement of forebody	(m)	ft
	Y_b	Lateral body axis or displacement of forebody	(m)	ft
YBAR	\bar{Y}	c.g. offset along Y_b axis	(m)	ft
YBD	\dot{Y}_b	Y_b body axis velocity	(m/sec)	ft/sec
YD	\dot{Y}	Cross range velocity of forebody	(m/sec)	ft/sec
YDD	\ddot{Y}	Cross range acceleration of forebody	(m/sec ²)	ft/sec ²
YP	Y_p	Cross range inertial displacement of decelerator	(m)	ft
YPBD	\dot{Y}_{pb}	Y_{pb} body axis velocity of decelerator	(m/sec)	ft/sec
YPD	\dot{Y}_p	Cross range velocity of decelerator	(m/sec)	ft/sec
YPDD	\ddot{Y}_p	Cross range acceleration of decelerator	(m/sec ²)	ft/sec ²
Z		Vertical inertial axis or displacement of forebody	(m)	ft
	Z_b	Vertical body axis or displacement of forebody	(m)	ft

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<u>FORTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
ZBAR	\bar{Z}	c.g. offset along Z_b axis	(m)	ft
ZBD	\dot{Z}_b	Z_b body axis velocity	(m/sec)	ft/sec
ZD	\dot{Z}	Vertical velocity of forebody	(m/sec)	ft/sec
ZDD	\ddot{Z}	Vertical acceleration of forebody	(m/sec ²)	ft/sec ²
ZP	Z_p	Vertical inertial displacement of decelerator	(m)	ft
ZPBD	\dot{Z}_{pb}	Z_{pb} body axis velocity of decelerator	(m/sec)	ft/sec
ZPD	\dot{Z}_p	Vertical velocity of decelerator	(m/sec)	ft/sec
ZPDD	\ddot{Z}_p	Vertical acceleration of decelerator	(m/sec ²)	ft/sec ²

CHAPTER I - INTRODUCTION

The system to be simulated is two rigid bodies joined by an elastic tether. The forebody may have a completely general shape and mass characteristics, and will be free to move with six degrees of freedom (three translational, three rotational). The decelerator is assumed to be symmetric in shape and mass characteristics about its longitudinal (roll) axis, and will be free to move with five degrees of freedom (three translational, two rotational). A frictionless swivel is assumed at the decelerator-tether confluence point. Thus the roll motions of the forebody will not couple with the decelerator. The tether is simulated by a spring and dashpot in parallel. Damping coefficients for tether lines are difficult to obtain; but spring constants for a tether can be found from experimental stress strain curves. Consequently; the damping coefficient is assumed constant, while the spring constant is assumed to be a function of elongation in the computer program, thereby introducing a quasilinear spring.

CHAPTER II DERIVATION OF EQUATIONS OF MOTION

SECTION 1 - COORDINATE SYSTEM

Figure 1 shows the different coordinate systems used to derive the equations of motion. $\bar{X}\bar{Y}\bar{Z}$ is an inertial orthogonal coordinate system attached to a flat non-rotating earth. XYZ and $X_p Y_p Z_p$ are orthogonal axes fixed to the forebody and decelerator at "O" and "O_p" respectively. Coordinate systems XYZ and $X_p Y_p Z_p$ translate with the bodies but do not rotate, always remaining parallel to corresponding inertial axes. The displacements X, Y, Z, X_p, Y_p, Z_p , as measured from the origin of $\bar{X}\bar{Y}\bar{Z}$, are the six translational degrees of freedom of the two bodies. The reference forebody body axes, longitudinal (X_b), lateral (Y_b), and vertical (Z_b), intersect at "O", the origin of the aerodynamics load system of the forebody. The reference decelerator body axes, longitudinal (X_{pb}), lateral (Y_{pb}), and vertical (Z_{pb}) intersect at "O_p", the c.g. of the decelerator. The variables $\bar{X}, \bar{Y}, \bar{Z}$ are the distances from "O" to the c.g. of the forebody measured positively in the direction of the positive body axes X_b, Y_b, Z_b respectively. For orientation purposes, the reader should position himself as a pilot in an airplane. In this position, X_b is positive toward the nose, Y_b is positive toward the left wing and Z_b is positive up. \vec{r}_1 is the vector distance from the intersection of the longitudinal, lateral, and vertical axes of the forebody ("O") to the tether confluence point of the forebody. \vec{r}_2 is the vector distance from the c.g. of the decelerator ("O_p") to the tether confluence point of the decelerator; \vec{r}_2 lies along X_{pb} .

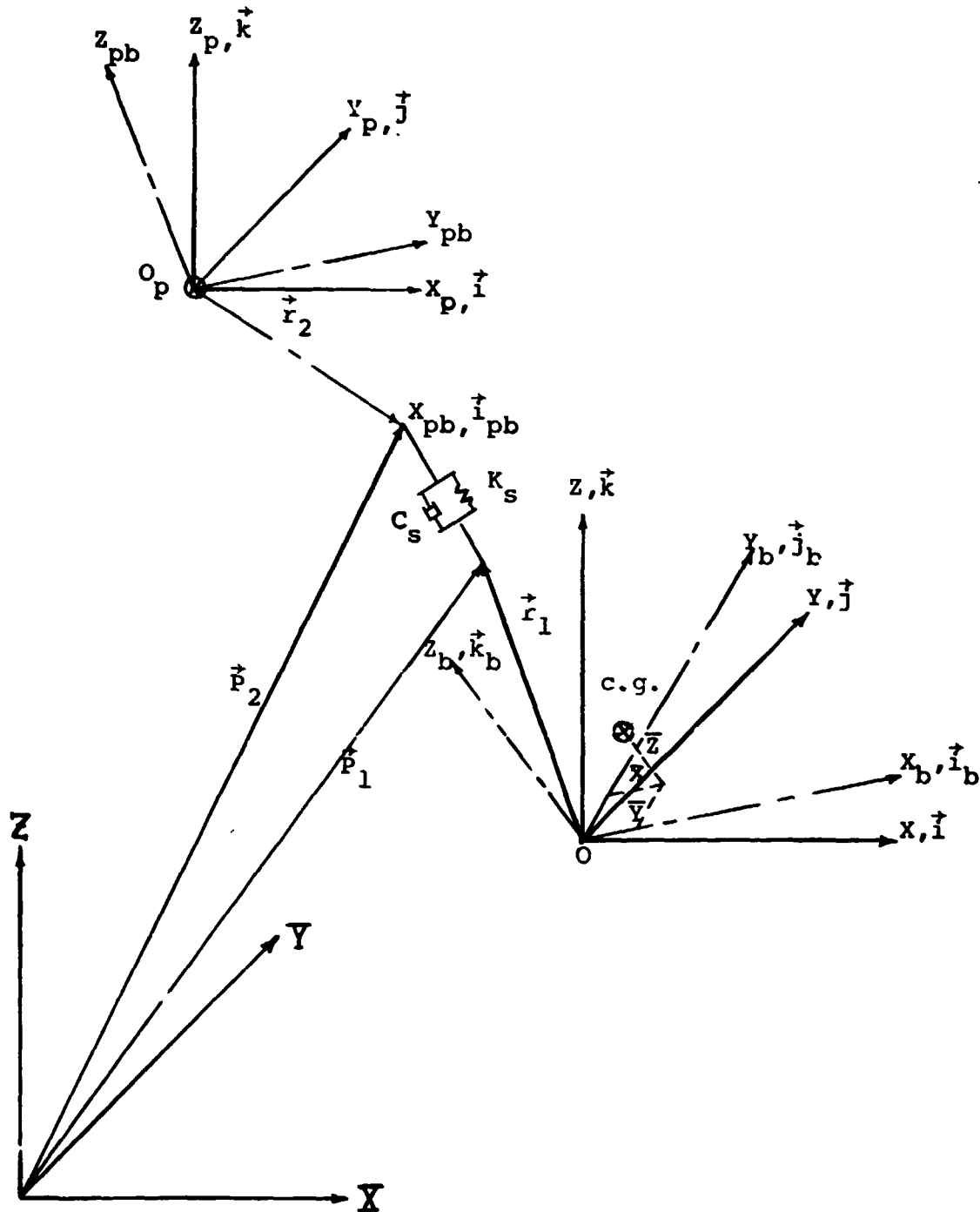


FIGURE 1 - COORDINATE SYSTEMS

SECTION 2 - EULER ANGLE TRANSFORMATION

In order to specify the angular orientation of a body with reference to a non-rotating coordinate system (X, Y, Z), three successive rotations are made as shown in Figure 2. The first rotation is in the direction, -OZ, such that OX and OY are rotated through an angle ψ into Oa and ON respectively. The second rotation is in the direction, -ON, such that Oa and OZ are rotated through an angle θ into OX_b and Ob respectively. The final rotation is about OX_b such that ON and Ob are rotated through an angle ϕ into OY_b and OZ_b respectively. The three angular rotations (ψ , θ , ϕ) specify the orientation of the body axes (X_b, Y_b, Z_b) with respect to the inertial axes (X, Y, Z). Again, from a pilots viewpoint, a positive ψ is a nose to the right yaw; a positive θ is a nose up pitch; and a positive ϕ is a right wing down roll.

The transformation matrix between the body axes and inertial axes is now found by considering one rotation at a time and then combining. The first rotation is given by:

$$\begin{Bmatrix} Oa \\ ON \\ OZ \end{Bmatrix} = \begin{bmatrix} C\psi & -S\psi & 0 \\ S\psi & C\psi & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{Bmatrix} OX \\ OY \\ OZ \end{Bmatrix} \quad (1)$$

where $S\psi = \sin\psi$ and $C\psi = \cos\psi$.

The second rotation is:

$$\begin{Bmatrix} OX_b \\ ON \\ Ob \end{Bmatrix} = \begin{bmatrix} C\theta & 0 & S\theta \\ 0 & 1 & 0 \\ -S\theta & 0 & C\theta \end{bmatrix} \begin{Bmatrix} Oa \\ ON \\ OZ \end{Bmatrix} \quad (2)$$

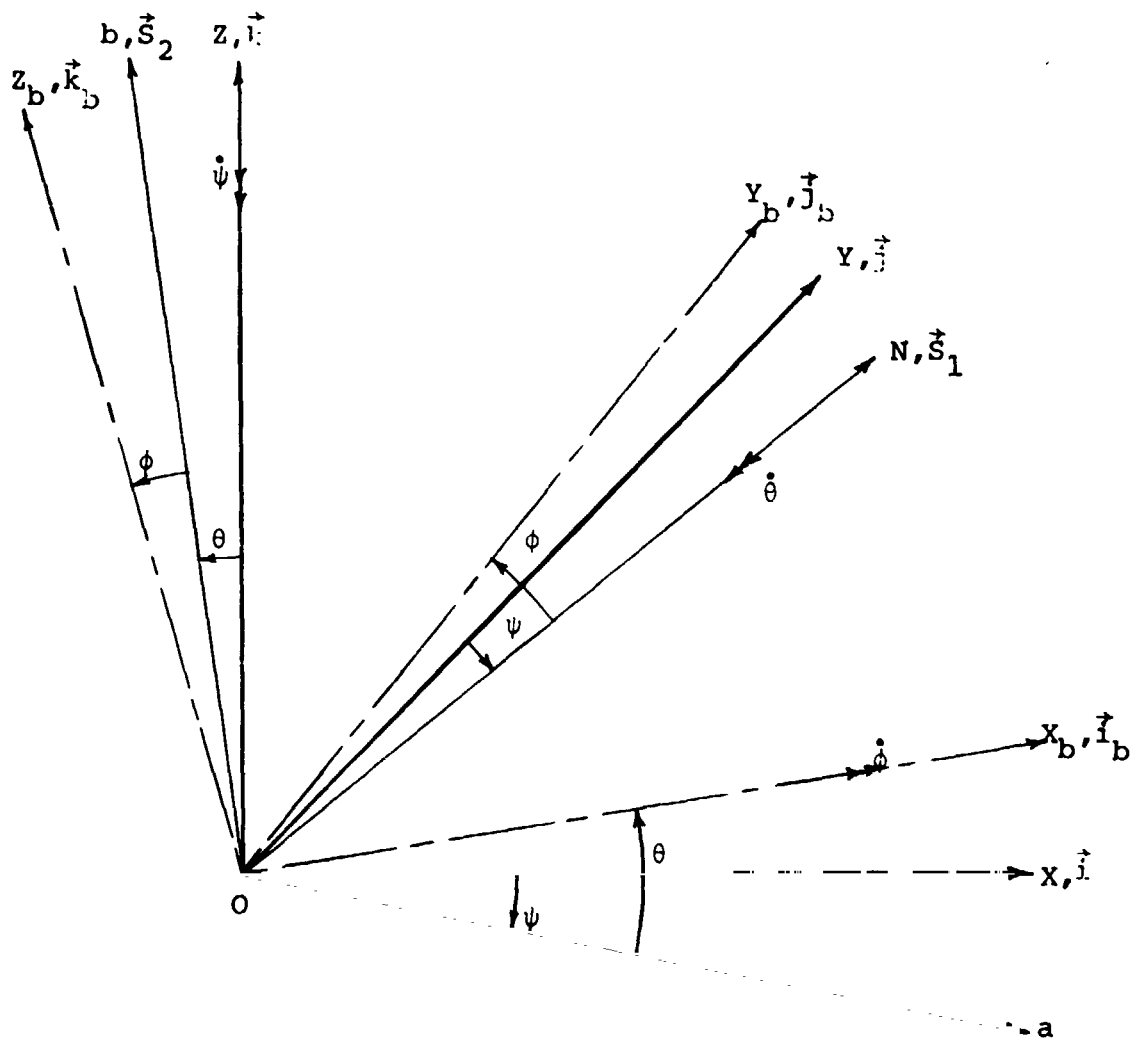


FIGURE 2 - EULER ANGLE ROTATIONS

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The final rotation is:

$$\begin{Bmatrix} OX_b \\ OY_b \\ OZ_b \end{Bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & C\phi & S\phi \\ 0 & -S\phi & C\phi \end{bmatrix} \begin{Bmatrix} OX_b \\ ON \\ Ob \end{Bmatrix} \quad (3)$$

By substituting Equation (1) into (2) and (2) into (3), the transformation matrix [C] is formed

$$\begin{Bmatrix} OX_b \\ OY_b \\ OZ_b \end{Bmatrix} = \begin{bmatrix} C\psi C\theta & -S\psi C\theta & S\theta \\ -C\psi S\theta S\phi + S\psi C\phi & S\psi S\theta S\phi + C\psi C\phi & C\theta S\phi \\ -C\psi S\theta C\phi - S\psi S\phi & S\psi S\theta C\phi - C\psi S\phi & C\theta C\phi \end{bmatrix} \begin{Bmatrix} OX \\ OY \\ OZ \end{Bmatrix} \quad (4)$$

Since [C] is a linear orthogonal ($\sum_{i=1}^3 C_{ij} C_{ik} = \delta_{jk}$; $j, k = 1, 2, 3$) transformation, its inverse is equal to its transpose.⁽¹⁾ Therefore,

$$\begin{Bmatrix} OX \\ OY \\ OZ \end{Bmatrix} = \begin{bmatrix} C\psi C\theta & -C\psi S\theta S\phi + S\psi C\phi & -C\psi S\theta C\phi - S\psi S\phi \\ -S\psi C\theta & S\psi S\theta S\phi + C\psi C\phi & S\psi S\theta C\phi - C\psi S\phi \\ S\theta & C\theta S\phi & C\theta C\phi \end{bmatrix} \begin{Bmatrix} OX_b \\ OY_b \\ OZ_b \end{Bmatrix} \quad (5)$$

For the decelerator, there is no rotation about the longitudinal axis. Consequently, the transformation matrix in (4) is simplified by letting $\phi = 0$. The result is $[C_p]$.

$$\begin{Bmatrix} OX_{pb} \\ OY_{pb} \\ OZ_{pb} \end{Bmatrix} = \begin{bmatrix} C\psi_p C\theta_p & -S\psi_p C\theta_p & S\theta_p \\ S\psi_p & C\psi_p & 0 \\ -C\psi_p S\theta_p & S\psi_p S\theta_p & C\theta_p \end{bmatrix} \begin{Bmatrix} OX_p \\ OY_p \\ OZ_p \end{Bmatrix} \quad (6)$$

The total angular velocity of the forebody is given by:

$$\vec{\omega} = \dot{\psi} \vec{k} - \dot{\theta} \vec{S}_1 + \dot{\phi} \vec{i}_b \quad (7)$$

From the inverse of (3):

$$\vec{S}_1 = c\phi \vec{j}_b - s\phi \vec{k}_b \quad (8)$$

$$\vec{S}_2 = s\phi \vec{j}_b + c\phi \vec{k}_b \quad (9)$$

From the inverse of (2):

$$\vec{k} = s\theta \vec{i}_b + c\theta \vec{S}_2 \quad (10)$$

Substituting (8), (9), and (10) into (7):

$$\vec{\omega} = [-\dot{\psi}(s\theta) + \dot{\phi}] \vec{i}_b + [-\dot{\psi}(c\theta s\phi) - \dot{\theta}(c\phi)] \vec{j}_b + [-\dot{\psi}(c\theta c\phi) + \dot{\theta}(s\phi)] \vec{k}_b \quad (11)$$

The components of angular velocity for the forebody are:

$$\omega_{xb} = -\dot{\psi}(s\theta) + \dot{\phi} \quad (12)$$

$$\omega_{yb} = -\dot{\psi}(c\theta s\phi) - \dot{\theta}(c\phi) \quad (13)$$

$$\omega_{zb} = -\dot{\psi}(c\theta c\phi) + \dot{\theta}(s\phi) \quad (14)$$

Likewise, for the decelerator, the angular velocities are:

$$\omega_{xpb} = -\dot{\psi}_p(s\theta_p) \quad (15)$$

$$\omega_{ypb} = -\dot{\theta}_p \quad (16)$$

$$\omega_{zpb} = -\dot{\psi}_p(c\theta_p) \quad (17)$$

SECTION 3 - KINETIC ENERGY

The kinetic energy of the system is due to the translational and rotational velocities of the forebody and the decelerator. The forebody is completely general in shape, and products of inertia and c.g. offsets will effect the kinetic energy. On the other hand, the decelerator is assumed to be symmetric about the longitudinal axis and the aerodynamic loads are referenced to the c.g. Therefore, all products of inertia and c.g. offsets are zero. The expression for kinetic energy is: ⁽²⁾

$$\begin{aligned}
 T = & \frac{1}{2} m [\dot{X}^2 + \dot{Y}^2 + \dot{Z}^2] + \frac{1}{2} [I_{xb} \omega_{xb}^2 + I_{yb} \omega_{yb}^2 + I_{zb} \omega_{zb}^2] \\
 & - [I_{yzb} \omega_{yb} \omega_{zb} + I_{xzb} \omega_{xb} \omega_{zb} + I_{xyb} \omega_{xb} \omega_{yb}] \\
 & + m [\dot{X}_b (\omega_{yb} \bar{Z} - \omega_{zb} \bar{Y}) + \dot{Y}_b (\omega_{zb} \bar{X} - \omega_{xb} \bar{Z}) + \dot{Z}_b (\omega_{xb} \bar{Y} - \omega_{yb} \bar{X})] \\
 & + \frac{1}{2} m_{pl} [\dot{X}_{pb}^2] + \frac{1}{2} m_{ps} [\dot{Y}_{pb}^2 + \dot{Z}_{pb}^2] \\
 & + \frac{1}{2} [I_{xpb} \omega_{xpb}^2 + I_{ypb} \omega_{ypb}^2 + I_{zpb} \omega_{zpb}^2]
 \end{aligned} \tag{18}$$

In Equation (18), m_{pl} and m_{ps} include directional mass terms due to the air enclosed in the canopy, I_{xpb} , I_{ypb} , and I_{zpb} are apparent mass moments of inertia.

SECTION 4 - POTENTIAL ENERGY

The potential energy of the system is due to the gravitational potential of both bodies and the elastic potential of the tether.

$$V = mg[Z + \bar{X}(S\theta) + \bar{Y}(C\theta S\phi) + \bar{Z}(C\theta C\phi)] + m_p g z_p + \frac{1}{2} K_s [L_T - L_{T0}]^2 \quad (19)$$

L_{T0} is the unstretched length of the tether; and L_T is the stretched length of the tether as given by the geometry of the system. Referring to Figure 1:

$$L_T = |\vec{P}_2 - \vec{P}_1| \quad (20)$$

\vec{P}_1 and \vec{P}_2 are the vectors from the inertial coordinate system ($\bar{X} \bar{Y} \bar{Z}$) to the confluence points of the forebody and decelerator respectively. For the forebody,

$$\vec{P}_1 = x\vec{i} + y\vec{j} + z\vec{k} + \vec{r}_1 \quad (21)$$

$$\vec{r}_1 = a\vec{i}_b + b\vec{j}_b + c\vec{k}_b \quad (22)$$

a , b , and c are measured along positive body axes X_b , Y_b , and Z_b respectively. Using the coordinate transformation matrix (4):

$$\begin{aligned} \vec{P}_1 = & [X + a(C\psi C\theta) + b(-C\psi S\theta S\phi + S\psi C\phi) + c(-C\psi S\theta C\phi - S\psi S\phi)] \vec{i} \\ & + [Y + a(-S\psi C\theta) + b(S\psi S\theta S\phi + C\psi C\phi) + c(S\psi S\theta C\phi - C\psi S\phi)] \vec{j} \\ & + [Z + a(S\theta) + b(C\theta S\phi) + c(C\theta C\phi)] \vec{k} \end{aligned} \quad (23)$$

Similarly for the decelerator:

$$\vec{p}_2 = x_p \vec{i} + y_p \vec{j} + z_p \vec{k} + \vec{r}_2 \quad (24)$$

$$\vec{r}_2 = a_p \vec{i}_{pb} \quad (25)$$

Substituting (25) into (24) and using matrix Equation (6),

$$\vec{p}_2 = [x_p + a_p (C\psi_p C\theta_p)] \vec{i} + [y_p + a_p (-S\psi_p C\theta_p)] \vec{j} + [z_p + a_p (S\theta_p)] \vec{k} \quad (26)$$

$$L_T = [L_T \cdot L_T]^{1/2} \quad (27)$$

$$\begin{aligned} L_T = & \{ [x_p + a_p (C\psi_p C\theta_p) - X - a (C\psi C\theta) - b (-C\psi S\theta S\phi + S\psi C\phi) - c (-C\psi S\theta C\phi - S\psi S\phi)]^2 \\ & + [y_p + a_p (-S\psi_p C\theta_p) - Y - a (-S\psi C\theta) - b (S\psi S\theta S\phi + C\psi C\phi) - c (S\psi S\theta C\phi - C\psi S\phi)]^2 \\ & + [z_p + a_p (S\theta_p) - Z - a (S\theta) - b (C\theta S\phi) - c (C\theta C\phi)]^2 \}^{1/2} \end{aligned} \quad (28)$$

Define the variables \bar{A} , \bar{B} , and \bar{C} such that:

$$L_T = \{ [\bar{A}]^2 + [\bar{B}]^2 + [\bar{C}]^2 \}^{1/2} \quad (29)$$

Further on in the derivation it will be necessary to know the total time derivative of L_T and the partial derivatives of \bar{A} , \bar{B} , and \bar{C} with respect to the generalized coordinates.

$$\dot{L}_T = [\bar{A} \dot{\bar{A}} + \bar{B} \dot{\bar{B}} + \bar{C} \dot{\bar{C}}] / L_T \quad (30)$$

$$\begin{aligned}\dot{\bar{A}} = & \dot{x}_p + a_p [\dot{\psi}_p (-s\psi_p c\theta_p) + \dot{\theta}_p (-c\psi_p s\theta_p)] - \dot{x} - a [\dot{\psi} (-s\psi c\theta) + \dot{\theta} (-c\psi s\theta)] \\ & - b [\dot{\psi} (s\psi s\theta s\phi + c\psi c\phi) + \dot{\theta} (-c\psi c\theta s\phi) + \dot{\phi} (-c\psi s\theta c\phi - s\psi s\phi)] \\ & - c [\dot{\psi} (s\psi s\theta c\phi - c\psi s\phi) + \dot{\theta} (-c\psi c\theta c\phi) + \dot{\phi} (c\psi s\theta s\phi - s\psi c\phi)]\end{aligned}\quad (31)$$

$$\begin{aligned}\dot{\bar{B}} = & \dot{y}_p + a_p [\dot{\psi}_p (-c\psi_p c\theta_p) + \dot{\theta}_p (s\psi_p s\theta_p)] - \dot{y} - a [\dot{\psi} (-c\psi c\theta) + \dot{\theta} (s\psi s\theta)] \\ & - b [\dot{\psi} (c\psi s\theta s\phi - s\psi c\phi) + \dot{\theta} (s\psi c\theta s\phi) + \dot{\phi} (s\psi s\theta c\phi - c\psi s\phi)] \\ & - c [\dot{\psi} (c\psi s\theta c\phi + s\psi s\phi) + \dot{\theta} (s\psi c\theta c\phi) + \dot{\phi} (-s\psi s\theta s\phi - c\psi c\phi)]\end{aligned}\quad (32)$$

$$\begin{aligned}\dot{\bar{C}} = & \dot{z}_p + a_p [\dot{\theta}_p (c\theta_p)] - \dot{z} - a [\dot{\theta} (c\theta)] - b [\dot{\theta} (-s\theta s\phi) + \dot{\phi} (c\theta c\phi)] \\ & - c [\dot{\theta} (-s\theta c\phi) + \dot{\phi} (-c\theta s\phi)]\end{aligned}\quad (33)$$

$$\frac{\partial \bar{A}}{\partial X} = \frac{\partial \bar{B}}{\partial Y} = \frac{\partial \bar{C}}{\partial Z} = -1 \quad (34)$$

$$\frac{\partial \bar{A}}{\partial X_p} = \frac{\partial \bar{B}}{\partial Y_p} = \frac{\partial \bar{C}}{\partial Z_p} = 1 \quad (35)$$

$$\begin{aligned}\frac{\partial \bar{A}}{\partial Y} = \frac{\partial \bar{A}}{\partial Z} = \frac{\partial \bar{A}}{\partial Y_p} = \frac{\partial \bar{A}}{\partial Z_p} = 0 \\ \frac{\partial \bar{B}}{\partial X} = \frac{\partial \bar{B}}{\partial Z} = \frac{\partial \bar{B}}{\partial X_p} = \frac{\partial \bar{B}}{\partial Z_p} = 0 \\ \frac{\partial \bar{C}}{\partial X} = \frac{\partial \bar{C}}{\partial Y} = \frac{\partial \bar{C}}{\partial X_p} = \frac{\partial \bar{C}}{\partial Y_p} = 0\end{aligned}\quad (36)$$

$$\frac{\partial \bar{A}}{\partial \psi} = a (S \psi C \theta) - b (S \psi S \theta S \phi + C \psi C \phi) - c (S \psi S \theta C \phi - C \psi S \phi) \quad (37)$$

$$\frac{\partial \bar{A}}{\partial \theta} = a (C \psi S \theta) + b (C \psi C \theta S \phi) + c (C \psi C \theta C \phi) \quad (38)$$

$$\frac{\partial \bar{A}}{\partial \phi} = b (C \psi S \theta C \phi + S \psi S \phi) - c (C \psi S \theta S \phi - S \psi C \phi) \quad (39)$$

$$\frac{\partial \bar{A}}{\partial \psi_p} = a_p (-S \psi_p C \theta_p) \quad (40)$$

$$\frac{\partial \bar{A}}{\partial \theta_p} = a_p (-C \psi_p S \theta_p) \quad (41)$$

$$\frac{\partial \bar{B}}{\partial \psi} = a (C \psi C \theta) - b (C \psi S \theta S \phi - S \psi C \phi) - c (C \psi S \theta C \phi + S \psi S \phi) \quad (42)$$

$$\frac{\partial \bar{B}}{\partial \theta} = a (-S \psi S \theta) - b (S \psi C \theta S \phi) - c (S \psi C \theta C \phi) \quad (43)$$

$$\frac{\partial \bar{B}}{\partial \phi} = -b (S \psi S \theta C \phi - C \psi S \phi) + c (S \psi S \theta S \phi + C \psi C \phi) \quad (44)$$

$$\frac{\partial \bar{B}}{\partial \psi_p} = a_p (-C \psi_p C \theta_p) \quad (45)$$

$$\frac{\partial \bar{B}}{\partial \theta_p} = a_p (S \psi_p S \theta_p) \quad (46)$$

$$\frac{\partial \bar{C}}{\partial \psi} = 0 \quad (47)$$

$$\frac{\partial \bar{C}}{\partial \theta} = a (-C \theta) + b (S \theta S \phi) + c (S \theta C \phi) \quad (48)$$

$$\frac{\partial \bar{C}}{\partial \phi} = b(-C\theta C\phi) + c(C\theta S\phi) \quad (49)$$

$$\frac{\partial \bar{C}}{\partial \psi_p} = 0 \quad (50)$$

$$\frac{\partial \bar{C}}{\partial \theta_p} = a_p(C\theta_p) \quad (51)$$

SECTION 5 - RALEIGH'S DISSIPATION FUNCTION

If the viscous damping force is proportional to the velocity of the particle at which the force acts, an expression analogous to the potential energy of a spring may be used. This function, F , is known as Rayleigh's dissipation function, and is defined as ⁽¹⁾

$$F = \frac{1}{2} \sum_{i=1}^n C_i \dot{q}_i^2 \quad (52)$$

For this problem, Rayleigh's damping is considered only in the tether.

$$F = \frac{1}{2} C_s \dot{L}_T^2$$

SECTION 6 - LAGRANGE'S EQUATION

The Lagrange equation for a non-conservative (aerodynamic forces) system with a holonomic (can be expressed as an algebraic expression), scleronomous (independent of time) constraint and Rayleigh's dissipation function (damping in the elastic tether) can be written as: ⁽¹⁾

$$\frac{d}{dt} \left(\frac{\partial L}{\partial \dot{q}_i} \right) - \frac{\partial L}{\partial q_i} - \lambda \frac{\partial \bar{g}}{\partial q_i} + \frac{\partial F}{\partial \dot{q}_i} = Q_i \quad (54)$$

In Equation (54), the term $\lambda \frac{\partial \bar{g}}{\partial q_i}$ expresses the generalized force exerted by the tether on the i^{th} degree of freedom. The constraint equation is:

$$\bar{g} = \{ [\bar{A}]^2 + [\bar{B}]^2 + [\bar{C}]^2 \}^{1/2} - L_T = 0 \quad (55)$$

Q_i is the generalized force due to the aerodynamics.

$\frac{\partial F}{\partial \dot{q}_i}$ is the force due to damping in the tether.

The Lagrangian is equal to the total kinetic energy of the system (Equation (18)) minus the total potential energy of the system (Equation (19)). With substitutions from Equations (4), (6) and (12) to (17), the Lagrangian is:

$$\begin{aligned} L = & \frac{1}{2} m [\dot{X}^2 + \dot{Y}^2 + \dot{Z}^2] + \frac{1}{2} m_{pl} [\dot{X}_p (C\psi_p C\theta_p) + \dot{Y}_p (-S\psi_p C\theta_p) + \dot{Z}_p (S\theta_p)]^2 \\ & + \frac{1}{2} m_{ps} \{ [\dot{X}_p (S\psi_p) + \dot{Y}_p (C\psi_p)]^2 + [\dot{X}_p (-C\psi_p S\theta_p) + \dot{Y}_p (S\psi_p S\theta_p) + \dot{Z}_p (C\theta_p)]^2 \} \\ & + \frac{1}{2} I_{xb} [-\dot{\psi}(S\theta) + \dot{\phi}]^2 + \frac{1}{2} I_{yb} [-\dot{\psi}(C\theta S\phi) - \dot{\theta}(C\phi)]^2 + \frac{1}{2} I_{zb} [-\dot{\psi}(C\theta C\phi) + \dot{\theta}(S\phi)]^2 \\ & - [I_{yzb} [-\dot{\psi}(C\theta S\phi) - \dot{\theta}(C\phi)] [-\dot{\psi}(C\theta C\phi) + \dot{\theta}(S\phi)] + I_{xzb} [-\dot{\psi}(S\theta) + \dot{\phi}] [-\dot{\psi}(C\theta C\phi) + \dot{\theta}(S\phi)]] \\ & + I_{xyb} [-\dot{\psi}(S\theta) + \dot{\phi}] [-\dot{\psi}(C\theta S\phi) - \dot{\theta}(C\phi)] \} \end{aligned}$$

$$\begin{aligned}
 & + \frac{1}{2} I_{xpb} [-\dot{\psi}_p^2 (S^2 \theta_p) + \frac{1}{2} I_{ypb} [\dot{\theta}_p^2 + \dot{\psi}_p^2 (C^2 \theta_p)] \\
 & + m \{ [\dot{X}(C\psi C\theta) + \dot{Y}(-S\psi C\theta) + \dot{Z}(S\theta)] [\bar{Z}(-\dot{\psi}(C\theta S\phi) - \dot{\theta}(C\phi)) - \bar{Y}(-\dot{\psi}(C\theta C\phi) + \dot{\theta}(S\phi))] \\
 & + [\dot{X}(-C\psi S\theta S\phi + S\psi C\phi) + \dot{Y}(S\psi S\theta S\phi + C\psi C\phi) + \dot{Z}(C\theta S\phi)] [\bar{X}(-\dot{\psi}(C\theta C\phi) + \dot{\theta}(S\phi)) - \bar{Z}(-\dot{\psi}(S\theta) + \dot{\phi})] \\
 & + [\dot{X}(-C\psi S\theta C\phi - S\psi S\phi) + \dot{Y}(S\psi S\theta C\phi - C\psi S\phi) + \dot{Z}(C\theta C\phi)] [\bar{Y}(-\dot{\psi}(S\theta) + \dot{\phi}) - \bar{X}(-\dot{\psi}(C\theta S\phi) - \dot{\theta}(C\phi))] \} \\
 & - mg [Z + \bar{X}(S\theta) + \bar{Y}(C\theta S\phi) + \bar{Z}(C\theta C\phi)] - m_p g Z_p - \frac{1}{2} K_s [L_T - L_{TO}]^2 \quad (56)
 \end{aligned}$$

Note: $I_{ypb} = I_{zpb}$ due to decelerator symmetry.

SECTION 7 - GENERAL EQUATIONS OF MOTION

Equation (56) displays all of the generalized coordinates explicitly except those appearing in L_T . The terms to be substituted into Equation (54) are now developed.

X Equation

$$\begin{aligned}
 \frac{d}{dt} \left(\frac{\partial L}{\partial \dot{X}} \right) &= \ddot{X}\{m\} + \ddot{\psi}\{m[\bar{X}(-S\psi C\theta) + \bar{Y}(S\psi S\theta S\phi + C\psi C\phi) + \bar{Z}(S\psi S\theta C\phi - C\psi S\phi)]\} \\
 &+ \ddot{\theta}\{m[\bar{X}(-C\psi S\theta) + \bar{Y}(-C\psi C\theta S\phi) + \bar{Z}(-C\psi C\theta C\phi)]\} \\
 &+ \ddot{\phi}\{m[\bar{Y}(-C\psi S\theta C\phi - S\psi S\phi) + \bar{Z}(C\psi S\theta S\phi - S\psi S\phi)]\} \\
 &+ \dot{\psi}\dot{\theta}\{m[\bar{X}(2S\psi S\theta) + \bar{Y}(2S\psi C\theta S\phi) + \bar{Z}(2S\psi C\theta C\phi)]\}
 \end{aligned}$$

$$\begin{aligned}
 & +\ddot{\psi}\dot{\phi}\{m[\bar{Y}(2S\psi S\theta C\phi-2C\psi S\phi)+\bar{Z}(-2S\psi S\theta S\phi-2C\psi C\phi)]\} \\
 & +\dot{\theta}\dot{\phi}\{m[\bar{Y}(-2C\psi C\theta C\phi)+\bar{Z}(2C\psi C\theta S\phi)]\} \\
 & +\dot{\psi}^2\{m[\bar{X}(-C\psi C\theta)+\bar{Y}(C\psi S\theta S\phi-S\psi C\phi)+\bar{Z}(C\psi S\theta C\phi+S\psi S\phi)]\} \\
 & +\dot{\theta}^2\{m[\bar{X}(-C\psi C\theta)+\bar{Y}(C\psi S\theta S\phi)+\bar{Z}(C\psi S\theta C\phi)]\} \\
 & +\dot{\phi}^2\{m[\bar{Y}(C\psi S\theta S\phi-S\psi C\phi)+\bar{Z}(C\psi S\theta C\phi+S\psi S\phi)]\}
 \end{aligned} \tag{57}$$

$$\frac{\partial L}{\partial X} = 0 \tag{58}$$

$$\frac{\partial \bar{g}}{\partial X} = \frac{-\bar{A}}{L_T} \tag{59}$$

$$\frac{\partial F}{\partial X} = 0 \tag{60}$$

Y Equation

$$\begin{aligned}
 \frac{d}{dt}\left(\frac{\partial L}{\partial \dot{Y}}\right) &= \ddot{Y}\{m\}+\ddot{\psi}\{m[\bar{X}(-C\psi C\theta)+\bar{Y}(C\psi S\theta S\phi-S\psi C\phi)+\bar{Z}(C\psi S\theta C\phi+S\psi S\phi)]\} \\
 & +\ddot{\theta}\{m[\bar{X}(S\psi S\theta)+\bar{Y}(S\psi C\theta S\phi)+\bar{Z}(S\psi C\theta C\phi)]\} \\
 & +\ddot{\phi}\{m[\bar{Y}(S\psi S\theta C\phi-C\psi S\phi)+\bar{Z}(-S\psi S\theta S\phi-C\psi C\phi)]\} \\
 & +\dot{\psi}\dot{\theta}\{m[\bar{X}(2C\psi S\theta)+\bar{Y}(2C\psi C\theta S\phi)+\bar{Z}(2C\psi C\theta C\phi)]\}
 \end{aligned}$$

$$\begin{aligned}
 & +\ddot{\psi}\dot{\phi}\{m[\bar{Y}(2C\psi S\theta C\phi+2S\psi S\phi)+\bar{Z}(-2C\psi S\theta S\phi+2S\psi C\phi)]\} \\
 & +\dot{\theta}\ddot{\phi}\{m[\bar{Y}(2S\psi C\theta C\phi)+\bar{Z}(-2S\psi C\theta S\phi)]\} \\
 & +\dot{\psi}^2\{m[\bar{X}(S\psi C\theta)+\bar{Y}(-S\psi S\theta S\phi-C\psi C\phi)+\bar{Z}(-S\psi S\theta C\phi+C\psi S\phi)]\} \\
 & +\dot{\theta}^2\{m[\bar{X}(S\psi C\theta)+\bar{Y}(-S\psi S\theta S\phi)+\bar{Z}(-S\psi S\theta C\phi)]\} \\
 & +\dot{\phi}^2\{m[\bar{Y}(-S\psi S\theta S\phi-C\psi C\phi)+\bar{Z}(-S\psi S\theta C\phi+C\psi S\phi)]\}
 \end{aligned} \tag{61}$$

$$\frac{\partial L}{\partial \dot{Y}} = 0 \tag{62}$$

$$\frac{\partial \bar{q}}{\partial \dot{Y}} = -\frac{\bar{B}}{L_T} \tag{63}$$

$$\frac{\partial F}{\partial \dot{Y}} = 0 \tag{64}$$

Z Equation

$$\begin{aligned}
 \frac{d}{dt}\left(\frac{\partial L}{\partial \dot{Z}}\right) &= \ddot{Z}\{m\}+\ddot{\theta}\{m[\bar{X}(C\theta)+\bar{Y}(-S\theta S\phi)+\bar{Z}(-S\theta C\phi)]\} \\
 & +\ddot{\phi}\{m[\bar{Y}(C\theta C\phi)+\bar{Z}(-C\theta S\phi)]\} \\
 & +\dot{\theta}\ddot{\phi}\{m[\bar{Y}(-2S\theta C\phi)+\bar{Z}(S\theta S\phi)]\} \\
 & +\dot{\theta}^2\{m[\bar{X}(-S\theta)+\bar{Y}(-C\theta S\phi)+\bar{Z}(-C\theta C\phi)]\} \\
 & +\dot{\phi}^2\{m[\bar{Y}(-C\theta S\phi)+\bar{Z}(-C\theta C\phi)]\}
 \end{aligned} \tag{65}$$

$$\frac{\partial L}{\partial \dot{Z}} = -mg \quad (66)$$

$$\frac{\partial \bar{q}}{\partial \dot{Z}} = -\frac{\bar{C}}{L_T} \quad (67)$$

$$\frac{\partial F}{\partial \dot{Z}} = 0 \quad (68)$$

X_p Equation

$$\begin{aligned} \frac{d}{dt} \left(\frac{\partial L}{\partial \dot{X}_p} \right) = & \dot{X}_p \{ m_{pl} [C^2 \psi_p C^2 \theta_p] + m_{ps} [S^2 \psi_p + C^2 \psi_p S^2 \theta_p] \} \\ & + \ddot{Y}_p \{ [m_{pl} - m_{ps}] [-\frac{1}{2} S 2 \psi_p C^2 \theta_p] \} \\ & + \ddot{Z}_p \{ [m_{pl} - m_{ps}] [\frac{1}{2} C \psi_p S 2 \theta_p] \} \\ & + \dot{X}_p \dot{\psi}_p \{ [m_{pl} - m_{ps}] [-S 2 \psi_p C^2 \theta_p] \} \\ & + \dot{X}_p \dot{\theta}_p \{ [m_{pl} - m_{ps}] [-C^2 \psi_p S 2 \theta_p] \} \\ & + \dot{Y}_p \dot{\psi}_p \{ [m_{pl} - m_{ps}] [-C 2 \psi_p C^2 \theta_p] \} \\ & + \dot{Y}_p \dot{\theta}_p \{ [m_{pl} - m_{ps}] [\frac{1}{2} S 2 \psi_p S 2 \theta_p] \} \\ & + \dot{Z}_p \dot{\psi}_p \{ [m_{pl} - m_{ps}] [-\frac{1}{2} S \psi_p S 2 \theta_p] \} \\ & + \dot{Z}_p \dot{\theta}_p \{ [m_{pl} - m_{ps}] [C \psi_p C 2 \theta_p] \} \end{aligned} \quad (69)$$

$$\frac{\partial L}{\partial \dot{X}_p} = 0 \quad (70)$$

$$\frac{\partial \bar{q}}{\partial \dot{X}_p} = \frac{\bar{A}}{L_T} \quad (71)$$

$$\frac{\partial F}{\partial \dot{X}_p} = 0 \quad (72)$$

Y_p Equation

$$\begin{aligned} \frac{d}{dt} \left(\frac{\partial L}{\partial \dot{Y}_p} \right) = & \ddot{X}_p \{ [m_{p\ell} - m_{ps}] [-\frac{1}{2} S 2\psi_p C^2 \theta_p] \} \\ & + \ddot{Y}_p \{ m_{p\ell} [S^2 \psi_p C^2 \theta_p] + m_{ps} [C^2 \psi_p + S^2 \psi_p S^2 \theta_p] \} \\ & + \ddot{Z}_p \{ m_{p\ell} - m_{ps} \} [-\frac{1}{2} S \psi_p S 2\theta_p] \} \\ & + \dot{X}_p \dot{\psi}_p \{ [m_{p\ell} - m_{ps}] [-C 2\psi_p C^2 \theta_p] \} \\ & + \dot{X}_p \dot{\theta}_p \{ [m_{p\ell} - m_{ps}] [\frac{1}{2} S 2\psi_p S 2\theta_p] \} \\ & + \dot{Y}_p \dot{\psi}_p \{ [m_{p\ell} - m_{ps}] [S 2\psi_p C^2 \theta_p] \} \\ & + \dot{Y}_p \dot{\theta}_p \{ [m_{p\ell} - m_{ps}] [-S^2 \psi_p S 2\theta_p] \} \\ & + \dot{Z}_p \dot{\psi}_p \{ [m_{p\ell} - m_{ps}] [-\frac{1}{2} C \psi_p S 2\theta_p] \} \\ & + \dot{Z}_p \dot{\theta}_p \{ [m_{p\ell} - m_{ps}] [-S \psi_p C 2\theta_p] \} \end{aligned} \quad (73)$$

$$\frac{\partial L}{\partial \dot{Y}_p} = 0 \quad (74)$$

$$\frac{\partial \bar{q}}{\partial \dot{Y}_p} = \frac{\bar{B}}{L_T} \quad (75)$$

$$\frac{\partial F}{\partial \dot{Y}_p} = 0 \quad (76)$$

Z_p Equation

$$\begin{aligned} \frac{d}{dt} \left(\frac{\partial L}{\partial \dot{Z}_p} \right) = & \ddot{X}_p \{ [m_{p\ell} - m_{ps}] \left[\frac{1}{2} C\psi_p S2\theta_p \right] \} \\ & + \ddot{Y}_p \{ [m_{p\ell} - m_{ps}] \left[-\frac{1}{2} S\psi_p S2\theta_p \right] \} \\ & + \ddot{Z}_p \{ m_{p\ell} [S^2\theta_p] + m_{ps} [C^2\theta_p] \} \\ & + \dot{X}_p \dot{\psi}_p \{ [m_{p\ell} - m_{ps}] \left[-\frac{1}{2} S\psi_p S2\theta_p \right] \} \\ & + \dot{X}_p \dot{\theta}_p \{ [m_{p\ell} - m_{ps}] [C\psi_p C2\theta_p] \} \\ & + \dot{Y}_p \dot{\psi}_p \{ [m_{p\ell} - m_{ps}] \left[-\frac{1}{2} C\psi_p S2\theta_p \right] \} \\ & + \dot{Y}_p \dot{\theta}_p \{ [m_{p\ell} - m_{ps}] [-S\psi_p C2\theta_p] \} \\ & + \dot{Z}_p \dot{\theta}_p \{ [m_{p\ell} - m_{ps}] [S2\theta_p] \} \end{aligned} \quad (77)$$

$$\frac{\partial L}{\partial \dot{z}_p} = -m_p g \quad (78)$$

$$\frac{\partial \bar{q}}{\partial \dot{z}_p} = \frac{\bar{C}}{\bar{L}_T} \quad (79)$$

$$\frac{\partial F}{\partial \dot{z}_p} = 0 \quad (80)$$

ψ Equation

$$\begin{aligned} \frac{d}{dt} \left(\frac{\partial L}{\partial \dot{\psi}} \right) = & \ddot{\psi} \{ I_{xb} (S^2 \theta) + [I_{yb} (S^2 \phi) + I_{zb} (C^2 \phi)] (C^2 \theta) + I_{yzb} (-C^2 \theta S 2 \phi) \\ & + [I_{xzb} (C \phi) + I_{xyb} (S \phi)] (-S 2 \theta) \} \\ & + \ddot{\theta} \{ [(I_{yb} - I_{zb}) \left(\frac{1}{2} S 2 \phi \right) - I_{yzb} (C 2 \phi)] (C \theta) + [I_{xzb} (S \phi) - I_{xyb} (C \phi)] (S \theta) \} \\ & + \ddot{\phi} \{ I_{xb} (-S \theta) + [I_{xzb} (C \phi) + I_{xyb} (S \phi)] (C \theta) \} \\ & + \ddot{X} \{ m [\bar{X} (-S \psi C \theta) + \bar{Y} (S \psi S \theta S \phi + C \psi C \phi) + \bar{Z} (S \psi S \theta C \phi - C \psi S \phi)] \} \\ & + \ddot{Y} \{ m [-\bar{X} (C \psi C \theta) - \bar{Y} (-C \psi S \theta S \phi + S \psi C \phi) - \bar{Z} (-C \psi S \theta C \phi - S \psi S \phi)] \} \\ & + \dot{\psi} \dot{\theta} \{ [I_{xb} - I_{yb} (S^2 \phi) - I_{zb} (C^2 \phi) + I_{yzb} (S 2 \phi)] (S 2 \theta) - [I_{xzb} (C \phi) + I_{xyb} (S \phi)] (2 C 2 \theta) \} \\ & + \dot{\psi} \dot{\phi} \{ [(I_{yb} - I_{zb}) (S 2 \phi) - I_{yzb} (2 C 2 \phi)] (C^2 \theta) + [I_{xzb} (S \phi) - I_{xyb} (C \phi)] (S 2 \theta) \} \\ & + \dot{\theta} \dot{\phi} \{ [-I_{xb} + (I_{yb} - I_{zb}) (C 2 \phi) + I_{yzb} (2 S 2 \phi)] (C \theta) \} \end{aligned}$$

$$\begin{aligned}
 & +\dot{\theta}^2 \{ [(I_{yb} - I_{zb}) (-\frac{1}{2} S 2\phi) + I_{yzb} (C 2\phi)] (S\theta) + I_{xzb} (C\theta S\phi) - I_{xyb} (C\theta C\phi) \} \\
 & +\dot{\phi}^2 \{ I_{xyb} (C\theta C\phi) - I_{xzb} (C\theta S\phi) \} \\
 & +\dot{X}\dot{\psi} \{ m [-\bar{X} (C\psi C\theta) - \bar{Y} (-C\psi S\theta S\phi + S\psi C\phi) - \bar{Z} (-C\psi S\theta C\phi - S\psi S\phi)] \} \\
 & +\dot{X}\dot{\theta} \{ m [\bar{X} (S\psi S\theta) + \bar{Y} (S\psi C\theta S\phi) + \bar{Z} (S\psi C\theta C\phi)] \} \\
 & +\dot{X}\dot{\phi} \{ m [\bar{Y} (S\psi S\theta C\phi - C\psi S\phi) - \bar{Z} (S\psi S\theta S\phi + C\psi C\phi)] \} \\
 & +\dot{Y}\dot{\psi} \{ m [-\bar{X} (-S\psi C\theta) - \bar{Y} (S\psi S\theta S\phi + C\psi C\phi) - \bar{Z} (S\psi S\theta C\phi - C\psi S\phi)] \} \\
 & +\dot{Y}\dot{\theta} \{ m [\bar{X} (C\psi S\theta) + \bar{Y} (C\psi C\theta S\phi) + \bar{Z} (C\psi C\theta C\phi)] \} \\
 & +\dot{Y}\dot{\phi} \{ m [-\bar{Y} (-C\psi S\theta C\phi - S\psi S\phi) + \bar{Z} (-C\psi S\theta S\phi + S\psi C\phi)] \} \quad (81)
 \end{aligned}$$

$$\begin{aligned}
 \frac{\partial L}{\partial \psi} = & \dot{X}\dot{\psi} \{ m [-\bar{X} (C\psi C\theta) - \bar{Y} (-C\psi S\theta S\phi + S\psi C\phi) - \bar{Z} (-C\psi S\theta C\phi - S\psi S\phi)] \} \\
 & +\dot{X}\dot{\theta} \{ m [\bar{X} (S\psi S\theta) + \bar{Y} (S\psi C\theta S\phi) + \bar{Z} (S\psi C\theta C\phi)] \} \\
 & +\dot{X}\dot{\phi} \{ m [\bar{Y} (S\psi S\theta C\phi - C\psi S\phi) - \bar{Z} (S\psi S\theta S\phi + C\psi C\phi)] \} \\
 & +\dot{Y}\dot{\psi} \{ m [-\bar{X} (-S\psi C\theta) - \bar{Y} (S\psi S\theta S\phi + C\psi C\phi) - \bar{Z} (S\psi S\theta C\phi - C\psi S\phi)] \} \\
 & +\dot{Y}\dot{\theta} \{ m [\bar{X} (C\psi S\theta) + \bar{Y} (C\psi C\theta S\phi) + \bar{Z} (C\psi C\theta C\phi)] \} \\
 & +\dot{Y}\dot{\phi} \{ m [-\bar{Y} (-C\psi S\theta C\phi - S\psi S\phi) + \bar{Z} (-C\psi S\theta S\phi + S\psi C\phi)] \} \quad (82)
 \end{aligned}$$

$$\frac{\partial \bar{g}}{\partial \psi} = \{ \bar{A} \frac{\partial \bar{A}}{\partial \psi} + \bar{B} \frac{\partial \bar{B}}{\partial \psi} \} / L_T \quad (83)$$

$$\frac{\partial F}{\partial \psi} = 0 \quad (84)$$

θ Equation

$$\begin{aligned} \frac{d}{dt} \left(\frac{\partial L}{\partial \dot{\theta}} \right) = & \ddot{\psi} \{ [(I_{yb} - I_{zb}) \left(\frac{1}{2} S 2\phi \right) - I_{yzb} (C 2\phi)] (C\theta) - [I_{xyb} (C\phi) - I_{xzb} (S\phi)] (S\theta) \} \\ & + \ddot{\theta} \{ I_{yb} (C^2\phi) + I_{zb} (S^2\phi) + I_{yzb} (S 2\phi) \} \\ & + \ddot{\phi} \{ I_{xyb} (C\phi) - I_{xzb} (S\phi) \} \\ & + \ddot{X} \{ m [\bar{X} (-C\psi S\theta) + \bar{Y} (-C\psi C\theta S\phi) + \bar{Z} (-C\psi C\theta C\phi)] \} \\ & + \ddot{Y} \{ m [\bar{X} (S\psi S\theta) + \bar{Y} (S\psi C\theta S\phi) + \bar{Z} (S\psi C\theta C\phi)] \} \\ & + \ddot{Z} \{ m [\bar{X} (C\theta) + \bar{Y} (-S\theta S\phi) + \bar{Z} (-S\theta C\phi)] \} \\ & + \dot{\psi} \dot{\theta} \{ [(I_{yb} - I_{zb}) \left(-\frac{1}{2} S 2\phi \right) + I_{yzb} (C 2\phi)] (S\theta) + [I_{xyb} (C\phi) - I_{xzb} (S\phi)] (-C\theta) \} \\ & + \dot{\psi} \dot{\phi} \{ [(I_{yb} - I_{zb}) (C 2\phi) + I_{yzb} (S 2\phi)] (C\theta) + [I_{xyb} (S\phi) + I_{xzb} (C\phi)] (S\theta) \} \\ & + \dot{\theta} \dot{\phi} \{ [I_{yb} - I_{zb}] (-S 2\phi) + I_{yzb} (S 2\phi) \} \\ & + \dot{\phi}^2 \{ -I_{xyb} (S\phi) - I_{xzb} (C\phi) \} \\ & + \dot{X} \dot{\psi} \{ m [\bar{X} (S\psi S\theta) + \bar{Y} (S\psi C\theta S\phi) + \bar{Z} (S\psi C\theta C\phi)] \} \\ & + \dot{X} \dot{\theta} \{ m [\bar{X} (-C\psi C\theta) + \bar{Y} (C\psi S\theta S\phi) + \bar{Z} (C\psi S\theta C\phi)] \} \\ & + \dot{X} \dot{\phi} \{ m [\bar{Y} (-C\psi C\theta C\phi) + \bar{Z} (C\psi C\theta S\phi)] \} \\ & + \dot{Y} \dot{\psi} \{ m [\bar{X} (C\psi S\theta) + \bar{Y} (C\psi C\theta S\phi) + \bar{Z} (C\psi C\theta C\phi)] \} \end{aligned}$$

$$\begin{aligned}
 & +\dot{Y}\dot{\theta}\{m[\bar{X}(S\psi C\theta)+\bar{Y}(-S\psi S\theta S\phi)+\bar{Z}(-S\psi S\theta C\phi)]\} \\
 & +\dot{Y}\dot{\phi}\{m[\bar{Y}(S\psi C\theta C\phi)+\bar{Z}(-S\psi C\theta S\phi)]\} \\
 & +\dot{Z}\dot{\theta}\{m[-\bar{X}(S\theta)-\bar{Y}(C\theta S\phi)-\bar{Z}(C\theta C\phi)]\} \\
 & +\dot{Z}\dot{\phi}\{m[\bar{Y}(-S\theta C\phi)+\bar{Z}(S\theta S\phi)]\}
 \end{aligned} \tag{85}$$

$$\begin{aligned}
 \frac{\partial L}{\partial \theta} = & \dot{\psi}\dot{\theta}\{[I_{zb}-I_{yb}](\frac{1}{2}S\theta S2\phi)+[-I_{xyb}(C\phi)+I_{xzb}(S\phi)](C\theta)+I_{yzb}(S\theta C2\phi)\} \\
 & +\dot{\psi}\dot{\phi}\{[I_{xb}](C\theta)+[I_{xzb}(C\phi)+I_{xyb}(S\phi)](-S\theta)\} \\
 & +\dot{\psi}^2\{[I_{xb}-I_{yb}(S^2\phi)-I_{zb}(C^2\phi)+I_{yzb}(S2\phi)](\frac{1}{2}S2\theta)-[I_{xzb}(C\phi)+I_{xyb}(S\phi)](C2\theta)\} \\
 & +\dot{X}\dot{\psi}\{m[\bar{X}(S\psi S\theta)+\bar{Y}(S\psi C\theta S\phi)+\bar{Z}(S\psi C\theta C\phi)]\} \\
 & +\dot{X}\dot{\theta}\{m[\bar{X}(-C\psi C\theta)+\bar{Y}(C\psi S\theta S\phi)+\bar{Z}(C\psi S\theta C\phi)]\} \\
 & +\dot{X}\dot{\phi}\{m[\bar{Y}(-C\psi C\theta C\phi)+\bar{Z}(C\psi C\theta S\phi)]\} \\
 & +\dot{Y}\dot{\psi}\{m[\bar{X}(C\psi S\theta)+\bar{Y}(C\psi C\theta S\phi)+\bar{Z}(C\psi C\theta C\phi)]\} \\
 & +\dot{Y}\dot{\theta}\{m[\bar{X}(S\psi C\theta)+\bar{Y}(-S\psi S\theta S\phi)+\bar{Z}(-S\psi S\theta C\phi)]\} \\
 & +\dot{Y}\dot{\phi}\{m[\bar{Y}(S\psi C\theta C\phi)+\bar{Z}(-S\psi C\theta S\phi)]\} \\
 & +\dot{Z}\dot{\theta}\{m[\bar{X}(-S\theta)+\bar{Y}(-C\theta S\phi)+\bar{Z}(-C\theta C\phi)]\} \\
 & +\dot{Z}\dot{\phi}\{m[\bar{Y}(-S\theta C\phi)+\bar{Z}(S\theta S\phi)]\} \\
 & -mg[\bar{X}(C\theta)+\bar{Y}(-S\theta S\phi)+\bar{Z}(-S\theta C\phi)]
 \end{aligned} \tag{86}$$

$$\frac{\partial g}{\partial \theta} = \{ \bar{A} \frac{\partial \bar{A}}{\partial \theta} + \bar{B} \frac{\partial \bar{B}}{\partial \theta} + \bar{C} \frac{\partial \bar{C}}{\partial \theta} \} / L_T \quad (87)$$

$$\frac{\partial F}{\partial \theta} = 0 \quad (88)$$

φ Equation

$$\begin{aligned} \frac{d}{dt} \left(\frac{\partial L}{\partial \dot{\phi}} \right) = & \ddot{\psi} \{ I_{xb} (-S\theta) + I_{xyb} (C\theta S\phi) + I_{xzb} (C\theta C\phi) \} \\ & + \ddot{\theta} \{ I_{xyb} (C\phi) - I_{xzb} (S\phi) \} + \ddot{\phi} \{ I_{xb} \} \\ & + \ddot{X} \{ m [\bar{Y} (-C\psi S\theta C\phi - S\psi S\phi) + \bar{Z} (C\psi S\theta S\phi - S\psi C\phi)] \} \\ & + \ddot{Y} \{ m [\bar{Y} (S\psi S\theta C\phi - C\psi S\phi) + \bar{Z} (-S\psi S\theta S\phi - C\psi C\phi)] \} \\ & + \ddot{Z} \{ m [\bar{Y} (C\theta C\phi) + \bar{Z} (-C\theta S\phi)] \} \\ & + \dot{\psi} \dot{\theta} \{ I_{xb} (-C\theta) + [I_{xyb} (S\phi) + I_{xzb} (C\phi)] (-S\theta) \} \\ & + \dot{\psi} \dot{\phi} \{ [I_{xyb} (C\phi) - I_{xzb} (S\phi)] (C\theta) \} \\ & + \dot{\theta} \dot{\phi} \{ -I_{xyb} (S\phi) - I_{xzb} (C\phi) \} \\ & + \dot{X} \dot{\psi} \{ m [\bar{Y} (S\psi S\theta C\phi - C\psi S\phi) + \bar{Z} (-S\psi S\theta S\phi - C\psi C\phi)] \} \\ & + \dot{X} \dot{\theta} \{ m [\bar{Y} (-C\psi C\theta C\phi) + \bar{Z} (C\psi C\theta S\phi)] \} \\ & + \dot{X} \dot{\phi} \{ m [\bar{Y} (C\psi S\theta S\phi - S\psi C\phi) + \bar{Z} (C\psi S\theta C\phi + S\psi S\phi)] \} \end{aligned}$$

$$\begin{aligned}
 & +\dot{Y}\dot{\psi}\{m[\bar{Y}(C\psi S\theta C\phi+S\psi S\phi)+\bar{Z}(-C\psi S\theta S\phi+S\psi C\phi)]\} \\
 & +\dot{Y}\dot{\theta}\{m[\bar{Y}(S\psi C\theta C\phi)+\bar{Z}(-S\psi C\theta S\phi)]\} \\
 & +\dot{Y}\dot{\phi}\{m[\bar{Y}(-S\psi S\theta S\phi-C\psi C\phi)+\bar{Z}(-S\psi S\theta C\phi+C\psi S\phi)]\} \\
 & +\dot{Z}\dot{\theta}\{m[\bar{Y}(-S\theta C\phi)+\bar{Z}(S\theta S\phi)]\}+\dot{Z}\dot{\phi}\{m[\bar{Y}(-C\theta S\phi)+\bar{Z}(-C\theta C\phi)]\} \quad (89)
 \end{aligned}$$

$$\begin{aligned}
 \frac{\partial L}{\partial \phi} = & \dot{\psi}\dot{\theta}\{[(I_{yb}-I_{zb})(C2\phi)+I_{yzb}(2S2\phi)](C\theta)+[I_{xyb}(S\phi)+I_{xzb}(C\phi)](S\theta)\} \\
 & +\dot{\psi}\dot{\phi}\{[I_{xyb}(C\phi)-I_{xzb}(S\phi)](C\theta)\} \\
 & +\dot{\theta}\dot{\phi}\{-I_{xyb}(S\phi)-I_{xzb}(C\phi)\} \\
 & +\dot{\psi}^2\{[(I_{yb}-I_{zb})(\frac{1}{2}S2\phi)-I_{yzb}(C2\phi)](C^2\theta)+[I_{xzb}(S\phi)-I_{xyb}(C\phi)](\frac{1}{2}S2\theta)\} \\
 & +\dot{\theta}^2\{(I_{yb}-I_{zb})(-\frac{1}{2}S2\phi)+I_{yzb}(C2\phi)\} \\
 & +\dot{X}\dot{\psi}\{m[\bar{Y}(S\psi S\theta C\phi-C\psi S\phi)+\bar{Z}(-S\psi S\theta S\phi-C\psi C\phi)]\} \\
 & +\dot{X}\dot{\theta}\{m[\bar{Y}(-C\psi C\theta C\phi)+\bar{Z}(C\psi C\theta S\phi)]\} \\
 & +\dot{X}\dot{\phi}\{m[\bar{Y}(C\psi S\theta S\phi-S\psi C\phi)+\bar{Z}(C\psi S\theta C\phi+S\psi S\phi)]\} \\
 & +\dot{Y}\dot{\psi}\{m[\bar{Y}(C\psi S\theta C\phi+S\psi S\phi)+\bar{Z}(-C\psi S\theta S\phi+S\psi C\phi)]\} \\
 & +\dot{Y}\dot{\theta}\{m[\bar{Y}(S\psi C\theta C\phi)+\bar{Z}(-S\psi C\theta S\phi)]\} \\
 & +\dot{Y}\dot{\phi}\{m[\bar{Y}(-S\psi S\theta S\phi-C\psi C\phi)+\bar{Z}(-S\psi S\theta C\phi+C\psi S\phi)]\}
 \end{aligned}$$

$$\begin{aligned}
 & +\dot{Z}\dot{\theta}\{m[\bar{Y}(-S\theta C\phi)+\bar{Z}(S\theta S\phi)]\} \\
 & +\dot{Z}\dot{\phi}\{m[\bar{Y}(-C\theta S\phi)+\bar{Z}(-C\theta C\phi)]\} \\
 & -mg[\bar{Y}(C\theta C\phi)-\bar{Z}(C\theta S\phi)]\}
 \end{aligned} \tag{90}$$

$$\frac{\partial \bar{q}}{\partial \phi} = \{\bar{A} \frac{\partial \bar{A}}{\partial \phi} + \bar{B} \frac{\partial \bar{B}}{\partial \phi} + \bar{C} \frac{\partial \bar{C}}{\partial \phi}\} / L_T \tag{91}$$

$$\frac{\partial F}{\partial \dot{\phi}} = 0 \tag{92}$$

ψ_p Equation

$$\begin{aligned}
 \frac{d}{dt} \left(\frac{\partial L}{\partial \dot{\psi}_p} \right) &= \ddot{\psi}_p \{I_{xpb}(S^2\theta_p) + I_{ypb}(C^2\theta_p)\} \\
 &+ \dot{\psi}_p \dot{\theta}_p \{[I_{xpb} - I_{ypb}](S2\theta_p)\}
 \end{aligned} \tag{93}$$

$$\begin{aligned}
 \frac{\partial L}{\partial \psi_p} &= \dot{x}_p^2 \{[m_{p\ell} - m_{ps}] [-\frac{1}{2}S2\psi_p C^2\theta_p]\} \\
 &+ \dot{y}_p^2 \{[m_{p\ell} - m_{ps}] [\frac{1}{2}S2\psi_p C^2\theta_p]\} \\
 &+ \dot{x}_p \dot{y}_p [m_{p\ell} - m_{ps}] [-C2\psi_p C^2\theta_p]\} \\
 &+ \dot{x}_p \dot{z}_p \{[m_{p\ell} - m_{ps}] [-\frac{1}{2}S\psi_p S2\theta_p]\} \\
 &+ \dot{y}_p \dot{z}_p [m_{p\ell} - m_{ps}] [-\frac{1}{2}C\psi_p S2\theta_p]\}
 \end{aligned} \tag{94}$$

$$\frac{\partial \bar{g}}{\partial \psi_p} = \{ \bar{A} \frac{\partial \bar{A}}{\partial \psi_p} + \bar{B} \frac{\partial \bar{B}}{\partial \psi_p} \} / L_T \quad (95)$$

$$\frac{\partial F}{\partial \dot{\psi}_p} = 0 \quad (96)$$

θ_p Equation

$$\frac{d}{dt} \left(\frac{\partial L}{\partial \dot{\theta}_p} \right) = I_{ypb} \ddot{\theta}_p \quad (97)$$

$$\begin{aligned} \frac{\partial L}{\partial \theta_p} = & \dot{x}_p^2 \{ [m_{pl} - m_{ps}] [-\frac{1}{2} C^2 \psi_p S 2\theta_p] \} \\ & + \dot{y}_p^2 \{ [m_{pl} - m_{ps}] [-\frac{1}{2} S^2 \psi_p S 2\theta_p] \} \\ & + \dot{z}_p^2 \{ [m_{pl} - m_{ps}] [\frac{1}{2} S 2\theta_p] \} \\ & + \dot{x}_p \dot{y}_p \{ [m_{pl} - m_{ps}] [\frac{1}{2} S 2\psi_p S 2\theta_p] \} \\ & + \dot{x}_p \dot{z}_p \{ [m_{pl} - m_{ps}] [C \psi_p C 2\theta_p] \} \\ & + \dot{y}_p \dot{z}_p \{ [m_{pl} - m_{ps}] [-S \psi_p C 2\theta_p] \} \\ & + \dot{\psi}_p^2 \{ [I_{xpb} - I_{ypb}] [\frac{1}{2} S 2\theta_p] \} \end{aligned} \quad (98)$$

$$\frac{\partial \bar{g}}{\partial \theta_p} = \{ \bar{A} \frac{\partial \bar{A}}{\partial \theta_p} + \bar{B} \frac{\partial \bar{B}}{\partial \theta_p} + \bar{C} \frac{\partial \bar{C}}{\partial \theta_p} \} / L_T \quad (99)$$

$$\frac{\partial F}{\partial \dot{\theta}_p} = 0 \quad (100)$$

L_T Equation

$$\frac{d}{dt} \left(\frac{\partial L}{\partial \dot{L}_T} \right) = 0 \quad (101)$$

$$\frac{\partial L}{\partial L_T} = -K_S (L_T - L_{TO}) \quad (102)$$

$$\frac{\partial \bar{q}}{\partial L_T} = -1 \quad (103)$$

$$\frac{\partial F}{\partial \dot{L}_T} = C_S \dot{L}_T \quad (104)$$

Substituting Equations (101) to (104) into (54) yields:

$$\lambda = -[K_S (L_T - L_{TO}) + C_S \dot{L}_T] \quad (105)$$

The value of λ in Equation (54) is now defined and is expressed in terms of the eleven generalized coordinator and their time derivatives. The eleven simultaneous, nonlinear, coupled differential equations of motion are then written as:

1. X Equation

$$\begin{aligned} & \ddot{X}\{m\} + \ddot{\psi}\{m[\bar{X} C_{12} + \bar{Y} C_{22} + \bar{Z} C_{32}]\} \\ & + \ddot{\theta}\{m[\bar{X}(-C\psi S\theta) + \bar{Y}(-C\psi C\theta S\phi) + \bar{Z}(-C\psi C\theta C\phi)]\} + \ddot{\phi}\{m[\bar{Y}C_{31} - \bar{Z}C_{21}]\} \\ & = \dot{\psi}\dot{\theta}\{-2m[\bar{X}(S\psi S\theta) + \bar{Y}(S\psi C\theta S\phi) + \bar{Z}(S\psi C\theta C\phi)]\} + \dot{\psi}\dot{\phi}\{-2m[\bar{Y}C_{32} - \bar{Z}C_{22}]\} \end{aligned}$$

$$\begin{aligned}
 & + \ddot{\theta} \dot{\phi} \{ 2m [\bar{Y} (C\psi C\theta C\phi) - \bar{Z} (C\psi C\theta S\phi)] \} + \dot{\psi}^2 \{ m [\bar{X}C_{11} + \bar{Y}C_{21} + \bar{Z}C_{31}] \} \\
 & + \dot{\theta}^2 \{ m [\bar{X}C_{11} + \bar{Y} (-C\psi S\theta S\phi) + \bar{Z} (-C\psi S\theta C\phi)] \} + \dot{\phi}^2 \{ m [\bar{Y}C_{21} + \bar{Z}C_{31}] \} \\
 & + [K_s (L_T - L_{TO}) + C_s \dot{L}_T] [\bar{A}/L_T] + F_x
 \end{aligned} \tag{106}$$

2. Y Equation

$$\begin{aligned}
 & \ddot{Y} \{ m \} + \ddot{\psi} \{ -m [\bar{X}C_{11} + \bar{Y}C_{21} + \bar{Z}C_{31}] \} \\
 & + \ddot{\theta} \{ m [\bar{X} (S\psi S\theta) + \bar{Y} (S\psi C\theta S\phi) + \bar{Z} (S\psi C\theta C\phi)] \} + \ddot{\phi} \{ m [\bar{Y}C_{32} - \bar{Z}C_{22}] \} \\
 = & \dot{\psi} \dot{\theta} \{ -2m [\bar{X} (C\psi S\theta) + \bar{Y} (C\psi C\theta S\phi) + \bar{Z} (C\psi C\theta C\phi)] \} + \dot{\psi} \dot{\phi} \{ 2m [\bar{Y}C_{31} - \bar{Z}C_{21}] \} \\
 & + \dot{\theta} \dot{\phi} \{ -2m [\bar{Y} (S\psi C\theta C\phi) - \bar{Z} (S\psi C\theta S\phi)] \} + \dot{\psi}^2 \{ m [\bar{X}C_{12} + \bar{Y}C_{22} + \bar{Z}C_{32}] \} \\
 & + \dot{\theta}^2 \{ m [\bar{X}C_{12} + \bar{Y} (S\psi S\theta S\phi) + \bar{Z} (S\psi S\theta C\phi)] \} + \dot{\phi}^2 \{ m [\bar{Y}C_{22} + \bar{Z}C_{32}] \} \\
 & + [K_s (L_T - L_{TO}) + C_s \dot{L}_T] [\bar{B}/L_T] + F_y
 \end{aligned} \tag{107}$$

3. Z Equation

$$\begin{aligned}
 & \ddot{Z} \{ m \} + \ddot{\theta} \{ m [\bar{X} (C\theta) + \bar{Y} (-S\theta S\phi) + \bar{Z} (-S\theta C\phi)] \} + \ddot{\phi} \{ m [\bar{Y}C_{33} - \bar{Z}C_{23}] \} \\
 = & \dot{\theta} \dot{\phi} \{ 2m [\bar{Y} (S\theta C\phi) - \bar{Z} (S\theta S\phi)] \} + \dot{\theta}^2 \{ m [\bar{X}C_{13} + \bar{Y}C_{23} + \bar{Z}C_{33}] \} \\
 & + \dot{\phi}^2 \{ m [\bar{Y}C_{23} + \bar{Z}C_{33}] \} + [K_s (L_T - L_{TO}) + C_s \dot{L}_T] [\bar{C}/L_T] - mg + F_z
 \end{aligned} \tag{108}$$

4. X_p Equation

$$\begin{aligned}
 & \ddot{X}_p \{m_{p\ell} [C^2\psi_p C^2\theta_p] + m_{ps} [S^2\psi_p + C^2\psi_p S^2\theta_p]\} \\
 & + \ddot{Y}_p \{[m_{p\ell} - m_{ps}] [-\frac{1}{2}S2\psi_p C^2\theta_p]\} + \ddot{Z}_p \{[m_{p\ell} - m_{ps}] [\frac{1}{2}C\psi_p S2\theta_p]\} \\
 = & [m_{p\ell} - m_{ps}] \{\dot{X}_p \dot{\psi}_p [S2\psi_p C^2\theta_p] + \dot{X}_p \dot{\theta}_p [C^2\psi_p S2\theta_p] + \dot{Y}_p \dot{\psi}_p [C2\psi_p C^2\theta_p] \\
 & + \dot{Y}_p \dot{\theta}_p [-\frac{1}{2}S2\psi_p S2\theta_p] + \dot{Z}_p \dot{\psi}_p [\frac{1}{2}S\psi_p S2\theta_p] + \dot{Z}_p \dot{\theta}_p [-C\psi_p C2\theta_p]\} \\
 & - [K_s (L_T - L_{T0}) + C_s \dot{L}_T] [\bar{A}/L_T] + F_{xp}
 \end{aligned} \tag{109}$$

5. Y_p Equation

$$\begin{aligned}
 & \ddot{X}_p \{[m_{p\ell} - m_{ps}] [-\frac{1}{2}S2\psi_p C^2\theta_p]\} + \ddot{Y}_p \{m_{p\ell} [S^2\psi_p C^2\theta_p] + m_{ps} [C^2\psi_p + S^2\psi_p S^2\theta_p]\} \\
 & + \ddot{Z}_p \{[m_{p\ell} - m_{ps}] [-\frac{1}{2}S\psi_p S2\theta_p]\} \\
 = & [m_{p\ell} - m_{ps}] \{\dot{X}_p \dot{\psi}_p [C2\psi_p C^2\theta_p] + \dot{X}_p \dot{\theta}_p [-\frac{1}{2}S2\psi_p S2\theta_p] + \dot{Y}_p \dot{\psi}_p [-S2\psi_p C^2\theta_p] \\
 & + \dot{Y}_p \dot{\theta}_p [S^2\psi_p S2\theta_p] + \dot{Z}_p \dot{\psi}_p [\frac{1}{2}C\psi_p S2\theta_p] + \dot{Z}_p \dot{\theta}_p [S\psi_p C2\theta_p]\} \\
 & - [K_s (L_T - L_{T0}) + C_s \dot{L}_T] [\bar{B}/L_T] + F_{yp}
 \end{aligned} \tag{110}$$

6. z_p Equation

$$\begin{aligned} & \ddot{x}_p \{ [m_{pl} - m_{ps}] [\frac{1}{2} \psi_p S 2\theta_p] \} + \ddot{y}_p \{ [m_{pl} - m_{ps}] [\frac{1}{2} S \psi_p S 2\theta_p] \} \\ & + \ddot{z}_p \{ m_{pl} [S^2 \theta_p] + m_{ps} [C^2 \theta_p] \} \\ = & [m_{pl} - m_{ps}] \{ \dot{x}_p \dot{\psi}_p [\frac{1}{2} S \psi_p S 2\theta_p] + \dot{x}_p \dot{\theta}_p [-C \psi_p C 2\theta_p] + \dot{y}_p \dot{\psi}_p [\frac{1}{2} C \psi_p S 2\theta_p] \\ & + \dot{y}_p \dot{\theta}_p [S \psi_p C 2\theta_p] + \dot{z}_p \dot{\theta}_p [-S 2\theta_p] \} \\ & - [K_s (L_T - L_{T0}) + C_s \dot{L}_T] [\bar{C}/L_T] - m_p g + F_{zp} \end{aligned} \quad (111)$$

7. ψ Equation

$$\begin{aligned} & \ddot{\psi} \{ I_{xb} (S^2 \theta) + [I_{yb} (S^2 \phi) + I_{zb} (C^2 \phi)] (C^2 \theta) + I_{yzb} (-C^2 \theta S 2\phi) \\ & + [I_{xzb} (C \phi) + I_{xyb} (S \phi)] (-S 2\theta) \} + \ddot{\theta} \{ [(I_{yb} - I_{zb}) (\frac{1}{2} S 2\phi) - I_{yzb} (C 2\phi)] (C \theta) \\ & + [I_{xzb} (S \phi) - I_{xyb} (C \phi)] (S \theta) \} + \ddot{\phi} \{ -I_{xb} C_{13} + I_{xyb} C_{23} + I_{xzb} C_{33} \} \\ & + \ddot{x} \{ m [\bar{X} C_{12} + \bar{Y} C_{22} + \bar{Z} C_{32}] \} + \ddot{y} \{ -m [\bar{X} C_{11} + \bar{Y} C_{21} + \bar{Z} C_{31}] \} \\ = & \dot{\psi} \dot{\theta} \{ [I_{xb} - I_{yb} (S^2 \phi) - I_{zb} (C^2 \phi) + I_{yzb} (S 2\phi)] (-S 2\theta) + [I_{xzb} (C \phi) \\ & + I_{xyb} (S \phi)] (2C 2\theta) \} + \dot{\psi} \dot{\phi} \{ [(I_{yb} - I_{zb}) (S 2\phi) - I_{yzb} (2C 2\phi)] (-C^2 \theta) \\ & + [I_{xzb} (S \phi) - I_{xyb} (C \phi)] (-S 2\theta) \} + \dot{\theta} \dot{\phi} \{ [I_{xb} - (I_{yb} - I_{zb}) (C 2\phi) - I_{yzb} (2S 2\phi)] (C \theta) \} \\ & + \dot{\theta}^2 \{ [(I_{yb} - I_{zb}) (\frac{1}{2} S 2\phi) - I_{yzb} (C 2\phi)] (S \theta) - I_{xzb} C_{23} + I_{xyb} C_{33} \} \end{aligned}$$

$$\begin{aligned}
 & +\dot{\phi}^2 \{-I_{xyb} C_{33} + I_{xzb} C_{23}\} \\
 & - [K_S (L_T - L_{TO}) + C_S \dot{L}_T] [\bar{A} \frac{\partial \bar{A}}{\partial \psi} + \bar{B} \frac{\partial \bar{B}}{\partial \psi}] / L_T + Q_\psi
 \end{aligned} \tag{112}$$

8. θ Equation

$$\begin{aligned}
 & \ddot{X}\{m[\bar{X}(-C\psi S\theta) + \bar{Y}(-C\psi C\theta S\phi) + \bar{Z}(-C\psi C\theta C\phi)]\} \\
 & + \ddot{Y}\{m[\bar{X}(S\psi S\theta) + \bar{Y}(S\psi C\theta S\phi) + \bar{Z}(S\psi C\theta C\phi)]\} \\
 & + \ddot{Z}\{m[\bar{X}(C\theta) + \bar{Y}(-S\theta S\phi) + \bar{Z}(-S\theta C\phi)]\} \\
 & + \ddot{\psi}\{[(I_{yb} - I_{zb})\frac{1}{2}S2\phi - I_{yzb}(C2\phi)](C\theta) + [I_{xyb}(C\phi) - I_{xzb}(S\phi)](-S\theta)\} \\
 & + \ddot{\theta}\{I_{yb}(C^2\phi) + I_{zb}(S^2\phi) + I_{yzb}(S2\phi)\} + \ddot{\phi}\{I_{xyb}(C\phi) - I_{xzb}(S\phi)\} \\
 = & \ddot{\psi}\{[I_{xb} + (I_{yb} - I_{zb})(C2\phi) + I_{yzb}(2S2\phi)](-C\theta) + [I_{xzb}(C\phi) + I_{xyb}(S\phi)](-2S\theta)\} \\
 & + \ddot{\theta}\{(I_{yb} - I_{zb})(S2\phi) - I_{yzb}(2C2\phi)\} \\
 & + \ddot{\psi}^2\{[I_{xb} - I_{yb}(S^2\phi) - I_{zb}(C^2\phi) + I_{yzb}(S2\phi)](\frac{1}{2}S2\theta) + [I_{xzb}(C\phi) \\
 & + I_{xyb}(S\phi)](-C2\theta)\} + \dot{\phi}^2\{I_{xyb}(S\phi) + I_{xzb}(C\phi)\} - mg[\bar{X}(C\theta) + \bar{Y}(-S\theta S\phi) + \bar{Z}(-S\theta C\phi)] \\
 & - [K_S (L_T - L_{TO}) + C_S \dot{L}_T] [\bar{A} \frac{\partial \bar{A}}{\partial \theta} + \bar{B} \frac{\partial \bar{B}}{\partial \theta} + \bar{C} \frac{\partial \bar{C}}{\partial \theta}] / L_T + Q_\theta
 \end{aligned} \tag{113}$$

9. ϕ Equation

$$\begin{aligned}
 & \ddot{X}\{m[\bar{Y}C_{31} - \bar{Z}C_{21}]\} + \ddot{Y}\{m[\bar{Y}C_{32} - \bar{Z}C_{22}]\} + \ddot{Z}\{m[\bar{Y}C_{33} - \bar{Z}C_{23}]\} \\
 & + \ddot{\psi}\{-I_{xb}C_{13} + I_{xyb}C_{23} + I_{xzb}C_{33}\} + \ddot{\theta}\{I_{xyb}(C\phi) - I_{xzb}(S\phi)\} + \ddot{\phi}\{I_{xb}\}
 \end{aligned}$$

$$\begin{aligned}
 = & \dot{\psi} \dot{\theta} \{ [I_{x_b} + (I_{y_b} - I_{z_b}) (C2\phi) + I_{y_{zb}} (2S2\phi)] (C\theta) + [I_{x_{yb}} (S\phi) + I_{x_{zb}} (C\phi)] (2S\theta) \} \\
 & + \dot{\psi}^2 \{ [(I_{y_b} - I_{z_b}) (\frac{1}{2}S2\phi) - I_{y_{zb}} (C2\phi)] (C^2\theta) + [I_{x_{zb}} (S\phi) - I_{x_{yb}} (C\phi)] (\frac{1}{2}S2\theta) \} \\
 & + \dot{\theta}^2 \{ (I_{y_b} - I_{z_b}) (-\frac{1}{2}S2\phi) + I_{y_{zb}} (C2\phi) \} - mg [\bar{Y}C_{33} - \bar{Z}C_{23}] \\
 & - [K_S (L_T - L_{T0}) + C_S \dot{L}_T] [\bar{A} \frac{\partial \bar{A}}{\partial \phi} + \bar{B} \frac{\partial \bar{B}}{\partial \phi} + \bar{C} \frac{\partial \bar{C}}{\partial \phi}] / L_T + Q_\phi
 \end{aligned} \tag{114}$$

10. ψ_p Equation

$$\begin{aligned}
 & \ddot{\psi}_p \{ I_{x_{pb}} (S^2\theta_p) + I_{y_{pb}} (C^2\theta_p) \} \\
 = & \dot{\psi}_p \dot{\theta}_p \{ (I_{x_{pb}} - I_{y_{pb}}) (-S2\theta_p) \} + [m_{p\ell} - m_{ps}] \{ \dot{x}_p \dot{y}_p [-C2\psi_p C^2\theta_p] \\
 & + \dot{x}_p \dot{z}_p [-\frac{1}{2}S\psi_p S2\theta_p] + \dot{y}_p \dot{z}_p [-\frac{1}{2}C\psi_p S2\theta_p] + \dot{x}_p^2 [-\frac{1}{2}S2\psi_p C^2\theta_p] + \dot{y}_p^2 [\frac{1}{2}S2\psi_p C^2\theta_p] \} \\
 & - [K_S (L_T - L_{T0}) + C_S \dot{L}_T] [\bar{A} \frac{\partial \bar{A}}{\partial \psi_p} + \bar{B} \frac{\partial \bar{B}}{\partial \psi_p}] / L_T + Q_{\psi_p}
 \end{aligned} \tag{115}$$

11. θ_p Equation

$$\begin{aligned}
 & \ddot{\theta}_p \{ I_{y_{pb}} \} \\
 = & \dot{\psi}_p^2 \{ (I_{x_{pb}} - I_{y_{pb}}) (\frac{1}{2}S2\theta_p) \} + [m_{p\ell} - m_{ps}] \{ \dot{x}_p \dot{y}_p [\frac{1}{2}S2\psi_p S2\theta_p] + \dot{x}_p \dot{z}_p [C\psi_p C2\theta_p] \\
 & + \dot{y}_p \dot{z}_p [-S\psi_p C2\theta_p] + \dot{x}_p^2 [-\frac{1}{2}C^2\psi_p S2\theta_p] + \dot{y}_p^2 [-\frac{1}{2}S^2\psi_p S2\theta_p] + \dot{z}_p^2 [\frac{1}{2}S2\theta_p] \} \\
 & - [K_S (L_T - L_{T0}) + C_S \dot{L}_T] [\bar{A} \frac{\partial \bar{A}}{\partial \theta_p} + \bar{B} \frac{\partial \bar{B}}{\partial \theta_p} + \bar{C} \frac{\partial \bar{C}}{\partial \theta_p}] / L_T + Q_{\theta_p}
 \end{aligned} \tag{116}$$

SECTION 8 - SIMPLIFIED EQUATIONS OF MOTION

Equations (106) to (116) are for the most general situation possible, and as a result, are quite lengthy. Under some circumstances, these equations can be simplified. If this can be accomplished, a significant decrease in computer time will be realized. The first simplification occurs if the forebody's aerodynamic (body) reference axes are principal axes. In this case $\bar{X} = \bar{Y} = \bar{Z} = 0$ and $I_{xyb} = I_{xzb} = I_{yzb} = 0$. Equations (106), (107), (108), (112), (113), and (114) become:

$$\ddot{X}\{m\} = [K_S (L_T - L_{TO}) + C_S \dot{L}_T] [\bar{A}/L_T] + F_x \quad (117)$$

$$\ddot{Y}\{m\} = [K_S (L_T - L_{TO}) + C_S \dot{L}_T] [\bar{B}/L_T] + F_y \quad (118)$$

$$\ddot{Z}\{m\} = [K_S (L_T - L_{TO}) + C_S \dot{L}_T] [\bar{C}/L_T] - mg + F_z \quad (119)$$

$$\begin{aligned} & \ddot{\psi} \{ I_{xb} (S^2 \theta) + [I_{yb} (S^2 \phi) + I_{zb} (C^2 \phi)] (C^2 \theta) \} + \ddot{\theta} \{ (I_{yb} - I_{zb}) (\frac{1}{2} C \theta S 2 \phi) \} + \ddot{\phi} \{ -I_{xb} C_{13} \} \\ & = \ddot{\psi} \dot{\theta} \{ [I_{xb} - I_{yb} (S^2 \phi) - I_{zb} (C^2 \phi)] (-S 2 \theta) \} + \ddot{\psi} \dot{\phi} \{ (I_{yb} - I_{zb}) (-C^2 \theta S 2 \phi) \} \\ & + \dot{\theta} \dot{\phi} \{ [I_{xb} - (I_{yb} - I_{zb}) (C 2 \phi)] (C \theta) \} + \dot{\theta}^2 \{ (I_{yb} - I_{zb}) (\frac{1}{2} S \theta S 2 \phi) \} \\ & - [K_S (L_T - L_{TO}) + C_S \dot{L}_T] [\bar{A} \frac{\partial \bar{A}}{\partial \psi} + \bar{B} \frac{\partial \bar{B}}{\partial \psi}] / L_T + Q_\psi \end{aligned} \quad (120)$$

$$\begin{aligned} & \ddot{\psi} \{ I_{yb} - I_{zb} \} (\frac{1}{2} C \theta S 2 \phi) \} + \ddot{\theta} \{ I_{yb} (C^2 \phi) + I_{zb} (S^2 \phi) \} \\ & = \ddot{\psi} \dot{\phi} \{ [I_{xb} + (I_{yb} - I_{zb}) (C 2 \phi)] (-C \theta) \} + \dot{\theta} \dot{\phi} \{ (I_{yb} - I_{zb}) (S 2 \phi) \} \\ & \ddot{\psi}^2 \{ [I_{xb} - I_{yb} (S^2 \phi) - I_{zb} (C^2 \phi)] (\frac{1}{2} S 2 \theta) \} \end{aligned}$$

$$- [K_S (L_T - L_{T0}) + C_S \dot{L}_T] [\bar{A} \frac{\partial \bar{A}}{\partial \theta} + \bar{B} \frac{\partial \bar{B}}{\partial \theta} + \bar{C} \frac{\partial \bar{C}}{\partial \theta}] / L_T + Q_\theta \quad (121)$$

$$\begin{aligned} & \ddot{\psi} \{-I_{xb} C_{13}\} + \ddot{\phi} \{I_{xb}\} \\ & = \dot{\psi} \dot{\theta} \{ [I_{xb} + (I_{yb} - I_{zb}) (C^2 \phi)] (C \theta) \} + \dot{\psi}^2 \{ (I_{yb} - I_{zb}) (\frac{1}{2} C^2 \theta S 2 \phi) \} \\ & \quad + \dot{\theta}^2 \{ (I_{yb} - I_{zb}) (-\frac{1}{2} S 2 \phi) \} \\ & - [K_S (L_T - L_{T0}) + C_S \dot{L}_T] [\bar{A} \frac{\partial \bar{A}}{\partial \phi} + \bar{B} \frac{\partial \bar{B}}{\partial \phi} + \bar{C} \frac{\partial \bar{C}}{\partial \phi}] / L_T + Q_\phi \end{aligned} \quad (122)$$

The above six equations of motion have not only been shortened, but they also have been uncoupled in the translational accelerations making them easier to solve. The second simplification involves the decelerator degrees of freedom. If the added masses of the decelerator are ignored ($m_{pl} = m_{ps} = m_p$), Equations (109), (110), (111), (115), and (116) become:

$$\ddot{X}_p \{m_p\} = - [K_S (L_T - L_{T0}) + C_S \dot{L}_T] (\bar{A} / L_T) + F_{xp} \quad (123)$$

$$\ddot{Y}_p \{m_p\} = - [K_S (L_T - L_{T0}) + C_S \dot{L}_T] (\bar{B} / L_T) + F_{yp} \quad (124)$$

$$\ddot{Z}_p \{m_p\} = - [K_S (L_T - L_{T0}) + C_S \dot{L}_T] (\bar{C} / L_T) - m_p g + F_{zp} \quad (125)$$

$$\ddot{\psi}_p \{I_{xpb} (S^2 \theta_p) + I_{ypb} (C^2 \theta_p)\} = \dot{\psi}_p \dot{\theta}_p \{ (I_{xpb} - I_{ypb}) (-S 2 \theta_p) \} \\ - [K_s (L_T - L_{TO}) + C_s \dot{L}_T] [\bar{A} \frac{\partial \bar{A}}{\partial \psi_p} + \bar{B} \frac{\partial \bar{B}}{\partial \psi_p}] / L_T + Q_{\psi p} \quad (126)$$

$$\ddot{\theta}_p \{I_{ypb}\} = \dot{\psi}_p^2 \{ (I_{xpb} - I_{ypb}) (\frac{1}{2} S 2 \theta_p) \} \\ - [K_s (L_T - L_{TO}) + C_s \dot{L}_T] [\bar{A} \frac{\partial \bar{A}}{\partial \theta_p} + \bar{B} \frac{\partial \bar{B}}{\partial \theta_p} + \bar{C} \frac{\partial \bar{C}}{\partial \theta_p}] / L_T + Q_{\theta p} \quad (127)$$

Like the simplified equation for the forebody, the decelerator equations have also shortened. Furthermore, they have completely uncoupled in the second derivatives making numerical integration easy.

SECTION 9 - GENERALIZED FORCES - AERODYNAMICS

The nonconservative forces acting on the forebody are due to aerodynamics. The aerodynamics and the convention used in this report apply to the Space Shuttle Solid Rocket Booster (S.R.B.). If a different body is to be simulated, the aerodynamic coefficients and possibly the convention used to define them, would change.

For the S.R.B., the aerodynamics are a function of roll angle, angle-of-attack, and Mach number. The angle-of-attack is measured from the total velocity vector to the positive longitudinal axis (X_b) as shown in Figure 3.

$$\alpha = \tan^{-1} \left[\frac{(\dot{Y}_b^2 + \dot{Z}_b^2)^{1/2}}{\dot{X}_b} \right] \quad (128)$$

The normal force coefficient, C_N , is in the plane formed by the velocity vector and the longitudinal axis, and is perpendicular to the longitudinal axis (X_b). The roll angle, ϕ_i , is then measured from the normal force coefficient to the Z_b body axis. The axial force coefficient is defined as usual, positive in the negative X_b direction. Finally, the side force coefficient is perpendicular to the X_b body axis and to the normal force, such that the directions of C_A , C_N , C_Y form a right-handed orthogonal coordinate system. Mathematically, the aerodynamics roll angle is given by:

$$\phi_i = \tan^{-1} [-\dot{Y}_b / -\dot{Z}_b] \quad (129)$$

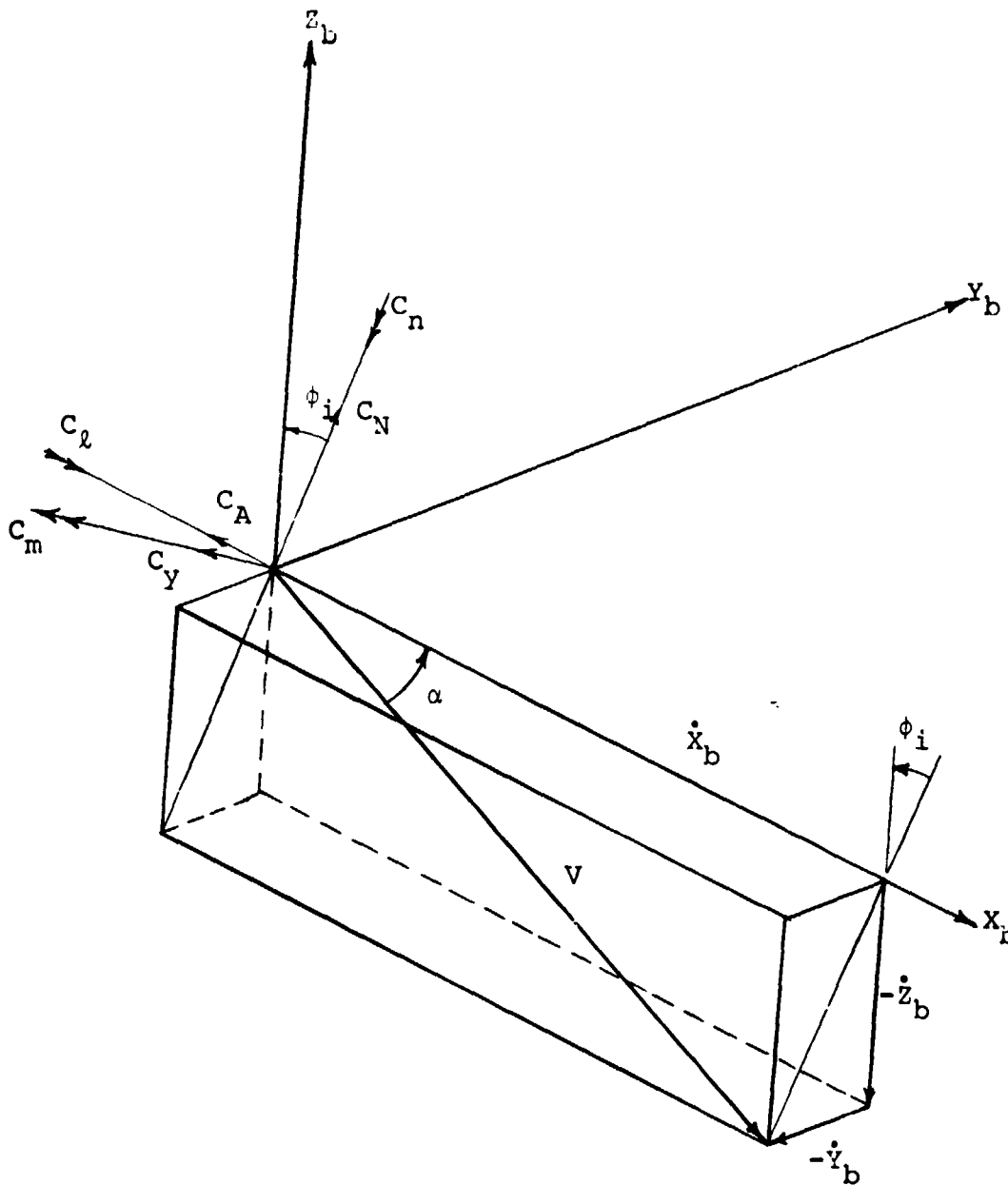


FIGURE 3 - AERODYNAMIC COORDINATE SYSTEM

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The positive directions of the moment coefficients are shown in Figure 3 as double arrows. Damping moment coefficients are about the body axes (X_b, Y_b, Z_b). Aerodynamic body axes forces are given as:

$$F_{xb} = -q S C_A \quad (130)$$

$$F_{yb} = qS[-C_Y C\phi_i + C_N S\phi_i] \quad (131)$$

$$F_{zb} = qS[C_Y S\phi_i + C_N C\phi_i] \quad (132)$$

The body axes forces are converted to inertial axes force using the elements of $[C]$, Equation 4.

$$F_x = F_{xb} C_{11} + F_{yb} C_{21} + F_{zb} C_{31} \quad (133)$$

$$F_y = F_{xb} C_{12} + F_{yb} C_{22} + F_{zb} C_{32} \quad (134)$$

$$F_z = F_{xb} C_{13} + F_{yb} C_{23} + F_{zb} C_{33} - mg \quad (135)$$

Body axes torques are:

$$T_{xb} = qSd[C_\ell + C_{\ell p}(\frac{\omega_{xb}^d}{2V})] \quad (136)$$

$$T_{yb} = qSd[-C_m C\phi_i - C_n S\phi_i + C_{m_q}(\frac{\omega_{yb}^d}{2V})] \quad (137)$$

$$T_{zb} = qSd[C_m S\phi_i - C_n C\phi_i + C_{n_r}(\frac{\omega_{zb}^d}{2V})] \quad (138)$$

The body axis torques are transformed to generalized torques using Equations (5) and (1) and noting sign conventions.

$$Q_{\psi} = -[T_{xb}C_{13} + T_{yb}C_{23} + T_{zb}C_{33}] \quad (139)$$

$$Q_{\theta} = -T_{yb}C_{\phi} + T_{zb}S_{\phi} \quad (140)$$

$$Q_{\phi} = T_{xb} \quad (141)$$

The aerodynamics of a decelerator (parachute) are not well known because a parachute is not a rigid body, and does not lend itself to easily obtainable test data, especially under dynamic conditions. Consequently the aerodynamics of a symmetric decelerator tend to be relatively simple due to a lack of better understanding rather than the inability to use available information. If better aerodynamic data is attainable, it is a simple matter to alter the body forces and torques appropriately.

For this report, the decelerator body forces and torques are:

$$F_{xpb} = -q_p S_p C_{Ap} \quad (142)$$

$$F_{ypb} = q_p S_p C_{NP} S_{\phi_{pi}} \quad (143)$$

$$F_{zpb} = q_p S_p C_{NP} C_{\phi_{pi}} \quad (144)$$

$$T_{ypb} = -q_p S_p d_p (C_{MP} - 0.1 * \dot{\theta}_p * D_p/V_p) C_{\phi_{pi}} \quad (145)$$

$$T_{zpb} = q_p S_p d_p (C_{MP} - 0.1 * \dot{\theta}_p * D_p/V_p) S_{\phi_{pi}} \quad (146)$$

$$\phi_{pi} = \tan^{-1}[-\dot{y}_{pb}/-\dot{z}_{pb}] \quad (147)$$

The generalized forces for the decelerator are:

$$F_{xp} = F_{xpb} C_{p11} + F_{ypb} C_{p21} + F_{zpb} C_{p31} \quad (148)$$

$$F_{yp} = F_{xpb} C_{p12} + F_{ypb} C_{p22} + F_{zpb} C_{p32} \quad (149)$$

$$F_{zp} = F_{xpb} C_{p13} + F_{zpb} C_{p33} - m_p g \quad (150)$$

$$Q_{\psi p} = -T_{zpb} C_{p33} \quad (151)$$

$$Q_{\theta p} = -T_{ypb} \quad (152)$$

CHAPTER III COMPUTER PROGRAM

SECTION 1 - FEATURES OF THE COMPUTER PROGRAM

The computer program contains the following features.

1. The program has many options which simplify the input of data or decrease the program run time. Use of the options are contained in the listing of the program as comment cards. These options are:
 - a. Options are included which change the dimensions of the aerodynamic coefficient arrays as dictated by input requirements.
 - b. An option is provided (OPDT = 1.0) which automatically determines the magnitude of the integration time interval, DT.
 - c. An option is provided (OPSP = 1.0) which calculates the parachute drag area (SP) time history. If this option is not used the drag area versus time is input into the program in the form of look-up arrays.
 - d. An option for including longitudinal and lateral added air mass effects on the parachute (OPAM = 1.0) is included in the program.
 - e. A provision is made to use simplified equations of motion (OPOS = 0.0) to reduce run time, if all the forebody products of inertia and center of mass offsets are equal to zero.
 - f. An option (OPPLOT = 1.0) for making a plot tape is available.
 - g. English or metric systems may be used for data input and out by equating OMETRC to 0.0 or 1.0 respectively.
2. All aerodynamic coefficients are read into the program as functions of angle of attack, roll angle, and mach number in the form of three dimensional look-up arrays.

3. The initial start conditions for the forebody and aft body are completely general.
4. The stacking of design cases is possible.
5. The attachment location of the tether to the forebody is completely general.
6. The tether load and the angle it makes with the centerline of the forebody are program outputs.
7. All load and trajectory data are output at pre-selected times.
8. Termination of a design case occurs at a predetermined time or altitude.
9. The program calculates the effective system spring constant.
10. The program calculates the parachute physical properties as the parachute inflates as a function of time.
11. The parachute may have three stages of reefing, if the automatic drag area versus time option is chosen.
12. As the parachute inflates, the drag area versus time follows a second degree curve ($y = ax^2$).

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SECTION 2 - INPUT

Except for the variable COM, all inputs are read in under the format statement 8F10.0. COM is an 80 column header card. All of the following variables are defined in the nomenclature.

<u>INPUT ITEM</u>	<u>VARIABLE</u>	<u>NUMBER OF CARDS</u>
a)	AIPHI, AIPHID, AJALPF, AJALPM, AKAM, AKAMD, OPSYM, OPDA	1 card
b)	PPHIE	1 card
c)	AALPFE	1 or 2 cards
d)	AALPME	1 or 2 cards
e)	AAM	1 card
f)	CCA	4 to 128 cards
g)	CCN	4 to 128 cards
h)	CCLM	4 to 128 cards
i)	CCY	0 or 4 to 128 cards
j)	CCLL	0 or 4 to 128 cards
k)	CCLN	0 or 4 to 128 cards
l)	CLLP, CLMQ, CLNR	0 or 1 card
m)	PPHIDE	0 or 1 card
n)	AALPDE	0 or 1 card
o)	AAMD	0 or 1 card
p)	CCLLP	0 or 4 to 64 cards
q)	CCLMQ	0 or 4 to 64 cards
r)	CCLNR	0 or 4 to 64 cards
s)	AALPPE	1 card
t)	AAMP	1 card
u)	CCAP	2 to 8 cards
v)	CCNP	2 to 8 cards
w)	CCMP	2 to 8 cards

<u>INPUT ITEM</u>	<u>VARIABLE</u>	<u>NUMBER OF CARDS</u>
x)	PS, PT, EPL, EPT	1 card
y)	X, Y, X, V, GAME, CHIE, EPSI, ETAI	1 card
z)	WT, LXB, IYB, IZB, IXYB, IXZB, IYZB	1 card
aa)	S, D, XBAR, YBAR, ZBAR, OPPRIN, OPLOT, OPOS	1 card
bb)	PSIE, THEE, PHIE, OMXBE, OMYBE, OMZBE	1 card
cc)	A, B, C, OPAM, OMETRC	1 card
dd)	PSIPE, THEPE, PSIPDE, THEPDE, VP, GAMPE, CHIE	1 card
ee)	LS, LTO, DLTO, NS, NT, DP, CCRIT	1 card
ff)	AMAX1, AMAX2, DSX1, DSX2, AMAY1, AMAY2, DSY1, DSY2	1 card
gg)	WTC, WTL, OPSP, OPDT IF (OPSP.EQ.0.0) GO TO ITEM kk)	
hh)	TRO, TR1, TR2, TR3	1 card
jj)	SPRO, SPR1, SPR2, SPR3, PCT01, PCT02, PCT03, POROS	1 card
kk)	TTIP, SSP IF (OPDT.EQ.0.0) GO TO ITEM mm)	4 cards
ll)	GLOAD, FSULT, AERATO, TO, DTP1, TTT, HHH	1 card
mm)	DT1, TO, DTP1, TTT, HHH	1 card
nn)	COM	1 card

The values of the variables read in input item "a" determine, in part, the sizes of the aerodynamic arrays. The axial and moment coefficients have the option of using either eight or sixteen angles-of-attack (one or two cards). If, for example, five or eleven angles-of-attack are needed, one or two cards are needed respectively. The roll and Mach number arrays may vary from two to eight. As an example consider the array CCA where the value of C_A depends on five roll angles (ϕ_i), eleven angles-of-attack (α) and seven Mach numbers (AM). The array PPHIE would be read in on one card containing five distinct roll angles, the last three fields of ten digits would be blanks. The array AALPFE would be read in on two cards. The first card would contain eight distinct angles-of-attack, and the second card would contain three distinct angles-of-attack and five blank fields of ten digits. The array AAM would be read in on one card containing seven distinct Mach numbers and one blank field of ten digits. The first element in each of the above arrays should start at zero and increase numerically until it is highest

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possible value expected to be encountered is specified. In this particular example, the array size used will be CCA(5, 16, 7). The proper read sequence is to first read two cards containing the values of C_A at eleven angle -of-attack, the initial roll angle (zero) and the initial Mach number (zero). These cards are followed by two cards containing values of C_A at eleven angles-of-attack, the second roll angle and the initial Mach number. This is continued for five roll angles at the initial Mach number. After these ten cards, the same procedure is followed for the second Mach number, and the third, etc. up to seven sets of ten cards.

All the aerodynamic coefficient arrays are read similarly. However, notice that the angle-of-attack array associated with the moment coefficients is different than that associated with the force coefficients. Also, the damping moment coefficient arrays (input items "p", "q", and "r") may not be read in at all, depending on the value of OPDA. Instead, input item "l" can be used if the damping coefficients are constant. Finally, the damping coefficients correspond to the arrays read in input items "m", "n", and "o".

Figure 4 helps to clarify the meaning of the input parameters associated with the added air mass on the parachute (Ref. Input Item ff).

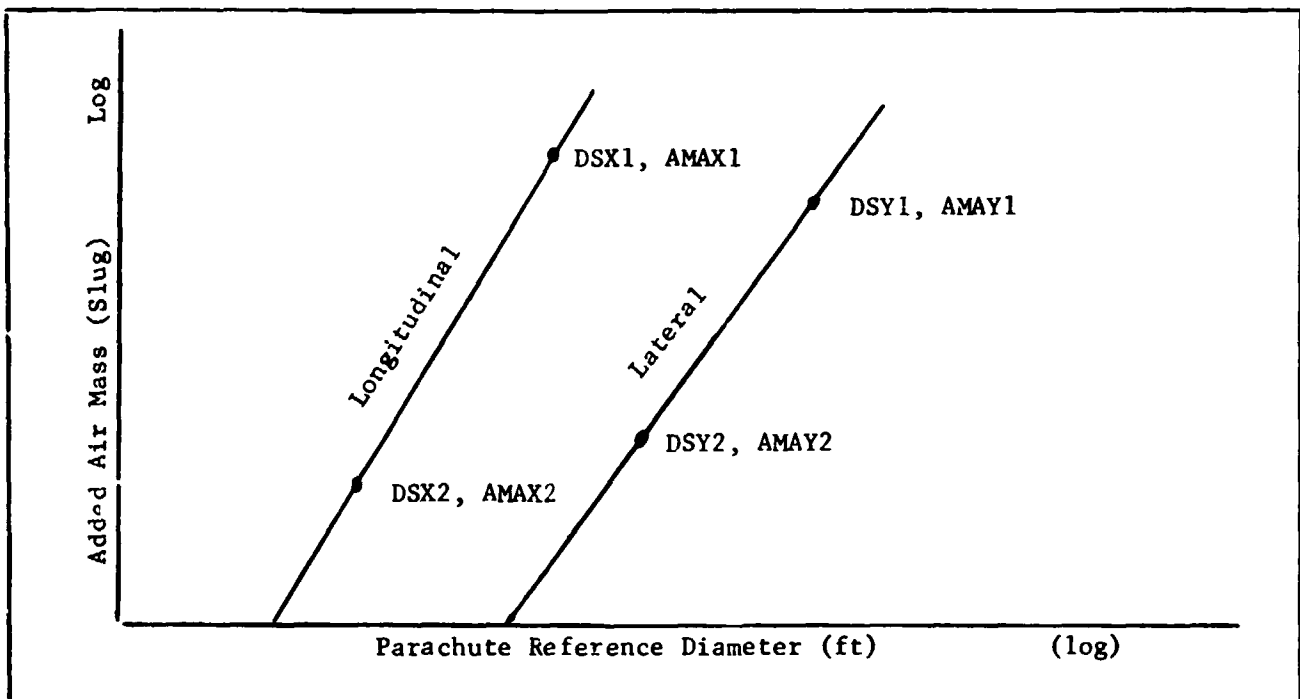


Figure 4. Input Parameters for Parachute Added Air Mass

Figure 5 helps to clarify the meaning of the parameters associated with OPSO = 1.0 which directs the program to calculate the parachute area time history as time advances (Reference Input Items hh and jj).

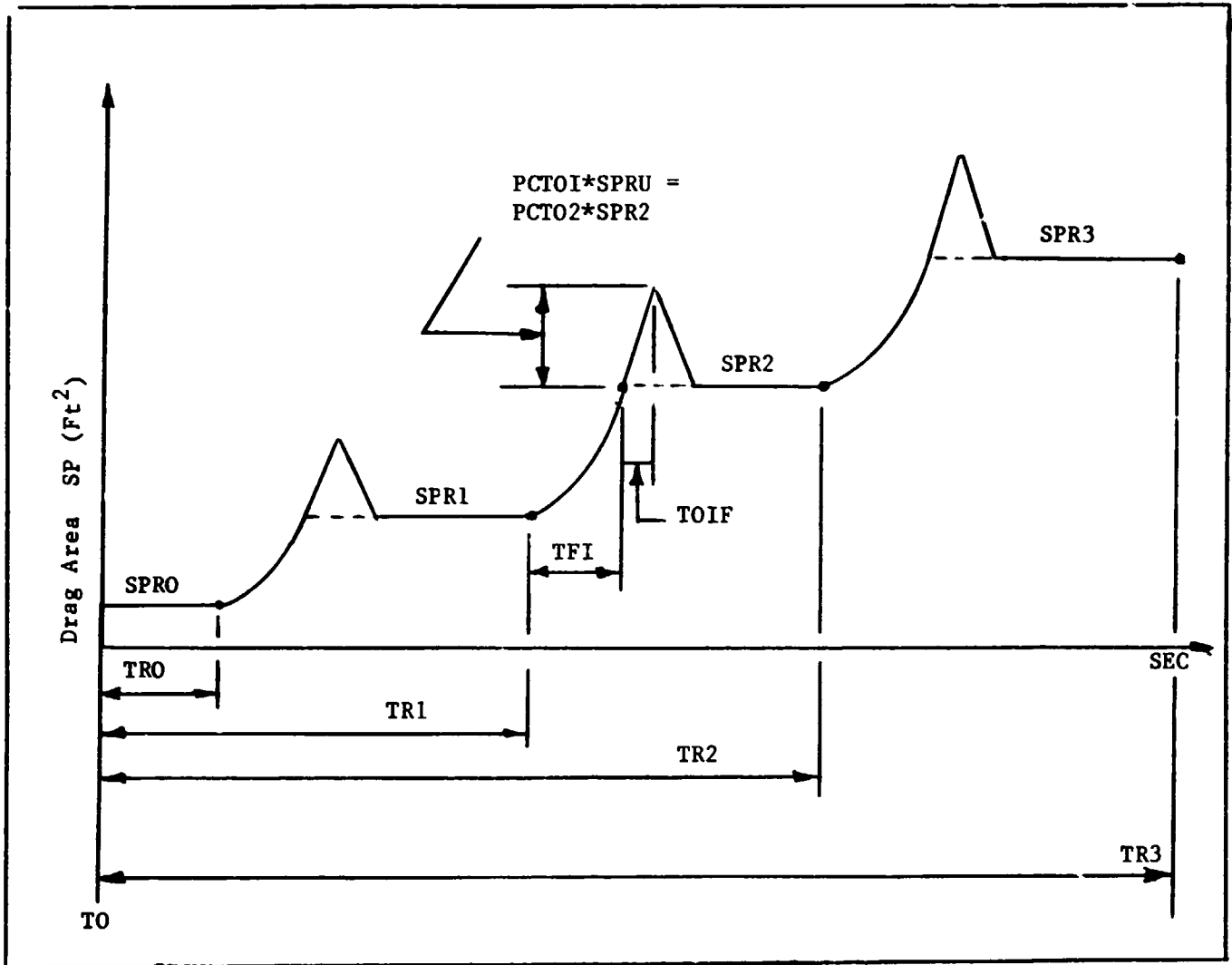


Figure 5. Parameters for Program Calculated Parachute Drag Area Time History

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SECTION 3 - OUTPUT

All output variables are defined in the nomenclature. Before beginning the simulation, the following variables, specifying the characteristics of the rigid body and initial parameters, are printed out.

Line 1. COM
Line 2. IXB, IXYB, XBAR, S, CLIP, OPPRIN, OPSYM, AIPHI, AIPHID, DT1 EPSI
Line 3. IYB, IXZB, YBAR, D, CLMQ, OPPLT, OPDA, AJALPF, AJALPM, AJALPD,
TTT, ETA1
Line 4. IZB, IYZB, ZBAR, WT, CLNR, OPOS, OMETRC, AKAM, AKAMD, HHH

If CLLP, CLMQ, and CLNR are constants for the simulation, their values are printed out in the appropriate place. If the damping coefficients are found from interpolation of three dimensional arrays, CLLP, CLMQ, and CLNR are set equal to zero for this printout only. Several variables dealing with the decelerator are then printed out.

Line 5. A, LTO, LS, AMAX1, AMAX2, AMAY1, AMAY2, AP, GLOAD, FREQP, OPAM,
PCTO1
Line 6. B, NT, NS, DSK1, DSK2, DSY1, DSY2, CHIPE, FSULT, POROS, OPDT,
PCTO2
Line 7. C, DLTO, DP, WTC, WTL, WTP, CCRIT, VP, AERATO, TO OPSO, PCTO3
Line 8. TRO, TR1, TR2, TR3, SPRO, SPR1, SPR2, SPR3

The parachute suspension line load and strain arrays are printed out next on Lines 9 and 10.

Line 9. PS(I)
Line 10. EPL(I)

The tether line load and strain arrays are printed out next on Lines 11 and 12.

Line 11. PT(I)
Line 12. EPT(I)

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The parachute inflation time history array and drag area array are printed out next. If the option (OPSP = 1.0) the arrays are set equal to zero because they are not known before initial time T0.

Line 13. TTIP(I)

Line 14. SSP(I)

The computer program then checks the option variable OPPRIN. If OPPRIN = 1., all the aerodynamic data is listed as follows:

PPHIE(I)
AALPFE(J)
AALPME(J)
AAM(K)

CCA(I,J,K)
CCN(I,J,K)
CCLM(I,J,K)

If OPSYM = 0., the following aerodynamic data is listed

CCY(I,J,K)
CCLL(I,J,K)
CCLN(I,J,K)

In the above aerodynamic coefficient arrays, AALPFE(J) is associated with CCA, CCN, and CCY; AALPME(J) is associated with CCLM, CCLL, and CCLN.

If OPDA = 1., the damping aerodynamics is listed.

PPHIDE(I)
AALPDE(J)
AAMD(K)

CCLLP(I,J,K)
CCLMQ(I,J,K)
CCLNR(I,J,K)

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The aerodynamic arrays associated with the decelerator then follow.

AALPPE(I)

AAMP(I)

CCAP(I)

CCNP(I)

CCMP(I)

After the listing of the input data, the computer program begins numerically integrating. At $T = T_0$ and at predetermined time increments, the following data is printed out.

Line 1. T, X, XD, XDD, FX, CA, V, TENS, XP, XPD, XPDD, FXP, CDAP, CMP
Line 2. TXB, Y, YD, YDD, FY, CN, AM, LT, YP, YPD, YPDD, FYP, CNP, AMP
Line 3. TYB, Z, ZD, ZDD, FZ, CY, DYPR, TPD, ZP, ZPD, ZPDD, FZP, TYPB, DYPRP
Line 4. TZB, PSIE, PSIDE, PSIDDE, QPSI, CLN, ALPE, OMXBE, PSIE, PSIPDE,
PSPDDE, QPSIP, TZPB, ALPPE
Line 5. GAME, THEE, THEDE, THEDDE, QTHE, CLM, PHIE, OMYBE, THEPE,
THEPDE, THPDDE, QTHER, TPDXB, GAMPE
Line 6. CHIE, PHIE, PHIDE, PHIDDE, QPHI, CLL, PHIAE, OMZBE, KS, CLLP,
CLMQ, CLNR, TYPDRB, PULAN
Line 7. MPAL, MPAS, DMD, QMAXPB, IXPB, IYPB, SPD, SP, SPRU, SPRL, TINT,
TNINY, TFI, XPBDI

When the simulation reaches HHH or TTT, the computer will write out "RUN ENDED BY CONSTRAINTS". It will then attempt to read in more data cards, to initialize for another simulation, starting with input item "y". If there are no data cards available, the program will CALL EXIT.

SECTION 4 - NUMERICAL SOLUTION

For the most general type rigid body, there are six second order differential equations, coupled in the acceleration terms. These six equations can be written as:

$$\sum_{i=1}^6 D_{ij} \ddot{U}_i = v_j \quad j = 1, 2, \dots, 6 \quad (153)$$

and solved simultaneously using the PIVERT subroutine. PIVERT uses Gauss elimination with complete pivoting to obtain the largest diagonal elements. After solving for the accelerations (\ddot{U}_i in equation (153)), the results are numerically integrated using Runge-Kutta, fourth order techniques⁽³⁾.

If the forebody has the properties that $\bar{X} = \bar{Y} = \bar{Z} = I_{xyb} = I_{xzb} = I_{yzb} = 0.$, the equations of motion greatly simplify for the forebody. In the case of integrating the Euler angles, three equations remain coupled in the acceleration terms, and are separated using PIVERT. The three translational accelerations are already in a suitable form to integrate immediately. A simpler situation occurs if the added masses of the decelerator are neglected. All five equations of motion are uncoupled in the second derivative and are easily integrated by 4th order Runge-Kutta.

SECTION 5 - PLOTTING ROUTINE

If OPLOT = 1., eleven variables are saved in arrays. At the end of the simulation, any or all of these variables are plotted by calling PLTRAJ and setting the appropriate arguments. PLTRAJ was originally written for use on a CALCOMP 563 plotter and 750 tape drive. It has been modified for use at M.S.F.C. where a SC 4020 plotter is the preferred plotter. The original PLTRAJ will plot up to 4 variables versus time on one graph for each call to PLTRAJ. The modified PLTRAJ for the SC 4020 plotter plots only one variable versus time per plot; therefore four plots will be made instead of one for each call to PLTRAJ. Two hundred data points are plotted on each graph per variable.

SECTION 6 - ENGLISH TO METRIC CONVERSION

The computer program operates in either English or Metric units. The program input and output is in English units unless the option parameter, OMETRC, is set equal to 1. If OMETRC = 1, the input and output is in the Metric System. A conversion table from English to Metric is given below for commonly used engineering parameters.

ENGLISH TO METRIC CONVERSION

REFERENCE NASA SP 7012

*EXACT

FORCE	(LB) X 4.4482216152605* = (1) NEWTON	N
LENGTH	(FT) X .30480060 * = (1) METER	m
MASS	(SLUG) X 14.5939029 = (1) KILOGRAM	kg
SPEED	(FT/SEC) X .3048 = (1) METERS SEC	m/sec
PRESSURE	(LB/FT ²) X 47.880258 = (1) NEWTON/METER ²	N/m ²
volume	(FT ³) x .028316846592* = METERS ³	m ³
AREA	(FT ²) X .09290304* = METERS ²	m ²
ACCELERATION	(FT/SEC ²) X .3048* = METER/SEC ²	m/sec ²
INERTIA	(SLUG-FT ²) X 1.355817945= KILOGRAM-METER ²	kg-m ²
TORQUE	(FT-LB) X 1.355817948 = METER - NEWTON	m-N
DENSITY	(SLUG/FT ³) X 515.379 = KILOGRAM/METER ³	kg/m ³
viscosity	(SLUG/FT-SEC) X 47.880258 = NEWTON SEC/METER ²	(N-sec)/m ²
SPRING CONSTANT	(LB/FT) X 14.59390293 = NEWTON/METER	N/m

* Exact Numbers - No round offs

SECTION 7 - CONCLUSIONS AND RECOMMENDATIONS

The following conclusions and recommendations are made for use of the 6+5 D.O.F. computer program.

1. The (6+5) DOF loads assessment computer program should be used primarily to analyze the loads induced on a wobbling or spinning body when the body is stabilized by the deployment of a drogue parachute.
2. After the body has been stabilized by the drogue, further parachute deployments (main chutes) should be analyzed using the planar (3+3) DOF computer program. The (3+3) program should be used because of the following reasons:
 - a. The (3+3) program is faster and easier to use than the (6+5) program.
 - b. Terminal descent with the forebody pitch angle equal to $\pm 90^\circ$ presents no mathematical solution problem using the (3+3) DOF program.
3. It should be noted here that the (6+5) DOF program has a mathematical singularity point at a forebody pitch angle of $\pm 90^\circ$. To permit passage through this point the six forebody accelerations are frozen at their last value when the pitch angle is in the region of $89.8^\circ < \theta < 90.2^\circ$. This induces some error in the translational coordinates and attitude of the forebody, but it has been shown to be small for normal velocity passes through this point. A time count (TNINY) for the time spent in this region is a program output.

CHAPTER IV - PROGRAM LISTING AND SAMPLE COMPUTER RUN

The following program listing is for the Univac 1108 at M.S.F.C. and adapted from the IBM 360 listing used by Goodyear Aerospace Corporation.

The sample problem, SRB Stabilization by 54' Drogue Parachute, represents the deployment of a 54' drogue from a SRB which is wobbling and flying broadside to the wind vector. The trajectory of the SRB is nearly vertical. The drogue is starting to inflate and is stretched out normal to the SRB centerline. The drogue has one stage of reefing (0.82 of full open area).

Some of the more important initial conditions are given in the table below.

Altitude	Ft	19,000.
Velocity	Ft/Sec	553.
Angle of Attack	Deg.	90.
Flight Path Angle	Deg.	- 85.
Body Axis Rates		
Pitch	Deg/Sec	- 1.0
Yaw	Deg/Sec	0.0
Roll	Deg/Sec	0.0

The output from the sample problem starts on Page 57, and selected portions of the trajectory are found starting on page 107.

E-ID-15(7 71)
REF: EOI 38(


```

300 9 WTCM,WTCM,CCRIT,LS,NS,NT,TO,TRO,TH1,TH2,TH3,SPRO,SPK1,SPR2,SPR3
310 A ,PCTO1,PCTO2,PCTO3,POROS,GLOAD,FSULT,ALNATO,FREQP,XPDON,DTI
320 B,SPNU,SPRL,TINT,TINF,TFL,XPD01,TOTRU,TOTRI,TOTR2,TOTR3,OPSP,TNINY
330 1 FORMAT(8F10.0)
340 2 FORMAT(13A6,A2)
350 30 FORMAT(11I,5X,'TIME',5X,'X',8X,'XD',7X,'XUD',6X,'FX',7X,'CA',7X,
360 'V',6X,'TENS',5X,'AP',7X,'XPD',6X,'XPD0',5X,'FXP',6X,'CDAP',5X,
370 '2C4P',/
380 '6X,'TXB',6X,'Y',6X,'YD',7X,'YDD',6X,'FY',7X,'CN',7X,'AM',7X,'LT',
390 '7X,'YP',7X,'YD',6X,'YD0',5X,'FYP',6X,'CNP',6X,'AMP',/
400 '56X,'TYB',6X,'Z',8X,'ZD',7X,'ZDD',6X,'FZ',7X,'CY',7X,'DYPR',5X,
410 '6TPD',6X,'7P',7X,'7PD',6X,'7PD0',5X,'F7P',6X,'7YPB',5X,'DYPM',/
420 '76X,'TZB',6X,'PSIE',5X,'PSIOE',4X,'PSIO0',3X,'OPSI',5X,'CLN',6X,
430 '8ALPE',5X,'OMXBE',4X,'PSIPE',4X,'PSIPE',3X,'SPODE',3X,'WPSIP',
440 '9X,'TZPB',5X,'ALPPE',/
450 'ASX',6X,'GAME',5X,'THEE',5X,'THEDE',4X,'THEDE',3X,'OTHE',5X,'CLM',6X,
460 'D'PHIE',4X,'OMYBE',4X,'THEPE',4X,'THEPE',3X,'IMPDE',3X,'QTHEP',
470 'CX',6X,'TPDXB',4X,'GAME',/
480 'DAX',6X,'CHIE',5X,'PHIE',5X,'PHIOE',4X,'PHIOE',3X,'OPHI',5X,'CLL',6X,
490 'E'PHIAE',4X,'OMZBE',4X,'KS',7X,'CLLP',5X,'CLMQ',5X,'CLNR',
500 'F 5X,'TPORB',4X,'PULAN',6X,'MPAL',5X,'MPAS',5X,'DMD',6X,'QMAAPB',
510 'G 3X,'IXPB',5X,'IYPB',5X,'SPD',6X,'SP',7X,'SPRU',5X,'SPRL',5X,
520 'H 'TINT',4X,'TNINY',5X,'TFL',6X,'XPB01',/
530 51 FORMAT(3X,F9.4,F9.0,2F9.3,F9.0,F9.3,F9.2,2F9.0,2F9.2,F9.0,F9.3,
540 '1F9.3',/
550 '23X,2F9.0,2F9.3,F9.0,3F9.3,F9.0,2F9.2,F9.0,2F9.3',/
560 '33X,2F9.0,2F9.3,F9.0,F9.3,F9.2,2F9.0,2F9.2,2F9.0,F9.2',/
570 '43X,F9.0,3F9.3,F9.0,F9.3,2F9.0,F9.3',/
580 '53X,4F9.3,F9.0,6F9.3,F9.0,F9.0,F9.3',/
590 '6 3X,4F9.3,F9.0,3F9.3,F9.0,3F9.3,2F9.0',/
600 '7 3X,2F9.1,F9.2,4F9.1,3F9.2,3F9.5,F9.2',/
610
620 C ALPHI IS THE NO. OF ELEMENTS IN PPHIE ARRAY (2. TO 8.)
630 C ALPHID IS THE NO. OF ELEMENTS IN PPHIDE ARRAY (2. TO 8.)
640 C AJALPF IS THE NO. OF ELEMENTS IN AALPFE ARRAY (8. OR 16.)
650 C AJALPM IS THE NO. OF ELEMENTS IN AALPME ARRAY (8. OR 16.)
660 C AKAM IS THE NO. OF ELEMENTS IN THE AAM ARRAY (2. TO 8.)
670 C AKAMD IS THE NO. OF ELEMENTS IN THE AAMD ARRAY (2. TO 8.)
680 C OPSYM EQUAL 1. IF BODY IS SYMMETRIC SUCH THAT CY=CLL=CLN=0.
690 C OPSYM EQUAL 0. IF BODY IS NOT SYMMETRIC
700 C
710 C OPDA EQUAL 1. TO READ AMPING COEFFICIENTS AS A FUNCTION OF
720 C ROLL ANGLE, ANGLE-OF-ATTACK, AND MACH NUMBER
730 C OPDA EQUAL 0. TO READ AMPING COEFFICIENTS AS CONSTANTS
740 C
750 C CALL PHARGI(46,'4','2')
760 C IIN = 5
770 C IOUT = 6
780 C IUSED = 0
790 C READ(IIN,1) ALPHI,ALPHID,AJALPF,AJALPM,AKAM,AKAM,OPSYM,OPDA
800 C IPHI=ALPHI
810 C IPHID=ALPHID
820 C JALPF=AJALPF
830 C JALPM=AJALPM
840 C AJALPM=0.
850

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-59-

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C
00446 1400
00457 1410
00465 1420
00477 1430
00510 1440
00522 1450
00532 1460
00541 1470
00552 1480
00563 1490
00575 1500
*DIAGNOSTIC* THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
00603
00603 1510 IF(OPSP.EQ.O) GO TO 91
00605 1520 READ(IIN,1)TRC,TRI,TR2,TR3
00613 1530 READ(IIN,1)SPRO,SPRI,SPR2,SPR3,PCTOI,PCTO2,PCTO3,POROS
00625 1540 DO 64 I=1,16
00630 1550 TTIP(I)=O.O
00631 1560 64 SSP(I)=O.O
00633 1570 CONTINUE
00634 1580 GO TO 92
00635 1590 91 READ(IIN,1) TTIP,SSP
00641 1600 TRO=O.O
00642 1610 TRI=O.O
00643 1620 TR2=O.O
00644 1630 TR3=O.O
00645 1640 SPRO=O.O
00646 1650 SPRI=O.O
00647 1660 SPR2=O.O
00650 1670 SPR3=O.O
00651 1680 PCTOI=O.O
00652 1690 PCTO2=O.O
00653 1700 PCTO3=O.O
00654 1710 POROS=O.O
00655 1720 CONTINUE
*DIAGNOSTIC* THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
00656 1730 IF(OPDT.EQ.O) GO TO 93
00660 1740 READ(IIN,1)GLOAD,FSULT,4ERATO,TO,DTPI,TTT,MHM
00671 1750 GO TO 94
00672 1760 93 READ(IIN,1)DTI,TO,D PI,TTT,MHM
00701 1770 GLOAD=O.O
00702 1780 FSULT=O.O
00703 1790 4ERATO=O.O
00704 1800 CONTINUE
94 READ(IIN,2)COM
N=O
WTP= WTL+ WTC
T = TO
TOTRO= TO+TRC
TOTRI= TO+TRI
TOTR2= TO+TR2
TOTR3= TO+TR3
C
00710 1820
00711 1830
00712 1840
00713 1850
00714 1860
00715 1870
00716 1880
00716 1890
00716 1900
00717 *DIAGNOSTIC* THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
00717 1910 IF(OPDT.EQ.O) GO TO 60
00721 1920 GO TO 63

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00722 1930 60 DTT=.04735*SQR((LS*WTP)/(GLOAD*WTF*SULT*AERATO))
00723 1940 FREQP=1./(12.*DTT)
00724 1950 YY=DTT
00725 1960 I=0
00726 1970 61 NN=YY
00727 1980 IF(NN*GE.1) GO TO 62
00731 1990 I=I+1
00732 2000 YY=YY*10.
00733 2010 GO TO 61
00734 2020 62 DT1=NN/10.*.1
00735 2030 63 CONTINUE
00736 2040 GO=32.*17
00737 2050 RHOO=.002378
00740 2060 RE=.0026435.
00741 2070 *DIAGNOSTIC THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
00743 2080 IF(OMETRC.EQ.1.) GO TO 140
00744 2090 GO TO 141
00745 2100 140 RE=.6378377.
00746 2110 RHOO=.1.22557
00747 2120 GO=.9.8054160
00750 2130 141 DPR=.57.2957795
00751 2140 M=WT/GO
00752 2150 MP=WT/GO
00753 2160 WTCM= WTC/32.17
00754 2170 WTLM= WTL/32.17
00755 2180 LSCLO= SQR((LS*.5*.10176*DP*DP)
00756 2190 AP= (WTC*(.1595*DP+LSCLO)+.5*LSCLO*WTL)/(WTC+WTL)
00757 2200 AX= (ALOG10(AMAX1)-ALOG10(AMAX2))/(ALOG10(DSX1)-ALOG10(DSX2))
00760 2210 BX= AMAX1/(DSX1*AX)
00761 2220 AY= (ALOG10(AMAY1)-ALOG10(AMAY2))/(ALOG10(DSY1)-ALOG10(DSY2))
00762 2230 BY= AMAY1/(DSY1*AY)
00763 2240 PSI=PSIE/DPR
00764 2250 PHI=PHIE/DPK
00765 2260 PSIP=PSIPE/DPR
00766 2270 THEP=THEPE/DPK
00767 2280 OMXB=OMXBE/DPK
00770 2290 OMYB=OMYBE/DPK
00771 2300 O'ZB=OMZBE/DPK
00772 2310 THEPD=THEPOE/DPR
00773 2320 PSIPD=PSIPOE/DPR
00774 2330 GAM=GAME/DPR
00775 2340 CHI=CHIE/DPR
00776 2350 GAMP=GAMPE/DPR
00777 2360 CHIP=CHIPLE/DPR
00780 2370 SGAM=SIGN(GAM)
00781 2380 CGAM=COS(GAM)
00782 2390 SCHI=SIN(CHI)
00783 2400 CCHI=COS(CHI)
00784 2410 SGAMP=SIN(GAMP)
00785 2420 CGAMP=COS(GAMP)
00786 2430 SCHIP=SIN(CHIP)
00787 2440 CCHIP=COS(CHIP)
00788 2450 XD=V*CGAM*CHI
00789 2460 YD=V*CGAM*CHI
00790 2470 ZD=V*SGAM

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01335 3590 DO 41 K=1,KAM
01340 3600 WRITE(10UT,20)
01342 3610 20 FORMAT(//,40X,'CN (NORMAL COEF. ARRAY (IPHI,JALPF,KAM))')
01343 3620 WRITE(10UT,17) AAM(K)
01344 3630 DO 41 I=1,IPHI
01351 3640 41 WRITE(10UT,10) (CCN(I,J,K),J=1,JALPF)
01361 3650 DO 44 K=1,KAM
01364 3660 WRITE(10UT,24)
01366 3670 26 FORMAT(//,40X,'CLM (PITCH MOM. COEF. ARRAY (IPHI,JALPM,KAM))')
01367 3680 WRITE(10UT,17) AAM(K)
01372 3690 DO 44 J=1,IPHI
01375 3700 44 WRITE(10UT,10) (CCLM(I,J,K),J=1,JALPM)
01405 3710 *DIAGNOSTIC*
01405 3710 THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
01405 3710 IF(OPSYM.EQ.1.) GO TO 95
01407 3720 DO 42 K=1,KAM
01412 3730 WRITE(10UT,22)
01414 3740 22 FORMAT(//,40X,'CY (LATERAL COEF. ARRAY (IPHI,JALPF,KAM))')
01415 3750 WRITE(10UT,17) AAM(K)
01420 3760 DO 42 I=1,IPHI
01423 3770 42 WRITE(10UT,10) (CCY(I,J,K),J=1,JALPF)
01433 3780 DO 43 K=1,KAM
01436 3790 WRITE(10UT,24)
01440 3800 24 FORMAT(//,40X,'CLL (ROLL MOM. COEF. ARRAY (IPHI,JALPM,KAM))')
01441 3810 WRITE(10UT,17) AAM(K)
01444 3820 DO 43 I=1,IPHI
01447 3830 43 WRITE(10UT,10) (CCLL(I,J,K),J=1,JALPM)
01457 3840 DO 45 K=1,KAM
01462 3850 WRITE(10UT,28)
01464 3860 25 FORMAT(//,40X,'CLN (YAW MOM. COEF. ARRAY (IPHI,JALPM,KAM))')
01465 3870 WRITE(10UT,17) AAM(K)
01470 3880 DO 45 I=1,IPHI
01473 3890 45 WRITE(10UT,10) (CCLN(I,J,K),J=1,JALPM)
01503 3900 95 CONTINUE
01504 3910 *DIAGNOSTIC*
01504 3910 THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
01506 3920 IF(OPDA.EQ.1.) GO TO 39
01507 3930 GO TO 38
01510 3940 39 CONTINUE
01512 3950 WRITE(10UT,8)
01513 3960 8 FORMAT(1H,10X,'PPHIDE (ROLL ANGLE-DEGREES)')
01521 3970 WRITE(10UT,9)
01523 3980 9 FORMAT(//,10X,'AALPDE (ANGLE OF ATTACK-DEGREES)')
01524 3990 WRITE(10UT,10) (AALPDE(J),J=1,JALPD)
01532 4000 WRITE(10UT,65)
01534 4010 65 FORMAT(//,10X,'AAMD (MACH NUMBER)')
01535 4020 WRITE(10UT,10) (AAMD(K),K=1,KAMD)
01543 4030 DO 47 K=1,KAMD
01544 4040 47 WRITE(10UT,30)
01550 4050 30 FORMAT(//,30X,'CLLF (ROLL DAMPING MOM. COEF. ARRAY (IPHI,JALPD,KAMD))')
01550 4060 WRITE(10UT,17) AAMD(K)
01551 4070 DO 47 I=1,IPHID
01554 4080 47 WRITE(10UT,34) (CCLLP(I,J,K),J=1,JALPD)
01557 4090 34 FORMAT(1X,8F15.3/)
01567 4100 DO 48 K=1,KAMD
01570 4110 48 WRITE(10UT,33)
01573 4120

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01575 4130
01576 4140
01577 4150
01601 4160
01604 4170
01614 4180
01617 4190
01621 4200
01621 4210
01622 4220
01625 4230
01630 4240
01640 4250
01642 4260
01643 4270
01652 4280
01652 4290
01652 4300
01652 4310
01652 4320
01653 4330
01654 4340
01656 4350
01660 4360
01662 4370
01664 4380
01665 4390
01667 4400
01670 4410
01671 4420
01673 4430
01675 4440
01675 4450
01675 4460
01675 4470
01676 4480
01677 4490
01700 4500
01701 4510
01702 4520
01703 4530
01704 4540
01705 4550
01706 4560
01707 4570
01710 4580
01711 4590
01712 4600
01713 4610
01714 4620
01715 4630
01716 4640
01717 4650
01720 4660
01721 4670
01722 4680

33 FORMAT(///,30X,CLHQ (PITCH DAMPING MOM. COEF. ARRAY(IPHID,JALPD,K
1AMD))//)
WRITE(IOUT,17) AAMD(K)
DO 48 I=1,IPHID
48 WRITE(IOUT,34)(CCLHQ(I,J,K),J=1,JALPD)
DO 49 K=1,KAMJ
WRITE(IOUT,32)
32 FORMAT(///,30X,CLNR (YAW DAMPING MOM. COEF. ARRAY(IPH,JALPD,KAMJ
1))//)
WRITE(IOUT,17) AAMD(K)
DO 49 I=1,IPHID
49 WRITE(IOUT,34)(CCLNR(I,J,K),J=1,JALPD)
38 WRITE(IOUT,66)
66 FORMAT(///,30X,AE DYNAMICS OF PARACHUTE'///)
WRITE(IOUT,67) AALPE,AAMP,CCAP,CCNP,CCMP
67 FORMAT(20X,'ANGLE OF ATTACK ARRAY (AALPE(8))',10X,8F10.3///,
A20X,'MACH NUMBER ARRAY(AAMP(8))',10X,8F10.3///,
120X,'AXIAL COEFF. ARRAY (CCAP(8,8))',8(10X,8F10.3)///,
220X,'NORMAL COEFF. ARRAY (CCNP(8,8))',8(10X,8F10.3)///,
320X,'PITCH MOM. COEFF. ARRAY (CCMP(8,8))',8(10X,8F10.3)///)
46 CONTINUE
WRITE(IOUT,50)
100 IF(2.0-T.HMM) CONSTR=0.
IF(T.GT.TTY) CONSTR=0.
IF(JJ.EQ.1) GO TO 101
DTPC=DTPC+1.
IF (DTPC.LT.DTP) GO 0 110
JJ=JJ+1
DTPC=0.
IF(JJJ.LE.6) GO TO 101
WRITE(IOUT,50)
JJJ=1
C CALCULATE AND WRITE OUTPUT
C
C 101 CALL SUBR
PSIE=PSI+DPR
THEE=THE+DPR
PHI=PHI+DPR
PSIPE=PSIPE+DPR
THEPE=THEPE+DPR
PSIDE=PSIDE+DPR
THEDE=THEDE+DPR
PHIDE=PHIDE+DPR
PSIPDE=PSIPDE+DPR
THEPDE=THEPDE+DPR
PSIDDE=EE(1)+DPR
THEDDE=EE(2)+DPR
PHIDDE=EE(3)+DPR
XDD=EE(4)
YDD=EE(5)
ZDD=EE(6)
PSPDDE=FF(1)+DPR
THPDDE=FF(2)+DPR
XPD=FF(3)
YPD=FF(4)

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01723 469 ZPDD=FF(5)
01724 470 CHIE=ATAN2(SNGL(YD), NGL(XD))*OPR
01725 471 GAM=ATAN2(SNGL(ZD), SQRT(SNGL(XD**2+YD**2)))
01726 472 IF(XD.LT.O.) GAM=3.14159265-GAM
01730 473 GAMP=ATAN2(SNGL(ZPD), SQRT(SNGL(XPD**2+YPD**2)))
01731 474 IF(XPD.LT.O.) GAMP=3.14159265-GAMP
01733 475 GAME=GAM*OPR
01734 476 ALPPE=ALPP*OPR
01735 477 GAMPE=GAMP*OPR
01736 478 OMXBE=OMXB*OPR
01737 479 OMYBE=OMYB*OPR
01740 480 OMZBE=OMZB*OPR
01741 481 CDAP=CAP*SP
01742 482 VD=SQRT(XDD**2+YDD**2+ZDD**2)
01743 483 VPD=SQRT(XPDD**2+YPDD**2+ZPDD**2)
01744 484 TPDDB=SQRT(TPDYB**2+ TPDZB**2)
01745 485 IF(LT.LT.1) GO TO 3
01747 486 PULAN= ATAN2(TPDB, TPDAB)*OPR
01750 487 GO TO 54
01751 488 53 PULAN= 180.
01752 489 54 CONTINUE
01753 490 WRITE(10UT,51)T,X,XD,XDD,FX,CA,V,TENS,XP,XPD,XPDD,FXP,CDAP,CMP,
01753 491 ITR,Y,YD,YDD,FY,CN,AM,LT,Y,YPD,YPDD,FYP,CNP,AMP,
01753 492 2TYR,Z,ZD,ZDD,FZ,CY,DYPR,TPD,ZP,ZPD,FZP,TYPB,DYPRP,
01753 493 3TYR,PSIE,PSUE,PSIODE,PSI,CLN,ALPE,OMXUE,PSIPE,PSIPDE,PSPDUE,
01753 494 4QPSIP,TZPE,ALPPE,
01753 495 5GAME,THEE,THEDE,THEDEDE,OTHE,CLM,PHIIE,OMYBE,THEPE,THEPDE,TPPDE,
01753 496 6OTHEP,TPDXR,GAMPE,
01753 497 7CHIE,PHIE,PHIDE,OPHI,CLL,PHIAE,OMZBE,KS,CLLP,CLMQ,CLNR
01753 498 8.TPDBR,PULAN,MPAL,MPAS,OMD,QMAXPB,IXPB,IYPB,SPD
01753 499 9. SP,SPRU,SPRL,TINT,TNINY,TFI,XPBDI
01753 500 JJ=2
01753 501 C
01753 502 C SPECIFY VARIABLES FOR LOT TAPE
01753 503 C
01753 504 C THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
01753 505 IF (OPPLOT.EQ.O.) GO TO 110
01753 506 N=H+1
01753 507 XAINI=T
01753 508 Y1(N)=PSIE
01753 509 Y2(N)=THEE
01753 510 Y3(N)=PHIE
01753 511 Y4(N)=ALPE
01753 512 Y5(N)=Z
01753 513 Y6(N)=AM
01753 514 Y7(N)=GAME
01753 515 Y8(N)=DYPR
01753 516 Y9(N)=TPD
01753 517 Y10(N)=ALPPE
01753 518 110 IF (CONSTR)113,111,111
01753 519 111 WRITE(10UT,52)
01753 520 52 FORMAT(15X,'RUN ENDED BY CONSTRAINTS.//)
01753 521 IF (OPPLOT) 99, 99,112
01753 522 112 IF (N.LE.1) GO TO 99
01753 523 IRET = 0
01753 524 GO TO 116

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02153 5240 113 IF (OPLOT)103,103,114
02156 5250 114 IF (N -200)103,115,115
02161 5260 115 IRET = 1
02162 5270 116 IUSED = 1
02163 5280 CALL PLTRAJIXA,Y1,Y2,Y3,Y4,N,10,2,3,4,5,COM)
02164 5290 CALL PLTRAJIXA,Y5,Y6,Y7,Y8,N,10,1,6,7,8,COM)
02165 5300 CALL PLTRAJIXA,Y9,Y10,Y3,Y4,N,10,9,11,0,0,COM)
02166 5310 N = 0
02167 5320 IF (IRET) 99, 99,103
02167 5330 C
02167 5340 C
02167 5350 C
02172 5360 103 ON 74 J=1,N
02175 5370 *DIAGNOSTIC* THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
02175 5370 IF (J.EQ.1.AND.DTPC.EQ.0.) GO TO 77
02177 5380 CALL SUBR
02200 5390 77 ON 75 I=1,6
02203 5400 75 A(I,J)=EE(I)*DT
02205 5410 DO 76 I=1,5
02210 5420 76 B(I,J)=FF(I)*DT
02212 5430 GO TO (71,72,73,74),J
02213 5440 71 PSIPSI+=S*PSID*DT
02214 5450 THE=THE+S*THED*DT
02215 5460 PHI=PHI+S*PHID*DT
02216 5470 X=X+S*XD*DT
02217 5480 Y=Y+S*YD*DT
02220 5490 Z=Z+S*ZD*DT
02221 5500 PSIP=PSIP+S*PSIPD*DT
02222 5510 THEP=THEP+S*THEPD*DT
02223 5520 XP=XP+S*XPD*DT
02224 5530 YP=YP+S*YPD*DT
02225 5540 ZP=ZP+S*ZPD*DT
02226 5550 PSID=PSID+S*AA(1,1)
02227 5560 THED= S*AA(2,1)
02230 5570 PHID= 10+S*AA(3,1)
02231 5580 XD=XD+S*AA(4,1)
02231 5590 YD=YD+S*AA(5,1)
02233 5600 ZD=ZD+S*AA(6,1)
02234 5610 PSIPD=PSIPD+S*BB(1,1)
02235 5620 THEPD=THEPD+S*BB(2,1)
02236 5630 XPD=XPD+S*BB(3,1)
02237 5640 YPD=YPD+S*BB(4,1)
02240 5650 ZPD=ZPD+S*BB(5,1)
02241 5660 T=T+S*DT
02242 5670 GO TO 74
02243 5680 72 FSI=PSI+S*AA(1,1)*DT
02244 5690 THEP=THEP+S*AA(2,1)*DT
02245 5700 PHI=PHI+S*AA(3,1)*DT
02246 5710 X=X+S*AA(4,1)*DT
02247 5720 Y=Y+S*AA(5,1)*DT
02248 5730 Z=Z+S*AA(6,1)*DT
02250 5740 PSIP=PSIP+S*BB(1,1)*DT
02251 5750 THEP=THEP+S*BB(2,1)*DT
02252 5760 XPD=XPD+S*BB(3,1)*DT
02253 5770 YPD=YPD+S*BB(4,1)*DT
02255 5780 ZPD=ZP+S*BB(5,1)*DT

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02256	5790	PSID=PSID+.5*(AA(1,2)-AA(1,1))
02257	5800	THED=THED+.5*(AA(2,2)-AA(2,1))
02260	5810	PHID=PHID+.5*(AA(3,2)-AA(3,1))
02261	5820	XD=XD+.5*(AA(4,2)-AA(4,1))
02262	5830	YD=YD+.5*(AA(5,2)-AA(5,1))
02263	5840	ZD=ZD+.5*(AA(6,2)-AA(6,1))
02264	5850	PSIP=PSIP+.5*(BB(1,2)-BB(1,1))
02265	5860	THEP=THEP+.5*(BB(2,2)-BB(2,1))
02266	5870	XPD=XPD+.5*(BB(3,2)-BB(3,1))
02267	5880	YPD=YPD+.5*(BB(4,2)-BB(4,1))
02270	5890	ZPD=ZPD+.5*(BB(5,2)-BB(5,1))
02271	5900	GO TO 74
02272	5910	PSI=PSI+DT*(.5*PSID+.25*(AA(1,2)-AA(1,1)))
02273	5920	THE=THE+DT*(.5*THEO+.25*(AA(2,2)-AA(2,1)))
02274	5930	PHI=PHI+DT*(.5*PHID+.25*(AA(3,2)-AA(3,1)))
02275	5940	X=X+DT*(.5*XD+.25*(AA(4,2)-AA(4,1)))
02276	5950	Y=Y+DT*(.5*YD+.25*(AA(5,2)-AA(5,1)))
02277	5960	Z=Z+DT*(.5*ZD+.25*(AA(6,2)-AA(6,1)))
02300	5970	PSIP=PSIP+DT*(.5*PSIP+.25*(BB(1,2)-BB(1,1)))
02301	5980	THEP=THEP+DT*(.5*THEP+.25*(BB(2,2)-BB(2,1)))
02302	5990	XP=XP+DT*(.5*XPD+.25*(BB(3,2)-BB(3,1)))
02303	6000	YP=YP+DT*(.5*YPD+.25*(BB(4,2)-BB(4,1)))
02304	6010	ZP=ZP+DT*(.5*ZPD+.25*(BB(5,2)-BB(5,1)))
02305	6020	PSID=PSID-.5*AA(1,2)+AA(1,3)
02306	6030	THEO=THEO-.5*AA(2,2)+AA(2,3)
02307	6040	PHID=PHID-.5*AA(3,2)+AA(3,3)
02310	6050	XD=XD-.5*AA(4,2)+AA(4,3)
02311	6060	YD=YD-.5*AA(5,2)+AA(5,3)
02312	6070	ZD=ZD-.5*AA(6,2)+AA(6,3)
02313	6080	PSIP=PSIP-.5*BB(1,2)+BB(1,3)
02314	6090	THEP=THEP-.5*BB(2,2)+BB(2,3)
02315	6100	XPD=XPD-.5*BB(3,2)+BB(3,3)
02316	6110	YPD=YPD-.5*BB(4,2)+BB(4,3)
02317	6120	ZPD=ZPD-.5*BB(5,2)+BB(5,3)
02320	6130	T=1+.5*DT
02321	6140	74 CONTINUE
02323	6150	PSID=PSID-AA(1,3)
02324	6160	THEO=THEO-AA(2,3)
02325	6170	PHID=PHID-AA(3,3)
02326	6180	XD=XD-AA(4,3)
02327	6190	YD=YD-AA(5,3)
02330	6200	ZD=ZD-AA(6,3)
02331	6210	PSIP=PSIP-BB(1,3)
02332	6220	THEP=THEP-BB(2,3)
02333	6230	XPD=XPD-BB(3,3)
02334	6240	YPD=YPD-BB(4,3)
02335	6250	ZPD=ZPD-BB(5,3)
02336	6260	PSI=PSI-DT*(PSID+.5*AA(1,2))
02337	6270	THE=THE-DT*(THEO+.5*AA(2,2))
02340	6280	PHI=PHI-DT*(PHID+.5*AA(3,2))
02341	6290	X=X-DT*(XD+.5*AA(4,2))
02342	6300	Y=Y-DT*(YD+.5*AA(5,2))
02343	6310	Z=Z-DT*(ZD+.5*AA(6,2))
02344	6320	PSIP=PSIP-DT*(PSIP+.5*BB(1,2))
02345	6330	THEP=THEP-DT*(THEP+.5*BB(2,2))
02346	6340	XP=XP-DT*(XPD+.5*BB(3,2))


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02347 635. V=0-DT*(ZPD+5*BB(4,2))
02350 636. ZP=Z-NT*(ZPD+5*BB(5,2))
02351 637. PS1=PS1-DT*(PS1D+AA(1,1)+AA(1,2)+AA(1,3))/6.)
02352 638. THE=THE-DT*(THED+AA(2,1)+AA(2,2)+AA(2,3))/6.)
02353 639. PH1=PH1-DT*(PH1D+AA(3,1)+AA(3,2)+AA(3,3))/6.)
02354 640. X=X-DT*(XD+AA(4,1)+AA(4,2)+AA(4,3))/6.)
02355 641. Y=Y-DT*(YD+AA(5,1)+AA(5,2)+AA(5,3))/6.)
02356 642. Z=Z-DT*(ZD+AA(6,1)+AA(6,2)+AA(6,3))/6.)
02357 643. PSIP=PSIP-DT*(PSIPD+BB(1,1)+BB(1,2)+BB(1,3))/6.)
02360 644. THEP=THEP-DT*(THEPD+BB(2,1)+BB(2,2)+BB(2,3))/6.)
02361 645. XP=XP-DT*(XPD+BB(3,1)+BB(3,2)+BB(3,3))/6.)
02362 646. YP=YP-DT*(YPD+BB(4,1)+BB(4,2)+BB(4,3))/6.)
02363 647. ZP=ZP-DT*(ZPD+BB(5,1)+BB(5,2)+BB(5,3))/6.)
02364 648. PS1D=PS1D+AA(1,1)+2*AA(1,2)+AA(1,3)+AA(1,4))/5.)
02365 649. THED=THED+AA(2,1)+2*AA(2,2)+AA(2,3)+AA(2,4))/6.)
02366 650. PH1D=PH1D+AA(3,1)+2*AA(3,2)+AA(3,3)+AA(3,4))/6.)
02367 651. XD=XD+AA(4,1)+2*AA(4,2)+AA(4,3)+AA(4,4))/6.)
02370 652. YD=YD+AA(5,1)+2*AA(5,2)+AA(5,3)+AA(5,4))/6.)
02371 653. ZD=ZD+AA(6,1)+2*AA(6,2)+AA(6,3)+AA(6,4))/6.)
02372 654. PS1PD=PS1PD+BB(1,1)+2*BB(1,2)+BB(1,3)+BB(1,4))/6.)
02373 655. THEPD=THEPD+BB(2,1)+2*BB(2,2)+BB(2,3)+BB(2,4))/6.)
02374 656. XPD=XPD+BB(3,1)+2*BB(3,2)+BB(3,3)+BB(3,4))/6.)
02375 657. YPD=YPD+BB(4,1)+2*BB(4,2)+BB(4,3)+BB(4,4))/6.)
02376 658. ZPD=ZPD+BB(5,1)+2*BB(5,2)+BB(5,3)+BB(5,4))/6.)
02377 659. IF(1-ABS(SIN(SNGLT(1)))>.5) DT=DT/5.
02401 660. IF(1-ABS(SIN(SNGLT(1)))>.5) DT=DT/5.
02402 661. GO TO 100
02403 662. 1000 CONTINUE
02404 663. IF(1-ABS(SIN(SNGLT(1)))>.5) GO TO 1010
02405 664. C END ALL PLOTTING BEFORE EXIT
02407 665. CALL ENDJOB
02410 666. 1010 STOP
02411 667. END

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END OF COMPILATION: 18 DIAGNOSTICS.

OFOR,US SUBR
MSD 11A -03/27/74-00119:12 (0.1)

SUBROUTINE SUBR ENTRY POINT 006176

STORAGE USED: CODE(1) 0062101 DATA(0) 0005761 BLANK COMMON(2) 020174

EXTERNAL REFERENCES (BLOCK, NAME)

0003 DENS
0004 DENS4
0005 INTERP
0006 PIVERT
0007 SIN
0010 COS
0011 SQRT
0012 ATAN2
0013 NPOUS
0014 NIO2S
0015 NSTOPS
0016 XPRR
0017 NERR38

STORAGE ASSIGNMENT IBLOCK, TYPE, RELATIVE LOCATION, NAME)

0001	000346	10L	000563	100L	0001	000575	101L	0001	001547	102L	0001	000631	103L	
0001	001551	104L	000354	11L	0001	001440	110L	0001	001652	111L	0001	000547	114L	
0001	000555	15L	000630	151L	0001	001411	160L	0001	001047	161L	0001	001105	162L	
0001	001143	163L	001156	190L	0001	001333	171L	0001	001421	174L	0001	001361	195L	
0000	000354	196F	001376	197L	0001	001414	198L	0001	001431	200L	0001	001663	210L	
0001	001675	211L	002015	214L	0001	002226	215L	0001	003306	31L	0001	001373	300L	
0001	002405	301L	003310	31L	0001	001162	40L	0001	00250	400L	0001	001362	401L	
0001	005311	41L	005431	42L	0001	00130	43L	0001	000627	50L	0001	004042	500L	
0001	002054	501L	002376	51F	0000	000411	52F	0001	002065	600L	0001	002077	601L	
0001	003207	61L	003221	62L	0001	003242	66L	0001	003162	665G	0001	003254	67L	
0001	003203	676G	002110	700L	0001	002222	71L	0001	000637	80L	0001	002325	800L	
0001	002337	801L	002675	81L	0001	000707	82L	0001	000721	84L	0001	004133	900L	
0001	002145	901L	002471	94L	0001	003243	97L	0001	002313	98L	0001	002316	99L	
0002	R 000155	A	0002	R 000334	AALPDE	0002	R 000244	AALPPE	0002	R 000264	AALPPE	0002	R 017746	AALPPE
0002	R 000324	AAM	0002	R 000334	AAND	0002	R 017360	AAMP	0000	R 000277	ABAND	0000	R 000302	ABAND
0002	020154	AERATO	0002	R 000177	ALPE	0000	R 000261	ALPFSL	0000	R 000106	ALPP	0002	R 000106	ALPP
0000	R 000231	ALPPE	0000	R 000252	ALPPSL	0000	R 000266	ALPFSL	0002	R 000166	AM	0002	R 017763	ANAKI
0002	017764	AMAX2	0002	017767	AMAY1	0002	017771	AMAY2	0002	R 000167	AMP	0000	R 000250	AMPSL
0000	R 000260	AMSL	0002	R 000160	AP	0002	R 017773	AX	0002	R 017775	AY	0002	R 000126	B
0000	R 000100	BBAR	0000	R 000303	BBARD	0002	R 017774	BA	0002	R 017776	BY	0002	R 000187	C
0002	R 000107	CA	0002	R 000115	CAP	0000	R 000303	CBAR	0000	R 000304	CRAND	0002	R 000233	CC
0002	R 000344	CCA	0002	R 017370	CCAP	0002	R 013344	CCLL	0002	R 014344	CCLLP	0002	R 000344	CCLM
0002	R 015344	CCLMQ	0002	R 012344	CCLN	0002	R 016344	CCLNR	0002	R 017570	CCMP	0002	R 000234	CCN
0002	R 017470	CCMP	0002	R 017670	CCP	0002	R 020131	CCRT	0002	R 004344	CCY	0000	R 000265	CF
0002	R 000114	CLL	0002	R 000122	CLLP	0002	R 000112	CLM	0002	R 000120	CLMW	0002	R 000113	CLN
0002	R 000121	CLNR	0002	R 000117	CMF	0002	R 000110	CM	0002	R 000116	CNP	0000	R 000162	CPM1
0000	R 000270	CPM11	0000	R 000253	CPM1P1	0000	R 000171	CPM12	0000	R 000160	CPS1	0000	R 000163	CPS1P

[illegible]

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00222 1040 XPRD=XPD*CCP(1,1)+YPD*CCP(1,2)+ZPD*CCP(1,3)
00223 1050 YPD=XPD*CCP(2,1)+YPD*CCP(2,2)
00224 1060 ZPD=XPD*CCP(3,1)+YPD*CCP(3,2)+ZPD*CCP(3,3)
00225 1070 VXPB=SQRT(YPD**2+ZPD**2)
00226 1080 ALPP=ATAN2(VXPB,XPD)
00227 1090 ALPE = ALPP-DPR
00230 1100 IF (VXPB) 13,13,14
00233 1110 13 PHIPI = 0.
00234 1120 GO TO 15
00235 1130 14 PHIPI = ATAN2(-YPD,-ZPD)
00236 1140 15 CONTINUE
00237 1150 C
00238 1160 *DIAGNOSTIC* THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
00239 1170 IF(OPSP.EQ.0) GO TO 103
00240 1180 C
00241 1190 1=2
00242 1200 100 IF(Y.LE.YTIP(1)) GO 0 101
00243 1210 1=1+1
00244 1220 GO TO 100
00245 1230 101 TSL=(Y-TTIP(1-1))/(TTIP(1)-TTIP(1-1))
00246 1240 SP=SSP(1-1)+(SSP(1)-SSP(1-1))*TSL
00247 1250 SPD= (SSP(1)-SSP(1-1))/(TTIP(1)-TTIP(1-1))
00248 1260 XPRD=XPD
00249 1270 IF(SPD.LY.0.0) GO TO 50
00250 1280 GO TO 151
00251 1290 50 XPRD= 0.0
00252 1300 151 CONTINUE
00253 1310 GO TO 200
00254 1320 103 CONTINUE
00255 1330 IF(1.GT.TOTR0) GO TO 80
00256 1340 GO TO 84
00257 1350 80 IF(1.GT.TINT.AND.1.LT.TINF) GO TO 81
00258 1360 *DIAGNOSTIC* THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
00259 1370 IF(1.GT.TINF) GO TO 84
00260 1380 IF(1.GE.TINF.AND.1.LT.TOIR) GO TO 82
00261 1390 81 IF(1/DT1.LE.2.) DT= DT/2.
00262 1400 GO TO 84
00263 1410 82 IF(1/DT1/DT1.LE.2.) DT= DT/2.
00264 1420 GO TO 84
00265 1430 84 CONTINUE
00266 1440 IF(1.LE.TOTR3.AND.1.GE.TO) GO TO 160
00267 1450 IF(1.LE.TOTR1.AND.1.GT.TOTR0) GO TO 161
00268 1460 IF(1.LE.TOTR2.AND.1.GT.TOTR1) GO TO 162
00269 1470 IF(1.LE.TOTR3.AND.1.GT.TOTR2) GO TO 163
00270 1480 160 SP=SPR0
00271 1490 SPD= 0.0
00272 1500 TINT= 0.0
00273 1510 TINF= 0.0
00274 1520 PCTOI= 0.0
00275 1530 XPRD1= 0.0
00276 1540 TFI= 0.0
00277 1550 SPRL= 0.0
00278 1560 SPRU= 0.0
00279 1570 IF(1.LE.TOTR0.AND.1.GT.(TOTR0-DT)) XPRD1=XPRD
00280 1580 GO TO 200
00281 1590 161 TINT = TOTR0
00282 1600

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00324      SPRL = SPRL
00327      SPRL = SPRL
00330      PCTOI = PCTOI
00331      TRU = TOTRI
00332      IF (T.LE.TOTRI.AND.T.GT.(TOTRI-OT)) XPBDI=XPBD
00334      GO TO 190
00335      TINT = TOTRI
00336      SPRL = SPRL
00337      SPRL = SPRL
00340      PCTOI = PCTOI
00341      TRU = TOTRI
00342      IF (T.LE.TOTRI.AND.T.GT.(TOTRI-OT)) XPBDI=XPBD
00344      GO TO 190
00345      TINT = TOTRI
00346      SPRL = SPRL
00347      SPRL = SPRL
00350      PCTOI = PCTOI
00351      TRU = TOTRI
00352      GO TO 190
00353      SPRL = SPRL
00354      TINT = TINT
00355      TINT = TINT
00356      TINT = TINT
00357      TINT = TINT
00358      TINT = TINT
00359      TINT = TINT
00360      TINT = TINT
00361      TINT = TINT
00362      TINT = TINT
00363      TINT = TINT
00364      TINT = TINT
00365      TINT = TINT
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00420      TINT = TINT
00421      TINT = TINT
00422      TINT = TINT
00423      TINT = TINT

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00424 2130 194 WRITE(3,194) TRU
00427 2140 STOP
00430 2150 CONTINUE
00431 2160 IF(1-ABS(STHE))<.LT.EPS1) TMINY=TMINY-DT
00433 2170 DS= SURT(1,2732405P)
00434 2180 DSP= .6380DS
00435 2190 LSCL= SORT(1,LS=.250DSP*DSP)
00436 2200 CS1GP= LSCL/LS
00437 2210 RH000= RH0/RH00
00440 2220 MPAL= RH000*BX*DS*AX
00441 2230 MPAS= RH000*BY*DS*AY
00442 2240 DMD= RH000*AX*BX*SPD*(1./SQRT(3.14159*SP))*.DS*(AX-1)
00443 2250 QMAXPB= DMD*XPBDR
00444 2260 *DIAGNOSTIC THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
00446 2270 IF(OPAM*EQ.O.C) GO TO 102
00447 2280 GO TO 104
00450 2290 102 MPAL= 0.0
00451 2300 MPAS= 0.0
00452 2310 MPL=MPAL*MP
00453 2320 MPS=MPAS*MP
00454 2330 MLMHSP=MPL-MPS
00455 2340 ICY0= .104167*WTCHD P*OSP
00456 2350 ICX0= .625*ICYO
00457 2360 ILY0= WTL*ICX0*.C8333*LS*LS*.03125*DSP*DSP)
00460 2370 ILX0= .125*WTL*DSP*DSP
00461 2380 IVPB= ICY0+ILY0+WTL*MP*(AP*.5*LS*CS1GP)*.2*(MPAS*WTCHM)*
00462 2390 I (.25*DSP*LS*CS1GP*AP)*.2
00463 2400 IXPB= ICX0+ILX0
00464 2410 IXYPB=IXPB*IVPB
00465 2420 I=2
00467 2430 110 IF(AMP*LE.AAMP(1)) GO TO 111
00470 2440 I=I+1
00471 2450 GO TO 110
00472 2460 111 AMPSL=(AMP-AAMP(I-1))/(AAMP(I)-AAMP(I-1))
00473 2470 J=2
00475 2480 210 IF(ALPPE*LE.AALPPE(J)) GO TO 211
00476 2490 J=J+1
00477 2500 GO TO 210
00478 2510 211 ALPPSL= (ALPPE-AALPPE(J-1))/(AALPPE(J)-AALPPE(J-1))
00480 2520 CAP=(CCAP(I,J-1)-CCAP(I-1,J-1))/(AMP*SL+CCAP(I-1,J-1))*(CCAP(I,J)-
00481 2530 ICCAP(I-1,J))/(AMP*SL+CAP(I-1,J-1))*(CCAP(I,J-1)-CCAP(I-1,J-1))/(AMP*SL+
00482 2540 2CCAP(I-1,J-1))/(ALPPSL
00483 2550 CNP=(CCNP(I,J-1)-CCNP(I-1,J-1))/(AMP*SL+CCNP(I-1,J-1))*(CCNP(I,J)-
00484 2560 ICCNP(I-1,J))/(AMP*SL+CCNP(I-1,J-1))*(CCNP(I,J-1)-CCNP(I-1,J-1))/(AMP*SL+
00485 2570 2CCNP(I-1,J-1))/(ALPPSL
00486 2580 CMP=(CCMP(I,J-1)-CCMP(I-1,J-1))/(AMP*SL+CCMP(I-1,J-1))*(CCMP(I,J)-
00487 2590 ICCMP(I-1,J))/(AMP*SL+CCMP(I-1,J-1))*(CCMP(I,J-1)-CCMP(I-1,J-1))/(AMP*SL+
00488 2600 2CCMP(I-1,J-1))/(ALPPSL
00489 2610 CMP= CMP*(CNP*AP/DP)
00490 2620 CPHI=COS(PHI)
00491 2630 SPHI=SIN(PHI)
00492 2640 VPRB=SGRT(YB0**2+ZB0**2)
00493 2650 ALPE=ATAN2(VPRB,XB0)*OPR
00494 2660 IF (VPRB) 213,213,214
00495 2670 213 PHI= 0.

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00514 2680 GO TO 215
00515 2690 214 PH11 = ATAN2(-Y80,-Z80)
00516 2700 215 CONTINUE
00517 2710 PH11=PH11+DPR
00520 2720 PH1AE=PH11E
00521 2730 IF(PH11E.LT.0.) PH1AE=-PH11E
00521 2740
00521 2750 THE ABOVE STATEMENT SHOULD BECOME A COMMENT CARD IF THERE IS NO
00521 2760 AERODYNAMIC PLANE OF SYMMETRY
00521 2770
00521 2780 AERODYNAMICS
00521 2790
00523 2800 K=2
00524 2810 500 IF(AM.LE.AAM(K)) GO TO 501
00526 2820 K=K+1
00527 2830 GO TO 500
00530 2840 501 AMSL=(AM-AAM(K-1))/(AAM(K)-AAM(K-1))
00531 2850 J=2
00532 2860 600 IF(ALPE.LE.AALPFE(J)) GO TO 601
00534 2870 J=J+1
00535 2880 GO TO 600
00536 2890 601 ALPFSL=(ALPE-AALPFE(J-1))/(AALPFE(J)-AALPFE(J-1))
00537 2900 I=2
00540 2910 700 IF(PH1AE.LE.PPH1E(I)) GO TO 701
00542 2920 I=I+1
00543 2930 GO TO 700
00544 2940 701 PH1SL=(P11AE-PPH1E(I-1))/(PPH1E(I)-PPH1E(I-1))
00545 2950 JJ=2
00546 2960 900 IF(ALPE.LE.AALPME(JJ)) GO TO 901
00550 2970 JJ=JJ+1
00551 2980 GO TO 900
00552 2990 901 ALPMSL=(ALPE-AALPME(JJ-1))/(AALPME(JJ)-AALPME(JJ-1))
00552 3000
00552 3010 THE FIFTH, SIXTH, AND SEVENTH ARGUMENTS OF SUBROUTINE 'INTERP'
00552 3020 C MUST AGREE WITH THE DIMENSIONS OF THE FIRST ARGUMENT
00552 3030 C
00553 3040 CALL INTERP(CCA,AMSL,ALPFSL,PH1SL,8,16,8,1,J,K,CF)
00554 3050 CA=CF
00555 3060 CALL INTERP(CCN,AMSL,ALPFSL,PH1SL,8,16,8,1,J,K,CF)
00556 3070 CN=CF
00557 3080 CALL INTERP(CCLM,AMSL,ALPMSL,PH1SL,8,16,8,1,JJ,K,CF)
00560 3090 CLM=CF
00561 3100 THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
00561 3100 IF(OPSYN.EQ.1.) GO TO 98
00563 3110 CALL INTERP(CCY,AMSL,ALPFSL,PH1SL,8,16,8,1,J,K,CF)
00564 3120 CY=CF
00565 3130 CALL INTERP(CCLL,AMSL,ALPMSL,PH1SL,8,16,8,1,JJ,K,CF)
00566 3140 CLL=CF
00567 3150 CALL INTERP(CCLN,AMSL,ALPMSL,PH1SL,8,16,8,1,JJ,K,CF)
00570 3160 CLN=CF
00571 3170 GO TO 99
00572 3180 98 CY=0.
00573 3190 CLL=0.
00574 3200 CLN=0.
00575 3210 99 CONTINUE
00576 3220 THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.

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00576 3220 IF(OPDA,EG,1.) GO TO 97
00600 3230 GO TO 96
00601 3240 97 J=2
00602 3250 800 IF(ALPE,LE,AALPOE(J)) GO TO 801
00604 3260 J=J+1
00605 3270 GO TO 800
00606 3280 801 ALPSL=(ALPE-AALPOE(J-1))/(AALPOE(J)-AALPOE(J-1))
00607 3290 K=2
00610 3300 900 IF(AM,LE,AAMD(K)) GO TO 901
00612 3310 K=K+1
00613 3320 GO TO 400
00614 3330 901 AMSL=(AM-AAMD(K-1))/(AAMD(K)-AAMD(K-1))
00615 3340 I=2
00616 3350 300 IF(PHIAE,LE,PPHIDE(I)) GO TO 301
00620 3360 I=I+1
00621 3370 GO TO 300
00622 3380 301 PHISL=(PHIAE-PPHIDE(I))/(PPHIDE(I)-PPHIDE(I-1))
00623 3390 CALL INTERP(CCLP,AMSL,ALPSL,PHISL,0,0,0,1,J,K,CF)
00624 3400 CCLP=CF
00625 3410 CALL INTERP(CCLM,AMSL,ALPSL,PHISL,0,0,0,1,J,K,CF)
00626 3420 CLM=CF
00627 3430 CALL INTERP(CCLNR,AMSL,ALPSL,PHISL,0,0,0,1,J,K,CF)
00630 3440 CLNR=CF
00631 3450 96 SPHII=SIN(PHII)
00632 3460 CPHII=COS(PHII)
00633 3470
00632 3480 C CALCULATE GENERALIZED FORCES
00632 3490 C
00633 3500 FXB=-OYPR*CA
00634 3510 FYB=OYPR*S*(CNSP*PHII-CY*CPHII)
00635 3520 FZB=OYPR*S*(CNS*CPHII+CY*SPHII)
00636 3530 OMB=PHID-PSID*CC(1,3)
00637 3540 OMYB=THED*CPHII-PSID*CC(2,3)
00640 3550 OMZB=THED*SPHII-PSID*CC(3,3)
00641 3560 TXB=OYPR*S*D*(CLL+CCLP*OMB*D/(2.*V))
00642 3570 TYB=OYPR*S*D*(CLM*CPHII-CLN*SPHII+CLM*OMB*D/(2.*V))
00643 3580 TZB=OYPR*S*D*(CLN*SPHII-CLM*CPHII+CLN*OMB*D/(2.*V))
00644 3590 FXPB=-OYPR*SP*CAP- MAXPB
00645 3600 FYPB=OYPR*SP*CPN*SPHII
00646 3610 FZPB=OYPR*SP*CPN*CPHII
00647 3620 TYPB=OYPR*SP*DP*(CMP-1)*THEPD*DP/VP1*CPHII
00650 3630 TZPB=OYPR*SP*DP*(CMP-1)*THEPD*DP/VP1*SPHII
00651 3640 ABARXP=AP*CCP(1,1)-X*ACC(1,1)-B*CC(2,1)-C*CC(3,1)
00652 3650 BBARYP=AP*CCP(1,2)-Y*ACC(1,2)-B*CC(2,2)-C*CC(3,2)
00653 3660 CBARZP=AP*CCP(1,3)-Z*ACC(1,3)-B*CC(2,3)-C*CC(3,3)
00654 3670 ABARDXP=AP*PSID*CCP(1,2)+THEPD*CCP(3,1)-XD*A*(PSID*
00654 3680 ICC(1,2)-THED*CC(2,2)-B*(PSID*CC(2,2)+PHID*CC(3,1)-THED*CC(2,3)
00654 3690 2-C*(PSID*CC(3,2)-PHID*CC(2,1)-THED*CC(2,3))
00655 3700 BBARDYP=AP*PSID*CCP(1,1)-THEPD*CCP(3,2))-YD*A*(PSID*
00655 3710 ICC(1,1)-THED*CC(2,2)-B*(PSID*CC(2,1)+PHID*CC(3,2)+THED*CC(2,3)
00655 3720 2-C*(PSID*CC(3,1)-PHID*CC(2,1)+THED*CC(2,3))
00656 3730 CBARDZP=AP*THEPD*CTHEP-ZD*A*THEPD*CTHEP-B*(THEPD*CC(2,3)+
00656 3740 ICC(3,3))+C*(THEPD*CC(2,3)+PHID*CC(2,3))
00657 3750 LT=SQRT(ABAR**2+BBAR**2+CBAR**2)
00660 3760 LTD=(ANAR*ABARD+BBAR*BBARD+CBAR*CBARD)/LT
00661 3770 DLT=LT-LTO

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00642 3780 IFILT,LT,LTO) 60 TO 0
00642 3790 C SPRING CONSTANT AS A FUNCTION OF ELONGATION
00642 3800 C
00642 3810 C
00644 3820 DO 40 I=1,8
00646 3830 PSX(I)=PS(I)*NS*CSIGP
00647 3840 PTX(I)=PT(I)*NT
00647 3850 DELSX(I)=EPL(I)*LS*CSIGP
00647 3860 DELTX(I)=EPT(I)*LTO
00647 3870 60 CONTINUE
00647 3880 DO 45 I=1,8
00647 3890 PX(I)=PSX(I)
00647 3900 J=2
00647 3910 41 IF(PX(I).LE.PTX(J)) 60 TO 42
00647 3920 J=J+1
00647 3930 60 TO 41
00647 3940 62 PTXSL= (PX(I)-PTX(J-1))/(PTX(J)-PTX(J-1))
00647 3950 DLTJ= DELTX(J-1)/(DELTX(J)-DELTX(J-1))-PTXSL
00647 3960 DLX(I)= DELSX(I)+ DLTJ
00647 3970 65 CONTINUE
00647 3980 I=2
00647 3990 66 IF(DLT,LE.DLX(I)) 60 TO 47
00647 4000 I=I+1
00647 4010 60 TO 46
00647 4020 47 DLXSL= (DLT-DLX(I-1))/(DLX(I)-DLX(I-1))
00647 4030 TENS= PX(I-1)*(PX(I)-PX(I-1))*DLXSL
00647 4040 KS= TENS/DLT
00647 4050 CS= 2.*CCRT*SQRT(KS*MPL)
00647 4060 DAMP=CS*LT
00647 4070 60 TO 31
00647 4080 30 TENS=0.
00647 4090 DAMP=0.
00647 4100 31 FX=FXB*CC(1,1)+FYB*CC(2,1)+FZB*CC(3,1)
00647 4110 FY=FYB*CC(1,2)+FYB*CC(2,2)+FZB*CC(3,2)
00647 4120 FZ=FZB*CC(1,3)+FYB*CC(2,3)+FZB*CC(3,3)-M*G
00647 4130 FXP=FXB*CCP(1,1)+FYPB*CCP(2,1)+FZPB*CCP(3,1)
00647 4140 FYP=FXB*CCP(1,2)+FYPB*CCP(2,2)+FZPB*CCP(3,2)
00647 4150 FZP=FXB*CCP(1,3)+FYPB*CCP(2,3)+FZPB*CCP(3,3)-M*G
00647 4160 QPSI=1+TXB*CC(1,3)+TYB*CC(2,3)+TZB*CC(3,3)
00647 4170 QTHE=TYB. PHI+TZB*SPH
00647 4180 QPHI=TXB
00647 4190 QPSIP=TZPR*CCP(3,3)
00647 4200 QTHEP=TYPB
00647 4210 OADPSI=-A*CC(1,2)-B*CC(2,2)-C*CC(3,2)
00647 4220 DADTHE=A*CI52+B*CI253+C*CI2C3
00647 4230 DADPHI=-B*CC(3,1)+C*CC(2,1)
00647 4240 DADSP=AP*CCP(1,2)
00647 4250 DADTHP=AP*CCP(3,1)
00647 4260 OBDPSI=A*CC(1,1)+B*CC(2,1)+C*CC(3,1)
00647 4270 OBDTHE=-A*S152-B*S1C253-C*S1C2C3
00647 4280 OBDPHI=-B*CC(3,2)+C*CC(2,2)
00647 4290 OBDSP=AP*CCP(1,1)
00647 4300 OBDTHP=AP*CCP(3,2)
00647 4310 OBDTHE=-A*CTHE+B*S253+C*S2C3
00647 4320 OBDPHI=-B*CC(3,3)+C*CC(2,3)
00647 4330 OBDTHP=AP*CCP(3,3)

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00760 4340 TPDS=TPD+DAMP
00761 4350 TPDX=TPD+ABAR/LT
00762 4360 TPDY=TPD+BBAR/LT
00763 4370 TPZ=TPD+CBAR/LT
00764 4380 TPDX=TPDX+CC(1,1)+TPDY+CC(1,2)+TPDZ+CC(1,3)
00765 4390 TPDY=TPDX+CC(1,1)+TPDY+CC(2,2)+TPDZ+CC(2,3)
00766 4400 TPZB=TPDX+CC(1,1)+TPDY+CC(3,2)+TPDZ+CC(3,3)
00767 4410 IF(POS.EQ.1.) GO TO 40
00767 4420 C
00767 4430 C
00767 4440 C
00771 4450
00773 4460
00774 4470
00775 4480
00776 4490
00777 4500
01000 4510
01001 4520
01002 4530
01003 4540
01004 4550
01004 4560
01004 4570
01005 4580
01005 4590
01005 4600
01006 4610
01006 4620
01006 4630
01007 4640
01010 4650
01012 4660
01015 4670
01016 4680
01017 4690
01020 4700
01021 4710
01022 4720
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01026 4780
01026 4790
01027 4800
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01034 4850
01035 4860
01036 4870
01037 4880

DIAGNOSTIC THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
IF(POS.EQ.1.) GO TO 40

EQUATIONS OF MOTION FOR SIMPLE FOREBODY

IF(1.-ABS(1STHE)).LT.(EPS1) GO TO 43
DD(1,1)=1X8*STHE2+(1Y8*SPH12+1Z8*CPH12)*CTHE2
DD(1,2)=CTHE*1YMZB*.5*S2PH1
DD(1,3)=-1X8*CC(1,3)
DD(2,1)=DD(1,2)
DD(2,2)=1Y8*CPH12+1Z8*SPH12
DD(2,3)=0.
DD(3,1)=DD(1,3)
DD(3,2)=0.
DD(3,3)=1X8
EE(1)=PSD*TD*(1X8-1Y8*SPH12-1Z8*CPH12)*(-S2THE)+PSOPND*1YMZB
11-CTHE2*S2PH1)+TDPND*(CTHE*(1X8-1YMZB*CPH1)+THE2*.5*STHE*1YMZB
1S2PH1-TPD*(ABAR*DAOPSI+BBAR*DBOPSI))/LT+SPSI
EE(2)=PSOPND*CTHE*(1X8-1YMZB*CPH1)+TDPND*1YMZB*S2PH1+PSID2*.5
1S2THE*(1X8-1Y8*SPH12-1Z8*CPH12)-TPD*(ABAR*DAOTHE+BBAR*DBOTHE+
2CBAR*DCOTHE)/LT+QTHE
EE(3)=PSD*TD*CTHE*(1X8+1YMZB*CPH1)+PS1D2*(CTHE2*1YMZB*.5*S2PH1)+
1THE2*(-.5*S2PH1*1YMZB)-TPD*(ABAR*DAOPH+BBAR*DBOPH+CBAR*DCDPH1)/
2LT+QPH1
CALL PIVERT(DD,EE,3,6,1,EPS,1ERSW)
IF(1ERSW.EQ.0) GO TO 43
WRITE(10UT,51) 1ERSW
51 FORMAT(/,5X,'INCONSISTENT EQUATIONS ON FOREBODY',/20X,'1ERSW=',I2)
STOP
43 EE(4)=(FX+TPD*ABAR/LT)/M
EE(5)=(FY+TPD*BBAR/LT)/M
EE(6)=(FZ+TPD*CBAR/LT)/M
GO TO 41
40 CONTINUE

EQUATIONS OF MOTION FOR GENERAL FOREBODY

IF(1.-ABS(1STHE)).LT.(EPS1) GO TO 41
DD(1,1)=STHE2*1X8+CTHE2*(1Y8*SPH12+1Z8*CPH12-1Y2B*S2PH1)
1-S2THE*(1X8*SPH1+1X2B*CPH1)
DD(1,2)=CTHE*(1YMZB*.5*S2PH1-1Y2B*CPH1)-1X2B*S2C3+1X2B*S2S3
DD(1,3)=-1X8*CC(1,3)+1X2B*CC(2,3)+1X2B*CC(3,3)
DD(1,4)=M*(1X8*CC(1,2)+YBAR*CC(2,2)+ZBAR*CC(3,2))
DD(1,5)=M*(1X8*CC(1,1)+YBAR*CC(2,1)+ZBAR*CC(3,1))
DD(1,6)=0.
DD(2,1)=DD(1,2)
DD(2,2)=1Y8*CPH12+1Z8*SPH12+1Y2B*S2PH1
DD(2,3)=1X2B*CPH1-1X2B*SPH1
DD(2,4)=M*(1X8*CC(1,2)+YBAR*CC(2,2)+ZBAR*CC(3,2))
DD(2,5)=M*(1X8*CC(1,1)+YBAR*CC(2,1)+ZBAR*CC(3,1))
DD(2,6)=0.
DD(3,1)=DD(1,3)
DD(3,2)=1Y8*CPH12+1Z8*SPH12+1Y2B*S2PH1
DD(3,3)=1X2B*CPH1-1X2B*SPH1
DD(3,4)=M*(1X8*CC(1,2)+YBAR*CC(2,2)+ZBAR*CC(3,2))
DD(3,5)=M*(1X8*CC(1,1)+YBAR*CC(2,1)+ZBAR*CC(3,1))
DD(3,6)=0.

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01107	5440	C	EQUATIONS OF MOTION IF NO ADDED MASS IS INCLUDED ON PARACHUTE
01107	5450	C	
01107	5460	C	
01111	5470		FF(1)=(-PSIPD*THEPD+S2THEP+IXMYPB-TPD*(ABAR*DADPSP+BBAR*DBOPSP)/
01111	5480		1LT+QPSIP)/(IXPB+S2THEP+IYPB*CTHEP2)
01112	5490		FF(2)=(-PSIPD*5+S2T EP+IXMYPB-TPD*(ABAR*DADTTP+BBAR*DBOTHP+)
01112	5500		ICBAR*DCOTHP)/LT+QTHEP)/IYPB
01113	5510		FF(3)=(-TPD*ABAR/LT+FXP)/MP
01114	5520		FF(4)=(-TPD*BBAR/LT+FYPI)/MP
01115	5530		FF(5)=(-TPD*CBAR/LT+FZPI)/MP
01116	5540		RETURN
01117	5550		42 CONTINUE
01117	5560	C	EQUATIONS OF MOTION IF ADDED MASS IS INCLUDED ON PARACHUTE
01117	5570	C	
01117	5580	C	
01120	5590		SPSIP2=SPSIP**2
01121	5600		CPSIP2=CPSIP**2
01122	5610		S2PSIP=2**SPSIP*CPSIP
01123	5620		C2PSIP=CPSIP2-SPSIP2
01124	5630		C2THEP=CTHEP2-STHEP2
01125	5640		XPD2=XPD**2
01126	5650		YPD2=YPD**2
01127	5660		ZPD2=ZPD**2
01130	5670		XPNYPD=XPD*YPD
01131	5680		XPDPD=XPD*ZPD
01132	5690		YPCZPD=YPD*ZPD
01133	5700		XPPSPD=XPD*PSIPD
01134	5710		XPTHPD=XPD*THEPD
01135	5720		YPPSPD=YPD*PSIPD
01136	5730		YPTHPD=YPD*THEPD
01137	5740		ZPPSPD=ZPD*PSIPD
01140	5750		ZPTHPD=ZPD*THEPD
01141	5760		DDP(1,1)=HPL*CTHEP2+CPSIP2+MPS*(SPSIP2+STHEP2+CPSIP2)
01142	5770		DDP(1,2)=HPL*CTHEP2+5*S2PSIP*CTHEP2
01143	5780		DDP(1,3)=HPL*CTHEP2+5*S2THEP*CPSIP
01144	5790		DDP(2,1)=DDP(1,2)
01145	5800		DDP(2,2)=HPL*CTHEP2+PSIP2+MPS*(CPSIP2+SPSIP2+STHEP2)
01146	5810		DDP(2,3)=HPL*CTHEP2+PSIP*52THEP
01147	5820		DDP(3,1)=DDP(1,3)
01150	5830		DDP(3,2)=DDP(2,3)
01151	5840		DDP(3,3)=HPL*STHEP2+MPS*CTHEP2
01152	5850		EEP(1)=2**XPPSPD*DDP(1,2)-2PPSPD*DDP(2,3)+MLMSP*(XPTHPD+S2THEP
01152	5860		1-CPSIP2+YPPSPD-C2PSIP*CTHEP2-YPTHPD*5+S2THEP*S2PSIP-ZPTHPD*5
01152	5870		2C2THEP*CPSIP)-TPD*ABAR/LT+FXP
01153	5880		EEP(2)=2**YPPSPD*DDP(1,2)+2PPSPD*DDP(1,3)+MLMSP*(XPPSPD+C2PSIP
01153	5890		1-CTHEP2-XPTHPD*5+S2THEP*S2PSIP+YPTHPD*52THEP*SPSIP2+ZPTHPD*5
01153	5900		2SPSIP*CTHEP1-TPD*BBAR/LT+FYPI
01154	5910		EEP(3)=XPPSPD*DDP(2,3)+YPPSPD*DDP(1,3)+MLMSP*(XPTHPD+CPSIP*5
01154	5920		1-CTHEP+YPTHPD*SPSIP+CTHEP2-2PTHPD*52THEP)-TPD*CBAR/LT+FZP
01155	5930		FF(1)=(-PSIPD*THEPD+S2THEP+IXMYPB-MLMSP*XPYPD*CTHEP2+C2PSIP+)
01155	5940		IXPD2PD*DDP(2,3)-YPD2PD*DDP(1,3)+XPD2-YPD2)*DDP(1,2)
01155	5950		2-TPD*(ABAR*DADPSP+BBAR*DBOPSP)/LT+QPSIP)/(IXPB+S2THEP+IYPB*CTHEP2)
01155	5960		FF(2)=(-PSIPD*5+S2T EP+IXMYPB+MLMSP*(5*(XPPYPD+S2THEP*S2PSIP
01156	5970		1-XPD2+S2THEP*CPSIP2-YPD2*S2THEP*SPSIP2+ZPD2+S2THEP)*XPD2PD+CPSIP
01156	5980		2-CTHEP-YPD2PD*SPSIP*CTHEP)-TPD*(ABAR*DADTTP+BBAR*DBOTHP+)
01156	5990		3CBAR*DCOTHP)/LT+QTHEP)/IYPB

01157	600*	CALL PIVERT(DDP,EEP,3,3,1,EPS,IERSM)
01160	601*	IF(IERSM.NE.0) WRITE(10UT,52)
01163	602*	IF(IERSM.NE.0) STOP
01165	603*	52 FORMAT(//5X,'INCONSISTENT EQUATIONS ON PARACHUTE'//20X,'IERSM=',
01165	604*	112)
01166	605*	FF(3)=EEP(1)
01167	606*	FF(4)=EEP(2)
01170	607*	FF(5)=EEP(3)
01171	608*	RETURN
01172	609*	END

END OF COMPILATION: 11 DIAGNOSTICS.

SUBROUTINE PLTRAJ ENTRY POINT 0C0172

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STORAGE USED: CODE(1) 000235: DATA(0) 000161: BLANK COMMON(2) 000000
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EXTERNAL REFERENCES (BLOCK, NAME)

0003	IDENT
0004	QUIK3V
0005	NERR3S

 STORAGE ASSIGNMENT (BLOCK, TYPE, RELATIVE LOCATION, NAME) |

0001	00013	150L	0001	000156	550L	0001	000156	900L	0000	R	000000	ADAKY	0000	N	000026	FLDX		
0000	R	000042	FLOY	0000	000142	INJPS	0000	I	000137	15YM	0000	I	000136	ITIME	0000	N	000036	LABELS

***** DIAGNOSTIC ***** THE NAME BUFF APPEARS IN A DIMENSION OR TYPE STATEMENT BUT IS NEVER REFERENCED.

SUBROUTINE PLTRAJ(X,Y1,Y2,Y3,Y4,N,IX,IY1,IY2,IY3,IY4,HDR)

X IS THE ARRAY CONTAINING THE ABSCISSA VALUES

Y1,Y2,Y3,Y4 ARE THE ARRAYS CONTAINING THE ORDINATE VALUES FOR THE
FOUR POSSIBLE ORDINATE AXES CORRESPONDING TO X
Y1 IS THE RIGHT MOST AXIS

N IS THE NUMBER OF POINTS PER ARRAY

IX SPECIFIES THE TITLE OF THE ABSCISSA AXIS
IF IX=10, THE TITLE IS 'TIME SEC.'

1Y1, 1Y2, 1Y3, 1Y4 SPECIFY THE TITLES OF THE FOUR ORDINATE AXES RESPECTIVELY
 IF ONLY ONE ORDINATE IS DESIRED , SET 1Y2=1Y3=1Y4=0
 IF ONLY TWO ORDINATES ARE DESIRED , SET 1Y3=1Y4=0
 IF ONLY THREE ORDINATES ARE DESIRED , SET 1Y4=0

NDNR IS AN ALPHAMERIC ARRAY USED AS A TITLE TO THE PLOT

ALL SCALING IS AUTOMATIC

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DIMENSION X(1),Y1(1),Y2(1),Y3(1),Y4(1),HDR(1),BUFF(500)

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DIMENSION ADAM(22),FLOX(12),FLOY(12)

REAL LABELS (4,12)

DATA ADARY / 19 INCH. PAPER, 1 CO., PY

[illegible]

DATA	FLDX	%
1	1	1
2	2	2
3	3	3
4	4	4
5	5	5
6	6	6
7	7	7
8	8	8
9	9	9
10	10	10
11	11	11
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99	99	99
100	100	100


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00110 310
00112 0DIAGNOSTIC THE LIST CONTAINS AN ILLEGAL ITEM.
00112 320 DATA FLOY
00112 330
00112 0DIAGNOSTIC A LIST IN THE ABOVE STATEMENT IS TOO LONG.
00114 340 DATA LABELS /ALTITU /DE M /
00114 350 'YAW ATTITUDE' DE M /
00114 360 'PITCH ATTITUDE' DE DEG
00114 370 'ROLL A ATTITUDE' DE DEG
00114 380 'ANGLE OF ATTACK' DEG
00114 390 'MACH NO' UMBER
00114 400 'FLIGHT PATH' ANGLE DEG
00114 410 'DYNAM' PRESS LB / FT002
00114 420 'TENSIO' N LB
00114 430 'TIME' SEC
00114 440 'CHUTE' ANG OF ATT DEG
00114 0DIAGNOSTIC A LIST IN THE ABOVE STATEMENT IS TOO LONG.
00114 450 DATA /TIME/O/
00120 460 IF (IA.LE. 0) GO TO 900
00120 470 IF (ITIME) GO TO 150
00125 480 100 CALL IDENT(9,ADARY)
00126 490 150 ITIME = ITIME + 1
00126 500
00126 510 C
00130 520 ISYM = 34
00131 530 FLOX(1) = LABELS(1,IX)
00132 540 FLOX(2) = LABELS(2,IX)
00133 550 FLOX(3) = LABELS(3,IX)
00134 560 FLOX(4) = LABELS(4,IX)
00137 570 IF (IY1) 550,55C,510
00140 580 510 CONTINUE
00141 590 FLOY(1) = LABELS(1,IY1)
00142 600 FLOY(2) = LABELS(2,IY1)
00143 610 FLOY(3) = LABELS(3,IY1)
00144 620 FLOY(4) = LABELS(4,IY1)
00145 630 CALL QUIK3V(1,ISYM,FLOX,FLOY,N,X,Y1)
00150 640 IF (IY2) 550,55C,520
00151 650 520 CONTINUE
00152 660 FLOY(1) = LABELS(1,IY2)
00153 670 FLOY(2) = LABELS(2,IY2)
00154 680 FLOY(3) = LABELS(3,IY2)
00155 690 FLOY(4) = LABELS(4,IY2)
00156 700 CALL QUIK3V(1,ISYM,FLOX,FLOY,N,X,Y2)
00161 710 IF (IY3) 550,55C,530
00162 720 530 CONTINUE
00163 730 FLOY(1) = LABELS(1,IY3)
00164 740 FLOY(2) = LABELS(2,IY3)
00165 750 FLOY(3) = LABELS(3,IY3)
00166 760 FLOY(4) = LABELS(4,IY3)
00172 770 CALL QUIK3V(1,ISYM,FLOX,FLOY,N,X,Y3)
00173 780 IF (IY4) 550,55C,540
00174 790 540 CONTINUE
00175 800 FLOY(1) = LABELS(1,IY4)
00176 810 FLOY(2) = LABELS(2,IY4)
00177 820 FLOY(3) = LABELS(3,IY4)
00177 830 FLOY(4) = LABELS(4,IY4)
00177 840 CALL QUIK3V(1,ISYM,FLOX,FLOY,N,X,Y4)

```

00200
00201
00202
00203

84.
85.
86.
87.
88.

SSO CONTINUE
C
900 CONTINUE
RETURN
END

END OF COMPILATION;

9 DIAGNOSTICS.

0700:US INTERP
MSD 11A -03/27/74-0(119128 (0,1))

SUBROUTINE INTERP ENTRY POINT 000113

STORAGE USED: CODE(1) 000125: DATA(0) 000017: BLANK COMMON(2) 000000

EXTERNAL REFERENCES (BLOCK, NAME)

0003 WERR38

STORAGE ASSIGNMENT (BLOCK, TYPE, RELATIVE LOCATION, NAME)

0000 R 000000 CFI 0000 R 000001 CF2 0000 000002 INJP's

```
00101 1* SUBROUTINE INTERP(CF,AMSL,ALPSL,PHISL,I,J,J,K,K,I,J,K,CF)
00101 2* C
00101 3* C THREE DIMENSIONAL LINEAR INTERPOLATION TO FIND AERO. COEFF.
00101 4* C
00103 5* DIMENSION CCF(11,J,J,K,K)
00104 6* CFI=(CCF(1,J-1,K)-CCF(1,J-1,K-1))*PHISL+CCF(1-1,J-1,K)
00104 7* 1+(CCF(1,J,K)-CCF(1-1,J,K))*PHISL+CCF(1-1,J,K)-((CCF(1,J-1,K)
00104 8* 2-CCF(1-1,J-1,K))*PHISL+CCF(1-1,J-1,K))*ALPSL
00105 9* CF2=(CCF(1,J-1,K-1)-CCF(1-1,J-1,K-1))*PHISL+CCF(1-1,J-1,K-1)+
00105 10* 1+(CCF(1,J,K-1)-CCF(1-1,J,K-1))*PHISL+CCF(1-1,J,K-1)-((CCF(1,
00105 11* 2J-1,K-1)-CCF(1-1,J-1,K-1))*PHISL+CCF(1-1,J-1,K-1))*ALPSL
00106 12* CF=AMSL*(CF1-CF2)+CF2
00107 RETURN
00110 END
```

END OF COMPILATION: NO DIAGNOSTICS.

FOR US PIVERT
MSO 11A -03/27/74-00:19:30 (0.1)

SUBROUTINE PIVERT ENTRY POINT 000640

STORAGE USED: CODE(1) 000705; DATA(0) 000111; BLANK COMMON(2) 000000

EXTERNAL REFERENCES (BLOCK, NAME)

0003 NERR39

STORAGE ASSIGNMENT (BLOCK, TYPE, RELATIVE LOCATION, NAME)

0001	000044	1166	0001	000240	120L	0001	000367	1216	0001	000123	1376	0001	000416	150L
0001	000205	1576	0001	000232	176G	0001	000451	180L	0001	000275	2056	0001	000371	2176
0001	000605	220L	0001	000376	2236	0001	000410	230L	0001	000423	2406	0001	000464	2546
0001	000537	2616	0001	000567	2666	0001	000133	30L	0001	000137	70L	0001	000021	1
0000	1	000025	11	0000	1	000026	111	0000	1	000016	11	0000	1	000017
0000	1	000022	J	0000	1	000020	K	0000	1	000024	K1	0000	1	000014
0000	1	000015	L2	0000	D	000002	ONE	0000	U	000004	PIV	0000	U	000014
0000	D	000012	TOL	0000	D	000000	ZE O	0000	U	000004	PIV1	0000	U	000010

SUBROUTINE PIVERT(A,R,M,MD,N,EPS,IER)

TO SOLVE A GENERAL SYSTEM OF SIMULTANEOUS LINEAR EQUATIONS.
SOLUTION IS DONE BY MEANS OF GAUSS-ELIMINATION WITH
COMPLETE PIVOTING.

DESCRIPTION OF PARAMETERS

A	- THE M BY M COEFFICIENT MATRIX. (DESTROYED)	IER=0	- NO ERROR.
R	- THE M BY N MATRIX OF RIGHT HAND SIDES. (DESTROYED)	IER=1	- NO RESULT BECAUSE OF M LESS THAN 1 OR PIVOT ELEMENT AT ANY ELIMINATION STEP EQUAL TO 0.
M	- ON RETURN R CONTAINS THE SOLUTION OF THE EQUATIONS.	IER=K	- WARNING DUE TO POSSIBLE LOSS OF SIGNIFI- CANCE INDICATED AT ELIMINATION STEP K+1. WHERE PIVOT ELEMENT WAS LESS THAN OR EQUAL TO THE INTERNAL TOLERANCE EPS TIMES ABSOLUTELY GREATEST ELEMENT OF MATRIX A.
MD	- THE NUMBER OF EQUATIONS IN THE SYSTEM.		
N	- THE DIMENSION OF A		
EPS	- AN INPUT CONSTANT WHICH IS USED AS RELATIVE TOLERANCE FOR TEST ON LOSS OF SIGNIFICANCE.		
IER	- RESULTING ERROR PARAMETER CODED AS FOLLOWS		

REMARKS

00101	10	C	GELG 70
00101	20	C	GELG 470
00101	30	C	GELG 480
00101	40	C	GELG 110
00101	50	C	GELG 120
00101	60	C	GELG 150
00101	70	C	GELG 130
00101	80	C	GELG 140
00101	90	C	GELG 160
00101	100	C	GELG 170
00101	110	C	GELG 180
00101	120	C	GELG 190
00101	130	C	GELG 200
00101	140	C	GELG 210
00101	150	C	GELG 220
00101	160	C	GELG 230
00101	170	C	GELG 240
00101	180	C	GELG 250
00101	190	C	GELG 260
00101	200	C	GELG 270
00101	210	C	GELG 280
00101	220	C	GELG 290
00101	230	C	GELG 300
00101	240	C	GELG 310
00101	250	C	
00101	260	C	
00101	270	C	

```

00101 280
00101 290
00101 300
00101 310
00101 320
00101 330
00101 340
00101 350
00101 360
00101 370
00101 380
00101 390
00103 400
00104 410
00105 420
00110 430
00110 440
00110 450
00110 460
00114 470
00115 480
00120 490
00123 500
00124 510
00127 520
00130 530
00131 540
00132 550
00135 560
00135 570
00135 580
00135 590
00135 600
00136 610
00136 620
00136 630
00141 640
00144 650
00147 660
00152 670
00153 680
00154 690
00155 700
00155 710
00155 720
00155 730
00156 740
00161 750
00162 760
00163 770
00163 780
00163 790
00165 800
00165 810
00165 820
00170 830

      THIS IS A MODIFICATION OF GELG (FROM IBM-SSP)
      INPUT MATRICES M AND A ARE ASSUMED TO BE STORED COLUMNWISE
      THE PROCEDURE GIVES RESULTS IF THE NUMBER OF EQUATIONS M IS
      GREATER THAN O AND PIVOT ELEMENTS AT ALL ELIMINATION STEPS
      ARE DIFFERENT FROM O. HOWEVER WARNING IER=K - IF GIVEN -
      INDICATES POSSIBLE LOSS OF SIGNIFICANCE. IN CASE OF A WELL
      SCALED MATRIX A AND APPROPRIATE TOLERANCE EPS, IER=K MAY BE
      INTERPRETED THAT MATRIX A HAS THE RANK K. NO WARNING IS
      GIVEN IN CASE M=1.

      .....
      DIMENSION A(MD,M),R(MD,M)
      DOUBLE PRECISION A,R,EPS,ZERO,ONE,PIV,PIV1,TB,TOL
      DATA ZERO,ONE/0.000,1.000/
      IF(M)230,230,10
      .....
      SEARCH FOR GREATEST ELEMENT IN MATRIX A
      10 IER = 0
      PIV = ZERO
      DO 30 L1=1,M
      DO 30 L2=1,M
      TB= DABS(A(L1,L2))
      IF(TB - PIV)30,30,20
      20 PIV = TB
      11 = L1
      12 = L2
      30 CONTINUE
      TOL = EPS*PIV

      A(I1) IS PIVOT ELEMENT. PIV CONTAINS THE ABSOLUTE VALUE OF A(I1).
      GELG 700

      START ELIMINATION LOOP
      DO 170 K=1,M
      .....
      TEST ON SINGULARITY
      IF(PIV)230,230,40
      40 IF(IER)70,50,70
      50 IF(PIV - TOL)60,60,70
      60 IER = K-1
      70 PIV1 = ONE/A(I1,I2)
      J = 11-K
      J = 12-K
      I+K IS ROW-INDEX, J+K COLUMN-INDEX OF PIVOT ELEMENT
      GELG 860
      GELG 870
      GELG 880

      PIVOT ROW REDUCTION AND ROW INTERCHANGE IN RIGHT HAND SIDE M
      DO 80 L=1,N
      TB = PIV1*A(I1,L)
      R(I1,L) = R(K,L)
      80 R(K,L) = TB

      IS ELIMINATION TERMINATED
      IF(K-M)90,180,180
      GELG 950

      COLUMN INTERCHANGE IN MATRIX A
      90 CONTINUE
      GELG 980

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```

PC171      940      IF(J)120,120,100
PC174      950      100 CONTINUE
PC175      960      DO 110 L=K,M
PC200      970      TB = A(L,K)
PC201      980      A(L,K) = A(L,12)
PC202      990      110 A(L,12) = TB
PC207      700      C
PC207      710      C
PC207      720      ROW INTERCHANGE AND PIVOT ROW REDUCTION IN MATRIX A
PC207      730      DO 130 L=K,M
PC210      740      TB = PIV(A(11,L))
PC211      750      A(11,L) = A(K,L)
PC211      760      130 A(K,L) = TB
PC211      770      C
PC211      780      C
PC213      790      SAVE COLUMN INTERCHANGE INFORMATION
PC213      800      A(K,K) = J
PC213      810      C
PC213      820      C
PC213      830      ELEMENT REDUCTION AND NEXT PIVOT SEARCH
PC214      840      PIV = ZERO
PC215      850      KI = K+1
PC216      860      DO 160 I=KI,M
PC221      870      PIV1 = -A(11,K)
PC222      880      DO 150 L=KI,M
PC225      890      A(11,L) = A(11,L) + PIV1*A(K,L)
PC226      900      TB=DABS(A(11,L))
PC227      910      IF(TB - PIV)150,150,140
PC232      920      140 PIV = TB
PC233      930      11 = 11
PC234      940      12 = L
PC235      950      150 CONTINUE
PC237      960      DO 160 L=1,M
PC242      970      140 R(11,L) = R(11,L) + PIV1*R(K,L)
PC245      980      170 CONTINUE
PC245      990      C
PC245      1000     END OF ELIMINATION LOOP
PC245      1010     C
PC245      1020     BACK SUBSTITUTION AND BACK INTERCHANGE
PC247      1030     180 IF(M-1)230,220,190
PC252      1040     190 CONTINUE
PC253      1050     DO 210 I=2,M
PC256      1060     11 = M+1 - I
PC257      1070     L = A(11,11) + .F
PC260      1080     DO 210 J=1,M
PC263      1090     TB = R(11,J)
PC264      1100     111 = 11+1
PC265      1110     DO 200 K=111,M
PC270      1120     200 TB = TB - A(11,K)*R(K,J)
PC272      1130     R(11,J) = R(11,L,J)
PC273      1140     210 R(11,L,J) = TB
PC274      1150     220 RETURN
PC274      1160     C
PC274      1170     ERROR RETURN
PC277      1180     230 IER = -1
PC277      1190     RETURN
PC300      1200     END
PC301      1210

```

6EL61080

6EL61150

6EL61180

6EL61380

6EL61410

6EL61620

END OF COMPILATION: NO DIAGNOSTICS.

0FOR,US DENS
MSD 11A -03/27/77-00119134 (0.1)

SUBROUTINE DENS ENTRY POINT 000106

STORAGE USED: CODE(1) 000121; DATA(0) 000 011 BLANK COMMON(2) 000000

EXTERNAL REFERENCES (BLOCK, NAME)

0003 EXP
0004 XPRR
0005 SORT
0006 MEMR35

STORAGE ASSIGNMENT (BLOCK, TYPE, RELATIVE LOCATION, NAME)

0001	000011 1216	0001	00022 2L	0001	00050 3L	0001	00060 4L	0000	K 000102 A
0000	R 000130 8	0000	R 000160 0M	0000	R 000164 M	0000	R 000000 MB	0000	I 000167 I
0000	000170 INJPS	0000	R 00026 P8	0000	R 000162 T	0000	R 000054 TB	0000	R 000161 TEMP

00101 SUBROUTINE DENSIZ, P, RHO, CS)
00102 DOUBLE PRECISION Z
00103 DIMENSION HB(22), PD(22), TB(22), A(22), B(22)
00104 DATA HB/0.,.36789239,65616,798,10496,88,15419,48,170603,67,
00105 1 200131,23,259186,35,291153,40,3230,2,75,354753,59,36406,39,
00106 2 480781,04,512046,16,543215,48,655268,46,728243,91,939894,75,
00107 3 1234619,4,152799,4,1798726,4,2068776,6/
00108 DATA PD/2116,217,472,67922,114,34505,16,128852,2,3162994,
00109 1 1,232512,3632173,021672818,003431482,00062812953,
00110 2 00015359986,0005264607,00010571582,0000077157071,
00111 3 000005832472,0000035196139,00000145371,39343987E-6,
00112 4 84176667E-7,22884174E-7,7205836E-8,24891264E-8/
00113 DATA TB/28A,15,29216,65,228,65,29270,65,252,65,2,180,65,210,65,
00114 1 260,65,362,65,960,65,111C,65,1210,65,1350,65,1550,65,1830,65,
00115 2 2180,65,2420,65,2590,65,2700,65/
00116 DATA A/-6A755856E-5,0.,.14068775E-5,.37325169E-5,0.,
00117 1 -.22523554E-5,0.,.M8256481E-5,0.,.52141408E-5,.74757236E-5,
00118 2 .1212076E-4,17,28281E-4,49941997E-5,.28886537E-5,
00119 3 .18635746E-5,1204117E-5,.85314774E-6,.6116347E-6,
00120 4 .42048419E-6,2526889E-6,2,1572315E-6/
00121 DATA B/5,255886,48063132E-4,34,163232,12,201179,38473567E-4,
00122 1 17,081627,8,540804,57641135E-4,11,055224,6,6127901,
00123 2 -3,2961763,1,6390858,-2,17,4464,3,245879,-4,6156449,
00124 3 -6,4033868,-7,8733154,-9,3039039,-11,4627,-17,025198,
00125 4 2,-25,562133/
C

H = 20855531.E02/(20855531.E0 + Z)
DO 1 I = 2, 22
IF (H-MB(I)2,1,1)

```

00126 300 1 CONTINUE
00130 310 I = 23
00131 320 2 I = I - 1
00132 330 DH = H - HB(I)
00133 340 TEMP = 1. + A(I)*DH
00134 350 T = TB(I)*TEMP
00135 360 IF(A(I))3,6,3
00140 370 6 TEMP = EXP(B(I)*DH)
00141 380 GO TO 4
00142 390 3 TEMP = TEMP**8(I)
00143 400 4 P = PB(I)*TEMP
00144 410 RH0 = .32364)4E-30P/T
00145 420 CS = 65.77032EQ*SQR(T)
00146 430 RETURN
00147 440 END

```

END OF COMPILATION: NO DIAGNOSTICS.

0708,US DENS

MSD 11A -03/27/74-00119:37 (0.1)

SUBROUTINE DENS ENTRY POINT 0C0111

STORAGE USED: CODE(1) 0001241 DATA(0) 000 061 BLANK COMMON(2) 0000003

EXTERNAL REFERENCES (BLOCK, NAME)

0003 EXP
0004 XPRR
0005 SORT
0006 MERR3S

STORAGE ASSIGNMENT (BLOCK, TYPE, RELATIVE LOCATION, NAME)

0001 000C13 1226	0001 000C24 2L	0001 000-52 3L	0001 000062 4L	000J M 000104 A
0000 R 000132 8	0000 R 000162 0M	0000 R 000160 M	0000 R 000002 M8	000U I 000161 I
0000 000175 INJPS	0000 R 000C30 PB	0000 R 000164 Y	0000 R 000056 T8	000U M 000163 TEMP
0000 0 000000 2				

SUBROUTINE DENS(121, P, RHO, CS)
DOUBLE PRECISION L,Z1
DIMENSION HB(22), PB(22), TB(22), A(22), B(22)
DATA HB/0.,.36289,239.65616,798,104986.88,154199.48,170603.67,
1 200131.23,259186.35,291153.40,323002.75,354753.59,386406.39,
2 480781.04,512046.16,543215.48,605268.46,728243.91,939894.75,
3 1234619.4,1526799.4,1798726.4,2068776.6/
DATA PB/2116.217,472.67922,114.34505,18.128852,2.3162994,
1 1.2322512,0.38032173,0.021672818,0.034331482,0.0062812953,
2 0.0015359986,0.0005266837,0.00010571582,0.000077157071,
3 0.000058324672,0.000035196139,0.0000145371,0.39343987E-6,
4 0.84176667E-7,0.22884174E-7,0.72058934E-8,0.24891264E-8/
DATA TB/28A,15.2,216.65,228.65,2270.65,252.65,2.180.65,210.65,
1 260.65,365.960.65,1110.65,11210.65,1350.65,1550.65,1800.65,
2 2160.65,2420.65,2590.65,2700.65/
DATA A/-68755056E-5,0.,0.14068775E-5,0.37325169E-5,0.,
1 -22523554E-5,0.4825481E-5,0.,0.521440E-5,0.74757236E-5,
2 -12120769E-4,0.17 28281E-4,0.49941997E-5,0.28886537E-5,
3 0.18635746E-5,0.12041172E-5,0.85314774E-6,0.6116347E-6,
4 0.2048419E-6,0.2526889E-6,0.201572315E-6/
DATA B/5.255886,0.48063102E-4,0.34.163232,-12.201179,0.38473567E-4,
1 17.081627,0.540804,-0.57641135E-4,-11.055226,-6.6127901,
2 -3.2961763,-1.6390858,-2.1704464,-3.2456979,4.6156949,
3 -6.4033868,-7.8733154,-9.3039039,-11.4627,-17.025198,
4 20.25.562133/
C

Z = 2103.28084
M = 20855531.E0+2/(20855531.E0 + 2)

```

00121 00 1 1 = 2, 22
00124 IF(M-NB(1))2,1,1
00127 CONTINUE
00131 1 = 23
00132 2 1 = 1 - 1
00133 DM = M - NB(1)
00134 TEMP = 1. + A(1)*DM
00135 T = TB(1)*TEMP
00136 IF(A(1))3,6,3
00141 4 TEMP = EXP(8(1)*DM)
00142 GO TO 4
00143 3 TEMP = TEMP*B(1)
00144 4 P = PB(1)*TEMP*47.88025
00145 RHO = .003483657*P/T
00146 CS = 20.04679*SQRT(T)
00147 RETURN
00150 END

```

END OF COMPILATION: NO DIAGNOSTICS.

DEPT,T
FURPUR 24HI-03/27-00:19

1HNTSV443021*TPFS ELEMENT TABLE

D NAME	VERSION	TYPE	DATE	TIME	SEN #	SIZE-PRE,TEAT	(CYCLE WORD)	PSRNUDE	LOCATION
PL6DOF		FOR SYMB	27 MAR 74	00:17:04	1	168	5	0	1792
PL6DOF		RELOCATABLE	27 MAR 74	00:17:14	2	204	5	0	1960
SUBR		FOR SYMB	27 MAR 74	00:17:20	3	147	5	0	2166
SUBR		RELOCATABLE	27 MAR 74	00:17:31	4	176	5	0	2313
PLTRAJ		FOR SYMB	27 MAR 74	00:17:33	5	24	5	0	2491
PLTRAJ		RELOCATABLE	27 MAR 74	00:17:35	6	13	5	0	2515
INTERP		FOR SYMB	27 MAR 74	00:17:36	7	5	5	0	2529
INTERP		RELOCATABLE	27 MAR 74	00:17:37	8	5	5	0	2534
PIVERT		FOR SYMB	27 MAR 74	00:17:55	9	41	5	0	2540
PIVERT		RELOCATABLE	27 MAR 74	00:17:58	10	25	5	0	2581
DENS		FOR SYMB	27 MAR 74	00:18:01	11	14	5	0	2607
DENS		RELOCATABLE	27 MAR 74	00:18:03	12	10	5	0	2621
DENSM		FOR SYMB	27 MAR 74	00:18:18	13	14	5	0	2632
DENSM		RELOCATABLE	27 MAR 74	00:18:19	14	11	5	0	2646
A		MAP SYMB	27 MAR 74	00:18:20	15	1	5	0	2654
CHUTE		ABSOLUTE	27 MAR 74	00:18:37	16	868	5	1	2659
PL6DOF		FOR SYMB	27 MAR 74	00:19:03	17	168	5	1	3527
PL6DOF		RELOCATABLE	27 MAR 74	00:19:12	18	204	5	1	3695
SUBR		FOR SYMB	27 MAR 74	00:19:15	19	147	5	1	3901
SUBR		RELOCATABLE	27 MAR 74	00:19:25	20	176	5	1	4048
PLTRAJ		FOR SYMB	27 MAR 74	00:19:26	21	24	5	1	4226
PLTRAJ		RELOCATABLE	27 MAR 74	00:19:27	22	13	5	1	4250
INTERP		FOR SYMB	27 MAR 74	00:19:28	23	5	5	1	4264
INTERP		RELOCATABLE	27 MAR 74	00:19:30	24	5	5	1	4269
PIVERT		FOR SYMB	27 MAR 74	00:19:31	25	41	5	1	4275
PIVERT		RELOCATABLE	27 MAR 74	00:19:34	26	25	5	1	4316
DENS		FOR SYMB	27 MAR 74	00:19:35	27	14	5	1	4342

54-FY. PROQUE DEPLOYMENT

IXB	IXYB	XBAR	S	CLLP	OPPRIN	OPSYM	ALPHI	AJALPH	ALPHID	DTI	EPST
IYB	IYZB	YBAR	D	CLMQ	OPPLPY	OPDA	AJALPF		AJALPD	TTY	ETAI
IZB	IYZB	ZBAR	WEIGHT	CLNR	OPOS	OMETNC	AKAM		AKAMD	MM	
171149.0		-2.000	116.260	.000	1.	0.	2.		2.	.0100	.000006
8539000.0		.000	12.167	.000	0.	0.	16.	16.	6.	20.0000	.000010
8539000.0		.000	161300.00	.000	1.	0.	6.		2.	6000.0	

A	LTO	LS	AMAX1	AMAX2	AMAY1	AMAY2	AP	GLOAD	FREQ	OPAM	PCT01
B	NT	NS	OSX1	OSX2	DSY1	DSY2	CHIPE	FSULT	POROS	OPOT	PCT02
C	DLTO	DP	WTC	WTL	WTP	CCRIT	VP	AERATO	TO	OPSP	PCT03
TRO	TRI	TM2	TK3	SPRO	SPR1	SPR2	SPR3				
83.800	6.500	100.000	650.000	16.500	720.000	11.500	63.819	.000	.000	1.000	.000
.000	3.000	56.000	150.000	43.000	210.000	52.000	.000	.000	.150	.000	.000
.010	.010	54.000	219.000	651.000	870.000	.040	552.300	.000	.000	1.000	.000
.000	13.000	100.000	100.000	6.000	1879.100	2290.200	.000				

PARACHUTE SUSPENSION LINE LOAD AND STRAIN ARRAYS

TETHER LINE LOAD AND STRAIN ARRAYS									
PS (A)	.00	1000.00	2000.00	4000.00	6000.00	10000.00	12000.00	16000.00	20000.00
EPL (A)	.0000	.0230	.0560	.0890	.1090	.1370	.1600		
PT (B)	.00	20000.00	35000.00	60000.00	80000.00	120000.00	160000.00	200000.00	240000.00
EPT (B)	.0000	.0250	.0500	.0750	.0900	.11000	.1200		

TEYHER LINE LOAD AND STRAIN ARRAYS

PT(8)	.60	20000.00	35000.00	60000.00	80000.00	120000.00	160000.00	200000.00
EPT(8)	.0000	.0250	.0500	.0750	.0900	.1100	.1200	

PARACHUTE INFLATION TIME HISTORY ARRAY, TTIP

00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00000	00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PARACHUTE AERODYNAMIC REF. AREA ARRAY, SSP

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54-FT. DROGUE DEPLOYMENT

IX8	IXY8	IXBAR	S	CLLP	GPPRIM	OPSYM	ALPHI	AJALPM	ALPHID	DTI	EPST
IX0	IXZ0	YBAR	0	CLMQ	OPLOT	OPDA	AJALPF		AJALPD	YTF	ETAP
IX8	IXZ8	ZBAR	WEIGHT	CLNR	OP05	ONECRC	AKAM		AKAMD	MMH	
171149.0	.0	-2.000	116.260	.000	1.	0.	2.		2.	.0100	.000086
8537000.0	.0	.000	12.107	.000	0.	0.	16.	16.	8.	5.0000	.000410
8537000.0	.0	.000	163300.00	.000	1.	0.	6.1		2.	10000.0	

A	LTO	LS	AMAX1	AMAX2	AMAY1	AMAY2	AP	GLOAD	FREQP	OPAM	PCT01
B	NT	NS	DSX1	DSX2	DSY1	DSY2	CHIPE	FSULT	POROS	OPOT	PCT02
C	DLTO	DP	WTC	WTL	WTP	CCRIT	VP	AERATO	TO	OPSP	PCT03
TRO	TH1	TR2	TN3	SPRO	SPR1	SPR2	SPR3				
03.00	6.500	100.000	660.000	16.500	720.000	11.500	63.819	3.000	7.234	1.000	.100
.000	3.000	54.000	150.000	43.000	210.000	52.000	.000	3.000	.100	1.000	.000
.000	.010	54.000	219.000	651.000	870.000	.060	552.300	1.000	.000	1.000	.000
.000	13.000	100.000	100.000	8.000	1879.100	2290.200	.000				

PARACHUTE SUSPENSION LINE LOAD AND STRAIN ARRAYS

PS(8)	.00	1000.00	2000.00	4000.00	6000.00	10000.00	12000.00
PL(8)	.00000	.0230	.0560	.0890	.1090	.1370	.1600
							.1800

TETHER LINE LOAD AND STRAIN ARRAYS

PT(6)	00	20000.00	35000.00	60000.00	90000.00	120000.00	160000.00	200000.00
EPY(6)	00000	.0250	.0500	.0750	.1000	.1250	.1500	.1750

PARACHUTE INFLATION TIME HISTORY ARRAY, TTIP

[illegible]

PARACHUTE AERODYNAMIC REF. AREA ARRAY, SSP

[illegible]

PPHIE (ROLL ANGLE-DEGREES)

000 340.000

AALPFE (ANGLE OF ATTACK-DEGREES)

Year	1990	1991	1992	1993	1994	1995	1996	1997	1998	1999	2000	2001	2002	2003	2004	2005	2006	2007	2008	2009	2010	2011	2012	2013	2014	2015	2016	2017	2018	2019	2020	2021	2022	2023	2024	2025	2026	2027	2028	2029	2030
Population	100,000	105,000	110,000	115,000	120,000	125,000	130,000	135,000	140,000	145,000	150,000	155,000	160,000	165,000	170,000	175,000	180,000	185,000	190,000	195,000	200,000	205,000	210,000	215,000	220,000	225,000	230,000	235,000	240,000	245,000	250,000	255,000	260,000	265,000	270,000	275,000	280,000	285,000	290,000	295,000	300,000
GDP	100,000	105,000	110,000	115,000	120,000	125,000	130,000	135,000	140,000	145,000	150,000	155,000	160,000	165,000	170,000	175,000	180,000	185,000	190,000	195,000	200,000	205,000	210,000	215,000	220,000	225,000	230,000	235,000	240,000	245,000	250,000	255,000	260,000	265,000	270,000	275,000	280,000	285,000	290,000	295,000	300,000
Unemployment	5.0%	5.5%	6.0%	6.5%	7.0%	7.5%	8.0%	8.5%	9.0%	9.5%	10.0%	10.5%	11.0%	11.5%	12.0%	12.5%	13.0%	13.5%	14.0%	14.5%	15.0%	15.5%	16.0%	16.5%	17.0%	17.5%	18.0%	18.5%	19.0%	19.5%	20.0%	20.5%	21.0%	21.5%	22.0%	22.5%	23.0%	23.5%	24.0%	24.5%	25.0%
Inflation	2.0%	2.5%	3.0%	3.5%	4.0%	4.5%	5.0%	5.5%	6.0%	6.5%	7.0%	7.5%	8.0%	8.5%	9.0%	9.5%	10.0%	10.5%	11.0%	11.5%	12.0%	12.5%	13.0%	13.5%	14.0%	14.5%	15.0%	15.5%	16.0%	16.5%	17.0%	17.5%	18.0%	18.5%	19.0%	19.5%	20.0%	20.5%	21.0%	21.5%	22.0%
Interest Rate	5.0%	5.5%	6.0%	6.5%	7.0%	7.5%	8.0%	8.5%	9.0%	9.5%	10.0%	10.5%	11.0%	11.5%	12.0%	12.5%	13.0%	13.5%	14.0%	14.5%	15.0%	15.5%	16.0%	16.5%	17.0%	17.5%	18.0%	18.5%	19.0%	19.5%	20.0%	20.5%	21.0%	21.5%	22.0%	22.5%	23.0%	23.5%	24.0%	24.5%	25.0%
Government Spending	100,000	105,000	110,000	115,000	120,000	125,000	130,000	135,000	140,000	145,000	150,000	155,000	160,000	165,000	170,000	175,000	180,000	185,000	190,000	195,000	200,000	205,000	210,000	215,000	220,000	225,000	230,000	235,000	240,000	245,000	250,000	255,000	260,000	265,000	270,000	275,000	280,000	285,000	290,000	295,000	300,000
Tax Revenue	100,000	105,000	110,000	115,000	120,000	125,000	130,000	135,000	140,000	145,000	150,000	155,000	160,000	165,000	170,000	175,000	180,000	185,000	190,000	195,000	200,000	205,000	210,000	215,000	220,000	225,000	230,000	235,000	240,000	245,000	250,000	255,000	260,000	265,000	270,000	275,000	280,000	285,000	290,000	295,000	300,000
Debt	100,000	105,000	110,000	115,000	120,000	125,000	130,000	135,000	140,000	145,000	150,000	155,000	160,000	165,000	170,000	175,000	180,000																								

ANGLE OF ATTACK-DEGREES

[illegible]

AAH (MACH NUMBER)

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100	101	102	103	104	105	106	107	108	109	110	111	112	113	114	115	116	117	118	119	120	121	122	123	124	125	126	127	128	129	130	131	132	133	134	135	136	137	138	139	140	141	142	143	144	145	146	147	148	149	150	151	152	153	154	155	156	157	158	159	160	161	162	163	164	165	166	167	168	169	170	171	172	173	174	175	176	177	178	179	180	181	182	183	184	185	186	187	188	189	190	191	192	193	194	195	196	197	198	199	200	201	202	203	204	205	206	207	208	209	210	211	212	213	214	215	216	217	218	219	220	221	222	223	224	225	226	227	228	229	230	231	232	233	234	235	236	237	238	239	240	241	242	243	244	245	246	247	248	249	250	251	252	253	254	255	256	257	258	259	260	261	262	263	264	265	266	267	268	269	270	271	272	273	274	275	276	277	278	279	280	281	282	283	284	285	286	287	288	289	290	291	292	293	294	295	296	297	298	299	300	301	302	303	304	305	306	307	308	309	310	311	312	313	314	315	316	317	318	319	320	321	322	323	324	325	326	327	328	329	330	331	332	333	334	335	336	337	338	339	340	341	342	343	344	345	346	347	348	349	350	351	352	353	354	355	356	357	358	359	360	361	362	363	364	365	366	367	368	369	370	371	372	373	374	375	376	377	378	379	380	381	382	383	384	385	386	387	388	389	390	391	392	393	394	395	396	397	398	399	400	401	402	403	404	405	406	407	408	409	410	411	412	413	414	415	416	417	418	419	420	421	422	423	424	425	426	427	428	429	430	431	432	433	434	435	436	437	438	439	440	441	442	443	444	445	446	447	448	449	450	451	452	453	454	455	456	457	458	459	460	461	462	463	464	465	466	467	468	469	470	471	472	473	474	475	476	477	478	479	480	481	482	483	484	485	486	487	488	489	490	491	492	493	494	495	496	497	498	499	500	501	502	503	504	505	506	507	508	509	510	511	512	513	514	515	516	517	518	519	520	521	522	523	524
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CA (AXIAL COEF. ARRAY (IPHI,JALPF,KAM))

MACH NO. = .000

[illegible][illegible]

CA (AXIAL COEF. ARRAY (3PHI, JALPF, KAH))

WACH NO. - .400

[illegible][illegible]

CA (AXIAL COEF. ARRAY (JPHI,JALPF,KAM))

MACH NO. -

[illegible][illegible]

CA (AXIAL COEF. ARRAY (IPHI,JALPF,KAM))

MACH NO.= .900

1.000	.900	.150	.600	.650	.600	.400	.200	-1.400	-2.600	-1.550	.000	.000	.000	.000	.000	.000
1.000	.500	.150	.600	.650	.600	.400	.200	-1.400	-2.600	-1.550	.000	.000	.000	.000	.000	.000

CA (AXIAL COEF. ARRAY (IPHI,JALPF,KAM))

MACH NO.= 1.200

1.550	1.400	.500	.600	.450	.250	.050	-.200	-1.500	-2.850	-2.100	.000	.000	.000	.000	.000	.000
1.550	1.400	.500	.600	.450	.250	.050	-.200	-1.500	-2.850	-2.100	.000	.000	.000	.000	.000	.000

CA (AXIAL COEF. ARRAY (IPHI,JALPF,KAM))

MACH NO.= 1.960

1.100	1.200	1.100	.600	.450	.250	.050	-.150	-1.300	-2.700	-2.300	.000	.000	.000	.000	.000	.000
1.100	1.200	1.100	.600	.450	.250	.050	-.150	-1.300	-2.700	-2.300	.000	.000	.000	.000	.000	.000

CN (NORMAL COEF. ARRAY (IPHI,JALPF,KAM))

MACH NO.= .000

.000	3.200	7.600	5.800	5.700	5.700	5.700	5.800	8.200	3.200	.000	.000	.000	.000	.000	.000	.000
.000	3.200	7.600	5.800	5.700	5.700	5.700	5.800	8.200	3.200	.000	.000	.000	.000	.000	.000	.000

CN (NORMAL COEF. ARRAY (IPHI,JALPF,KAM))

MACH NO.= .400

MACH NO. - .000

CLW (PITCH MON, COEF, ARRAY (PHI, JALPH, KAMK))

MACH NO. = .400

.000	5.100	10.000	5.700	4.300	2.500	.200	-2.100	-8.200	-3.600	.000	.000	.000
.000	5.100	10.000	5.700	4.300	2.500	.200	-2.100	-8.200	-3.600	.000	.000	.000

CLM (PITCH MON, COEF, ARRAY(IPHI,JALPH,KAM))

WACH NO. = .400

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100

CLM (PITCH MOM, COEF, ARRAY (PWL, JALPH, KAM))

MACH NO. 1,700

	7.600	23.100	14.000	11.200	8.200	5.300	.860	-9.500	-3.300	.000	.000	.000
.....	7.600	23.100	14.000	11.200	8.200	5.300	.860	-9.500	-3.300	.000	.000	.000
.....	7.600	23.100	14.000	11.200	8.200	5.300	.860	-9.500	-3.300	.000	.000	.000

CLM (PITCH MON. CORR. APPAYIRI, JALPH. KAM))

WACH NO-2 1-200

	8.000	9.000	10.700	9.400	7.700	6.000	-2.700	-5.700	.000	.000	.000
19.000	12.100	10.700	9.400	7.700	6.000	-2.700	-5.700	.000	.000	.000	.000
19.000	12.100	10.700	9.400	7.700	6.000	-2.700	-5.700	.000	.000	.000	.000

MACH NO. = 1.200

MACH NO. = 1.940

MACH NO. = .000

MACH NO. 0.400

CLL (ROLL MOM. COEF. ARRAY(IPHI,JALPM,KAM))

MACH NO.= .600

.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000

CLL (ROLL MOM. COEF. ARRAY(IPHI,JALPM,KAM))

MACH NO.= .900

.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000

CLL (ROLL MOM. COEF. ARRAY(IPHI,JALPM,KAM))

MACH NO.= 1.200

.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000

CLL (ROLL MOM. COEF. ARRAY(IPHI,JALPM,KAM))

MACH NO.= 1.960

.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000

CLN IYAN MOM. COEF. ARRAY(IPHI,JALPM,KAM))

MACH NO.= .000

.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000

CLN (YAW MOM, COEF, ARRAY(IPHI,JALPM,KAM))

MACH NO.= .900

.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000

CLN (YAW MOM, COEF, ARRAY(IPHI,JALPM,KAM))

MACH NO.= .600

.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000

CLN (YAW MOM, COEF, ARRAY(IPHI,JALPM,KAM))

MACH NO.= .900

.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000

CLN (YAW MOM, COEF, ARRAY(IPHI,JALPM,KAM))

MACH NO.= 1.200

.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000

CLN (YAW MOM, COEF, ARRAY(IPHI,JALPM,KAM))

MACH NO.= 1.960

AERODYNAMICS OF PARACHUTE

ANGLE OF ATTACK ARRAY (AALPPE(8))

.000	10.000	40.000	90.000	140.000	170.000	180.000	.000
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MACH NUMBER ARRAY (AAMP(8))

.000	10.000	.000	.000	.000	.000	.000	.000
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AXIAL COEFF. ARRAY (CCAP(8,8))

.550	.550	.000	.000	.000	.000	.000	.000
.500	.500	.000	.000	.000	.000	.000	.000
.300	.300	.000	.000	.000	.000	.000	.000
.100	.100	.000	.000	.000	.000	.000	.000
-.300	-.300	.000	.000	.000	.000	.000	.000
-.500	-.500	.000	.000	.000	.000	.000	.000
-.550	-.550	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000

NORMAL COEFF. ARRAY (CCNP(8,8))

.000	.000	.000	.000	.000	.000	.000	.000
.050	.050	.000	.000	.000	.000	.000	.000
.320	.320	.000	.000	.000	.000	.000	.000
1.000	1.000	.000	.000	.000	.000	.000	.000
.320	.320	.000	.000	.000	.000	.000	.000
.050	.050	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000

PITCH MOM. COEFF. ARRAY (CCMP(6,8))

.000	.000	.000	.000	.000	.000	.000	.000
-.050	-.050	.000	.000	.000	.000	.000	.000
-.320	-.320	.000	.000	.000	.000	.000	.000
-1.000	-1.000	.000	.000	.000	.000	.000	.000

-.320	-.320	.000	.000	.000	.000	.000
-.050	-.050	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000

[illegible]

TIME	X	XD	XDD	FX	CA	V	TENS	XP	XPD	XPDD	FAP	CDAP	CMP
T88	Y	YU	YDD	FZ	CN	AM	LT	YP	YD	YDD	FYP	CNP	AMP
T88	Z	ZU	ZDD	FZ	CV	DYPR	TPD	ZP	ZD	ZDD	FZP	TPB	DYPRP
T88	PSIE	PSIDE	PSIODE	GPSI	CLN	ALPE	OMKBE	PSIPE	PSIODE	PSPOUE	GPSIP	TZPR	ALPPE
GAME	THEE	THEDE	THEDEDE	QTHE	CLM	PHITE	OMYBE	THEPE	THEPDE	THPODE	QTHEP	TPDXB	GAPE
CHIE	PHIE	PHIDE	PHIODE	OPHI	CLL	PHIAE	OMZBE	K5	CLLP	CLMQ	CLNRY	TPDRB	PULAM
MPAL	MPAS	DND	OMAXPR	IXPB	IYPB	SPD	SP	SPRU	SPRL	TINT	TINRY	TFI	XPB01
.4200	20.	45.876	-7.625	-27309.	.049	545.28	113529.	96.	41.38	-13.98	-10339.	631.144	.000
0.	0.	.000	.000	0.	8.749	.523	12.471	0.	.00	.00	0.	.000	.469
-1195181.	18770.	-543.346	32.453	34862.	.000	196.37	116745.	18857.	-487.00	120.36	120362.	-2364.	157.77
0.	.000	.000	.000	0.	.000	92.710	.000	.000	.000	.000	0.	0.	.031
-85.174	7.536	15.705	77.686	1145181.	4.123	.000	-15.705	274.884	-1.108	-6.814	2364.	5494.	-85.143
.000	.000	.000	.000	0.	.000	.000	.000	19014.	.000	.000	.000	116616.	87.
6.5	2.6	45.21	22077.3	1768.5	37907.0	5427.9	1147.66	1879.10	8.00	.00000	.00000	.53811	552.30
.4300	20.	45.799	-8.117	-27659.	.043	544.94	124111.	97.	41.31	-1.42	-10798.	661.388	.000
0.	0.	.000	.000	0.	8.739	.523	12.803	0.	.00	.00	0.	.000	.469
-1121099.	18765.	-543.011	34.627	34358.	.000	196.16	127302.	18852.	-486.56	-26.00	125964.	-2538.	157.51
0.	.000	.000	.000	0.	.000	92.876	.000	.000	.000	.000	0.	0.	.024
-85.179	7.697	16.512	83.593	1121099.	4.041	.000	-16.512	274.877	-1.173	-6.216	2538.	6363.	-85.147
.000	.000	.000	.000	0.	.000	.000	.000	19692.	.000	.000	.000	127143.	87.
6.9	2.8	47.34	23116.0	1853.1	38360.0	5557.1	1202.78	1879.10	8.00	.00000	.00000	.53811	552.30
.4400	21.	45.716	-8.400	-28024.	.036	544.58	134125.	97.	41.34	7.03	-11317.	692.350	.000
0.	0.	.000	.000	0.	8.728	.523	13.116	0.	.00	.00	0.	.000	.469
-1095795.	18759.	-542.654	36.639	33821.	.000	195.93	137143.	18847.	-487.37	-126.36	132299.	-2710.	158.06
0.	.000	.000	.000	0.	.000	93.051	.000	.000	.000	.000	0.	0.	.016
-85.184	7.867	17.375	89.076	1095795.	3.954	.000	-17.375	274.864	-1.234	-5.921	2710.	7284.	-85.151
.000	.000	.000	.000	0.	.000	.000	.000	20272.	.000	.000	.000	136950.	87.
7.4	2.9	49.51	24217.8	1939.7	38832.1	5686.4	1259.00	1879.10	8.00	.00000	.00000	.53811	552.30
.4500	21.	45.631	-8.667	-28405.	.029	544.20	143220.	98.	41.44	11.10	-11882.	724.029	.000
0.	0.	.000	.000	0.	8.716	.522	13.401	0.	.00	.00	0.	.000	.471
-1069230.	18754.	-542.279	38.423	33255.	.000	195.69	145961.	18842.	-488.93	-178.32	139207.	-2890.	159.10
0.	.000	.000	.000	0.	.000	93.235	.000	.000	.000	.000	0.	0.	.008
-85.190	8.045	18.291	93.956	1069230.	3.863	.000	-18.291	274.852	-1.294	-6.171	2890.	8240.	-85.154
.000	.000	.000	.000	0.	.000	.000	.000	20752.	.000	.000	.000	145728.	87.
7.9	3.1	51.74	25386.3	2028.3	39323.8	5815.6	1316.51	1879.10	8.00	.00000	.00000	.53811	552.30
.4600	22.	45.543	-8.916	-28804.	.021	543.80	151200.	98.	41.55	11.04	-12474.	756.418	.000
0.	0.	.000	.000	0.	8.704	.522	13.651	0.	.00	.00	0.	.000	.473
-1041376.	18748.	-541.887	39.948	32663.	.000	195.44	153608.	18837.	-490.78	-185.40	146485.	3137.	160.33
0.	.000	.000	.000	0.	.000	93.429	.000	.000	.000	.000	0.	0.	.000
-85.196	8.233	19.252	98.149	1041376.	3.767	.000	-19.252	274.839	-1.374	-16.085	-3137.	9220.	-85.161
.000	.000	.000	.000	0.	.000	.000	.000	21143.	.000	.000	.000	163331.	87.
8.5	3.4	54.01	26601.1	2118.9	39835.8	5944.8	1375.31	1879.10	8.00	.00000	.00000	.53811	552.30
.4700	22.	45.452	-9.148	-29221.	.014	543.39	158017.	98.	41.65	8.06	-13073.	789.406	.000
0.	0.	.000	.000	0.	8.692	.521	13.865	0.	.00	.00	0.	.000	.474
-1012217.	18743.	-541.481	41.213	32047.	.000	195.18	160081.	18833.	-492.51	-155.75	153906.	3796.	161.49
0.	.000	.000	.000	0.	.000	93.632	.000	.000	.000	.000	0.	0.	.009
-85.202	8.430	20.252	101.453	1012217.	3.666	.000	-20.252	274.824	-1.545	-16.043	-3796.	10212.	-85.167
.000	.000	.000	.000	0.	.000	.000	.000	21456.	.000	.000	.000	159755.	86.
9.0	3.6	56.33	27841.4	2211.5	40368.4	6074.1	1435.41	1879.10	8.00	.00000	.00000	.53811	552.30

[illegible]

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